

Trig 3.5

Determine whether a function is continuous

Identify end behavior of a function

Determine whether a function is increasing or decreasing on an interval

continuous

discontinuous

end behavior (*algebra 2*)

increasing

decreasing

interval

infinite discontinuity

jump discontinuity

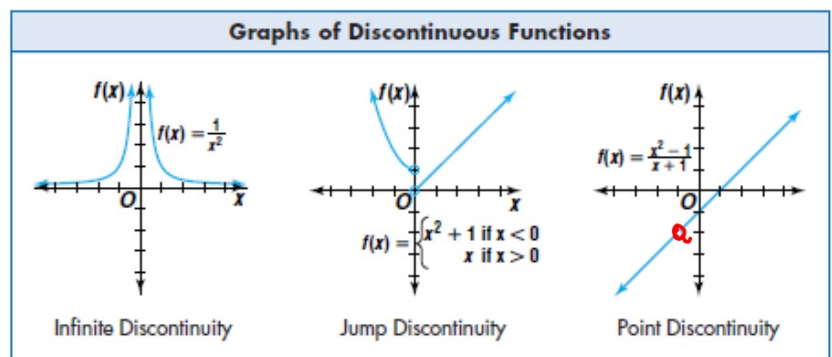
point discontinuity

$$x^2 - 1 = (x+1)(x-1)$$

$$x \neq 1$$

$$x+1=0$$

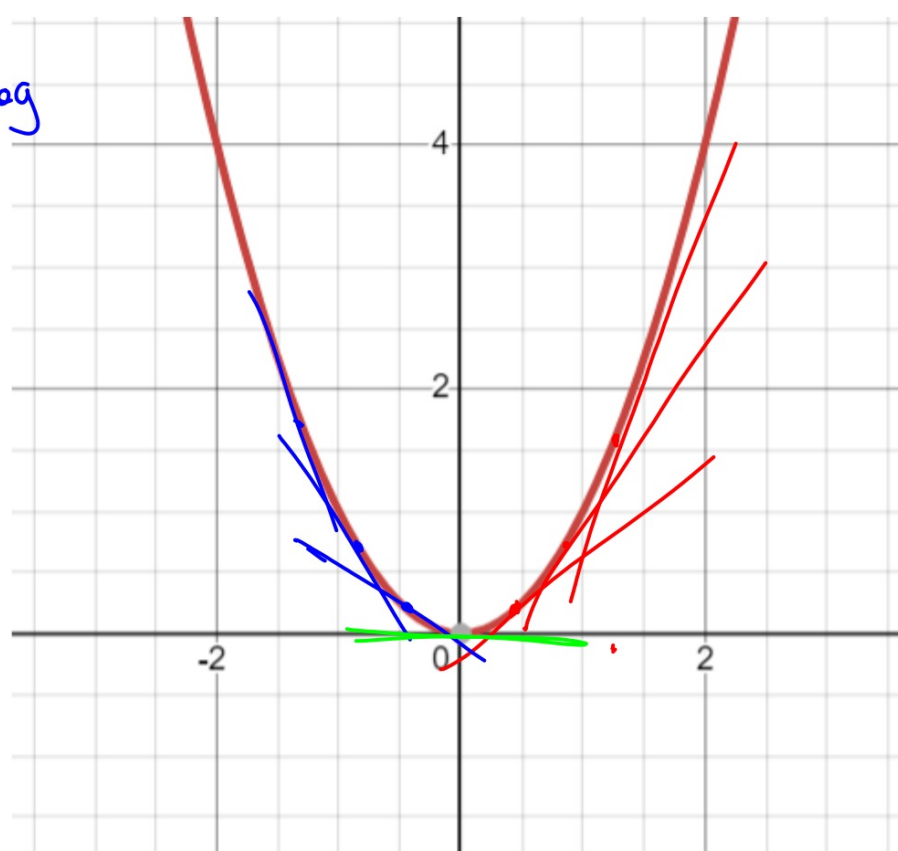
$$x=-1$$



graphing calculators--table

Related to slope...
Increasing function ^{pos.}
Decreasing function
(can be 0 at times) ^{neg}

Slope is changing
because nonlinear



Start with $x > 0$ etc.

Translate answers to "interval notation"

Graph each function. Determine the interval(s) for which the function is increasing and the interval(s) for which the function is decreasing.

26. $y = x^3 + 3x^2 - 9x$

dec. always $(-\infty, \infty)$

27. $y = -x^3 - 2x + 1$

Interval notation
open/closed

$(-\infty, -3)$

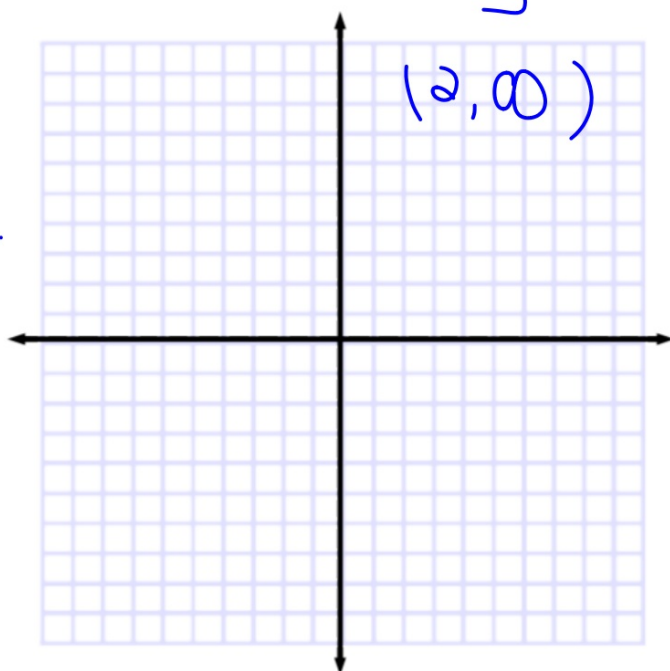
incr. $x < -3$

$[-3, 2]$

→ dec. $-3 \leq x \leq 2$

incr. $x > 2$

$(2, \infty)$



Graphing calc?

- 4** Graph each function. Determine the interval(s) on which the function is increasing and the interval(s) on which the function is decreasing.

a. $f(x) = 3 - (x - 5)^2$

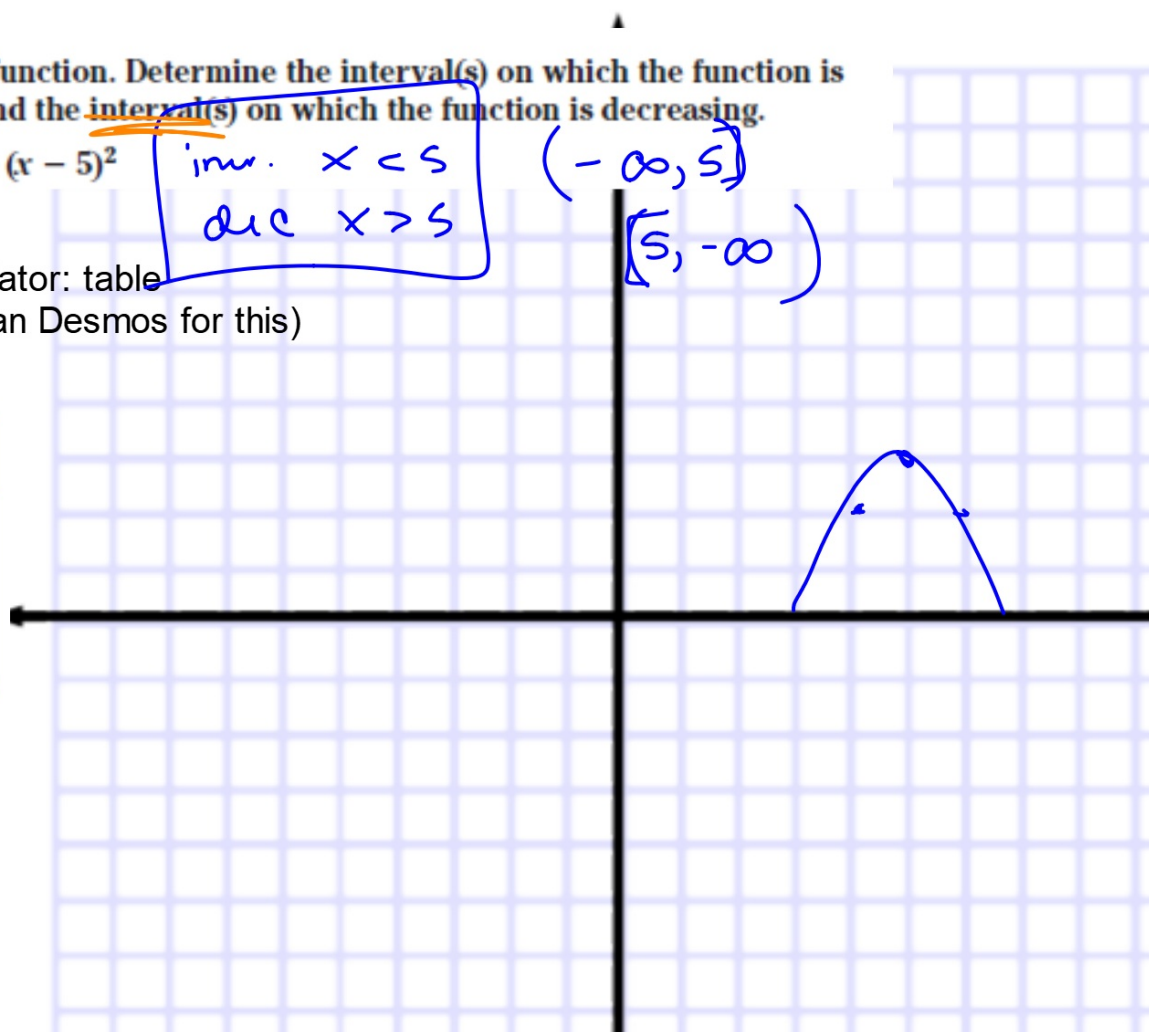
incr. $x < 5$ $(-\infty, 5]$
dec $x > 5$ $[5, -\infty)$

Graphing calculator: table
(gc is easier than Desmos for this)



**Graphing
Calculator
Tip**

By watching the x - and y -values while using the **TRACE** function, you can determine approximately where a function changes from increasing to decreasing and vice versa.



14. $f(x) = \frac{x+3}{(x-3)^2}; x = \underline{\underline{-3}}$

Continuous?

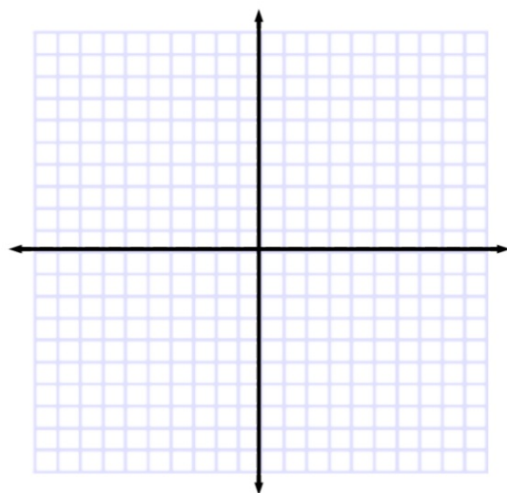
$$\frac{-3+3}{(-3-3)^2} = \frac{0}{36} = 0$$

16. $f(x) = \begin{cases} 3x + 5 & \text{if } x \leq -4 \\ -x + 2 & \text{if } x > -4 \end{cases}; x = -4$

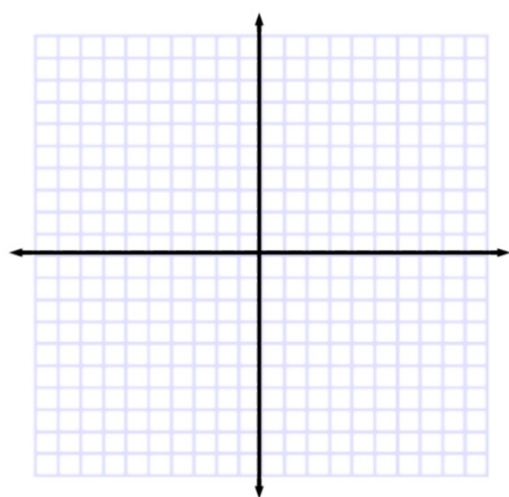
Continuous?

Describe the end behavior

20. $y = x^3 + 2x^2 + x - 1$



22. $f(x) = x^{10} - x^9 + 5x^8$



28. $f(x) = \frac{1}{x+1} - 4$

