

Trig 3.1

Use algebraic tests to determine whether a graph is symmetrical

Classify functions as even or odd

	(a, b)	
reflection →	x-axis	$(a, -b)$
rotation	y-axis	$(-a, b)$
	$y = x$	(b, a)
translation	$y = -x$	$(-b, -a)$
point symmetry (rotation)		

odd origin $(-a, -b)$

line symmetry (reflection)

activity: letters

$$x = \pm \sqrt{12 - 8y^2}$$

$$a = \pm \sqrt{12 - 8b^2}$$

$$a = \pm \sqrt{12 - 8b^2}$$

$$-a = \pm \sqrt{12 - 8b^2}$$

	(a, b)	
x-axis	(a, -b)	yes
y-axis	(-a, b)	yes

$$x^2 = 12 - 8y^2$$

$$\frac{x^2}{12} - \frac{8y^2}{12} = 1$$

$$y^2 = \sqrt{-\frac{1}{8}x^2 + 1.5}$$

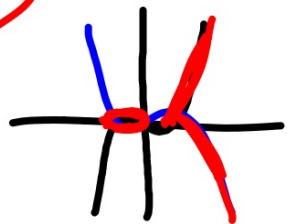
$$y = \sqrt{-\frac{1}{8}x^2 + 1.5}$$

$$y = \sqrt{-0.125x^2 + 1.5}$$

$$37. \quad |y| = x^3 - x$$

(a, b)

$$|b| = a^3 - a$$



x-axis
 $(a, -b)$
yes

$$|b| = a^3 - a$$

y-axis
 $(-a, b)$

$$|b| = -a^3 + a$$

$$y = x^3 - x$$

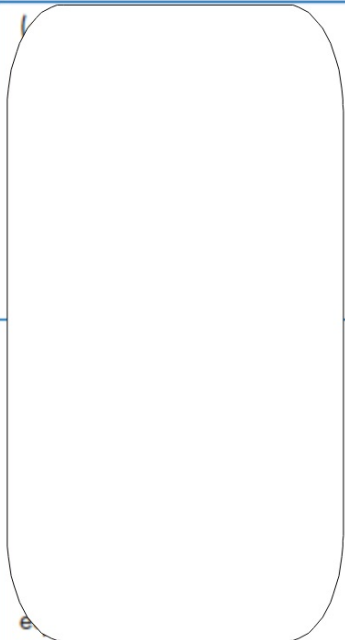
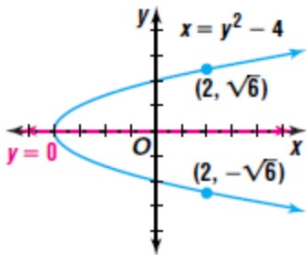
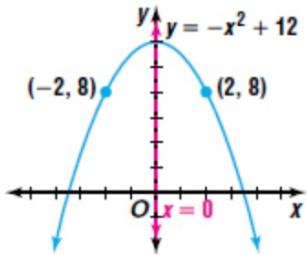
Symmetry
with Respect
to the Origin

The graph of a relation S is symmetric with respect to the origin if and only if $(a, b) \in S$ implies that $(-a, -b) \in S$.

$(a, b) \in S$ means the ordered pair (a, b) belongs to the solution set S .

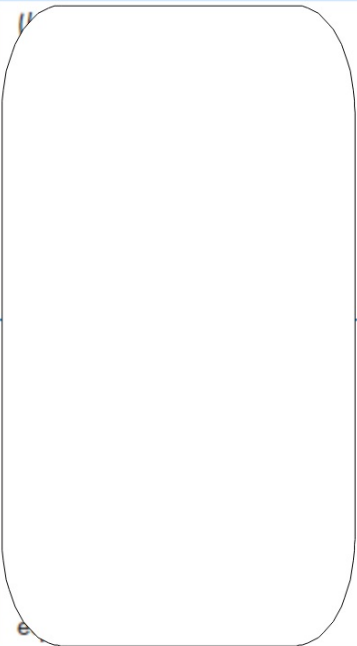
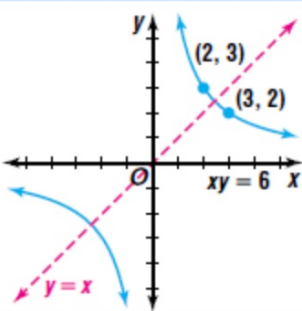
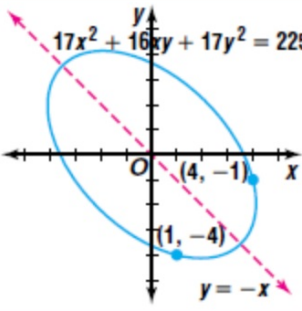
(a, b) and $(-a, -b)$

"Rotation"= symmetric with origin

Symmetry with Respect to the:	Definition and Test	Example
x-axis		
y-axis		

(a,b) maps to

(a,b) maps to

Symmetry with Respect to the Line:	Definition and Test	Example
$y = x$		
$y = -x$		

(a,b) maps to

(a,b) maps to

Test each possibility: yes or no

2 Determine whether the graph of ~~$x^2 + 2$~~ is symmetric with respect to the x -axis, y -axis, the line $y = x$, the line $y = -x$, or none of these.

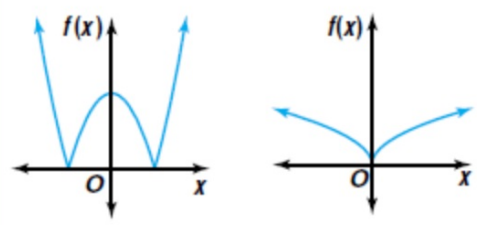
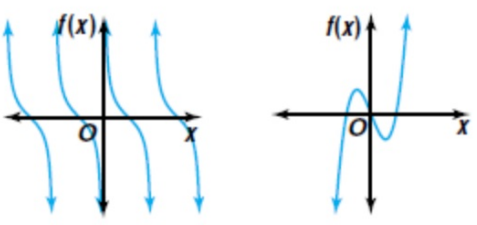
a) b) c) d)

★ $xy=6$

★ $y=x^2+6$

$$x^2+y^2=25$$

$$x=y^2-1$$

even functions	odd functions
	
symmetric with respect to the y-axis	symmetric with respect to the origin

reflect y-axis

rotate
180