

Trig 9.1

Graph polar coordinates

Graph polar equations

Determine distance between 2 polar coordinates

$P(1, \sqrt{3})$

ordered pair

$\begin{matrix} + & + \\ + & - \\ - & + \\ - & - \end{matrix}$

Cartesian coordinates

polar coordinate system

$(5, 37^\circ)$

polar axis

pole (origin)

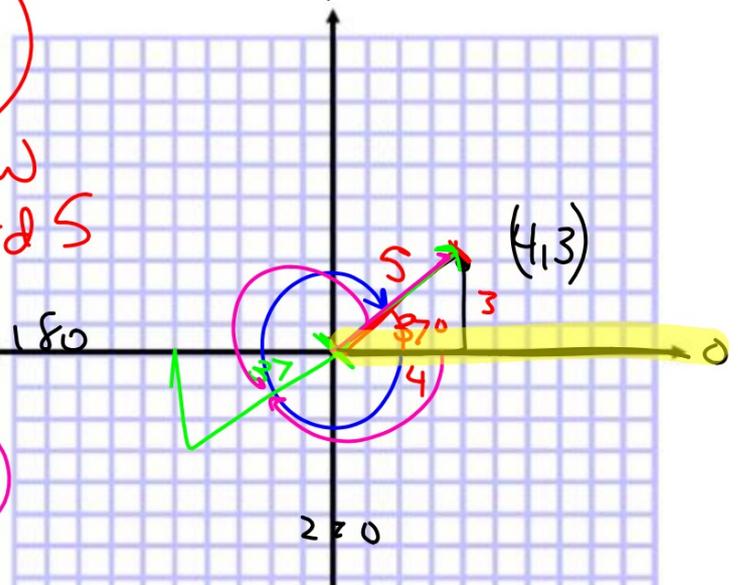
polar equation

polar graph

distance

$(-5, -143^\circ)$   
 $(5, -323^\circ)$   
 $(-5, 217^\circ)$

$4^2 + 3^2 = h^2 \quad \tan^{-1}\left(\frac{3}{4}\right)$   
 $S = h \cos \theta$



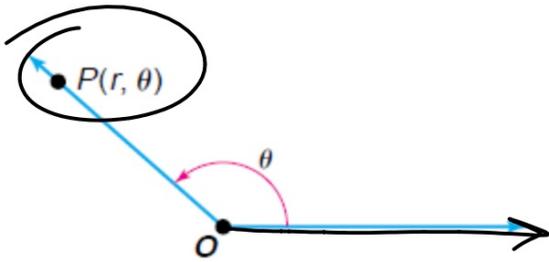
Floor graphs

1. rotate

2. step (forward)

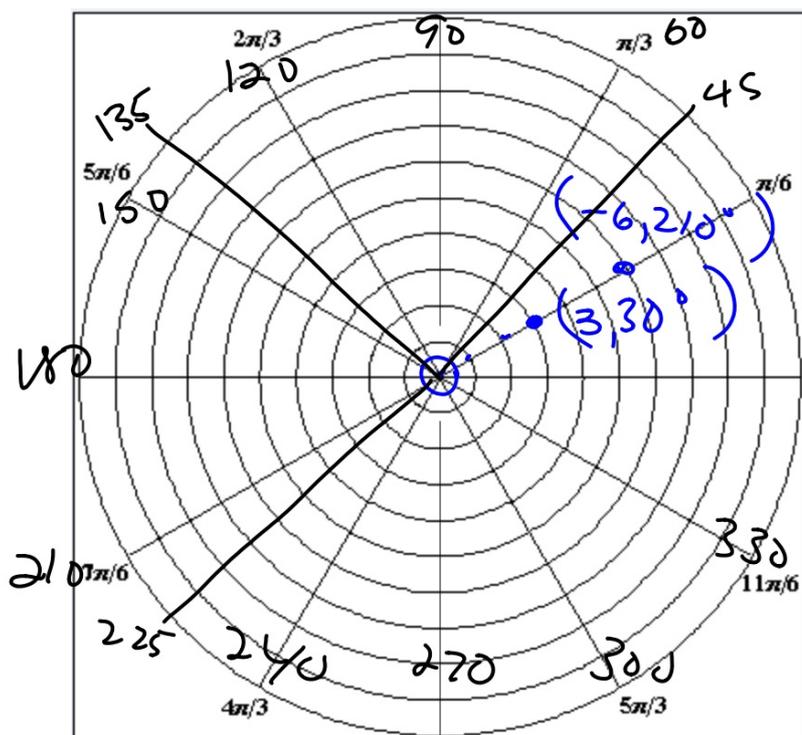
CCW(+)

CW-



But what if the angle is negative?

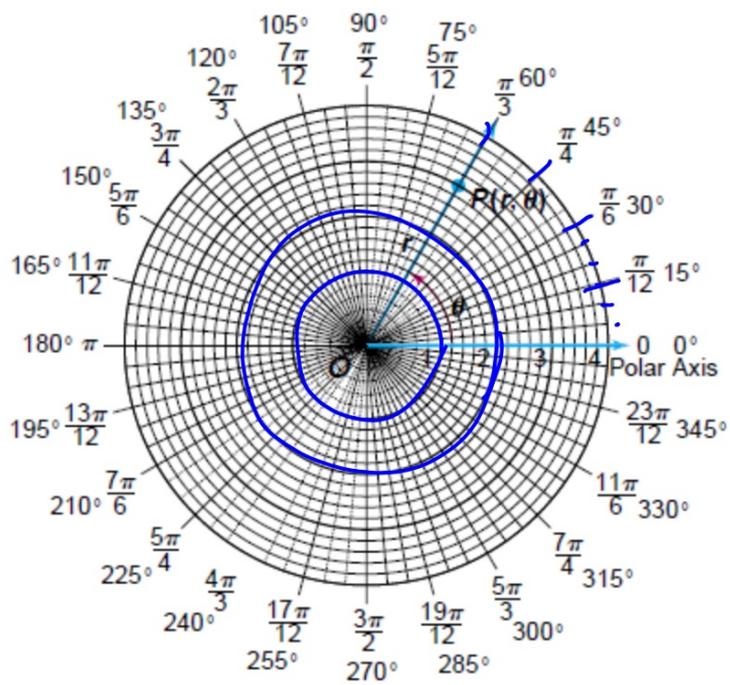
Floor graphs



$30 \quad (3, 30^\circ)$

$0 \quad (360)$

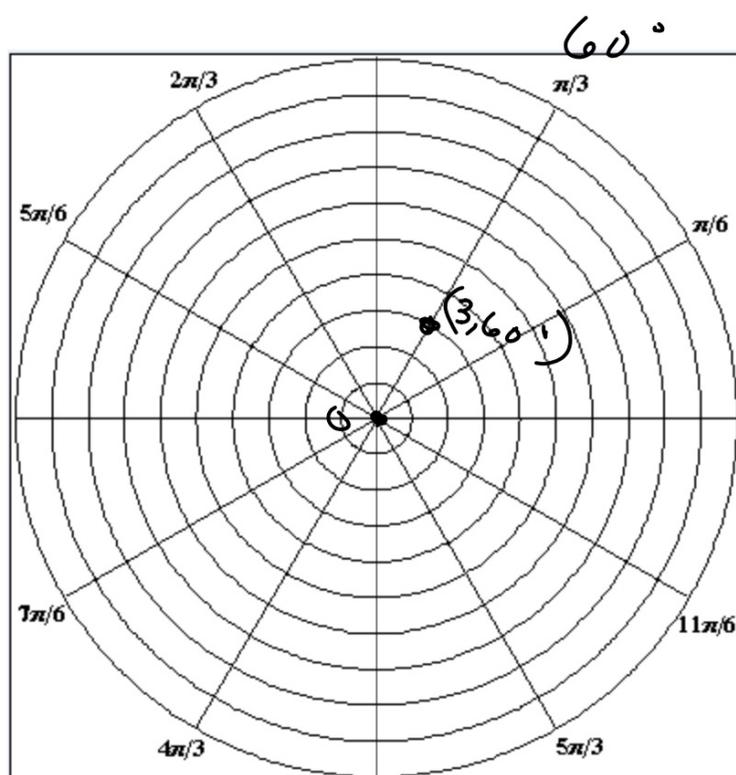
$(-6, 210^\circ)$



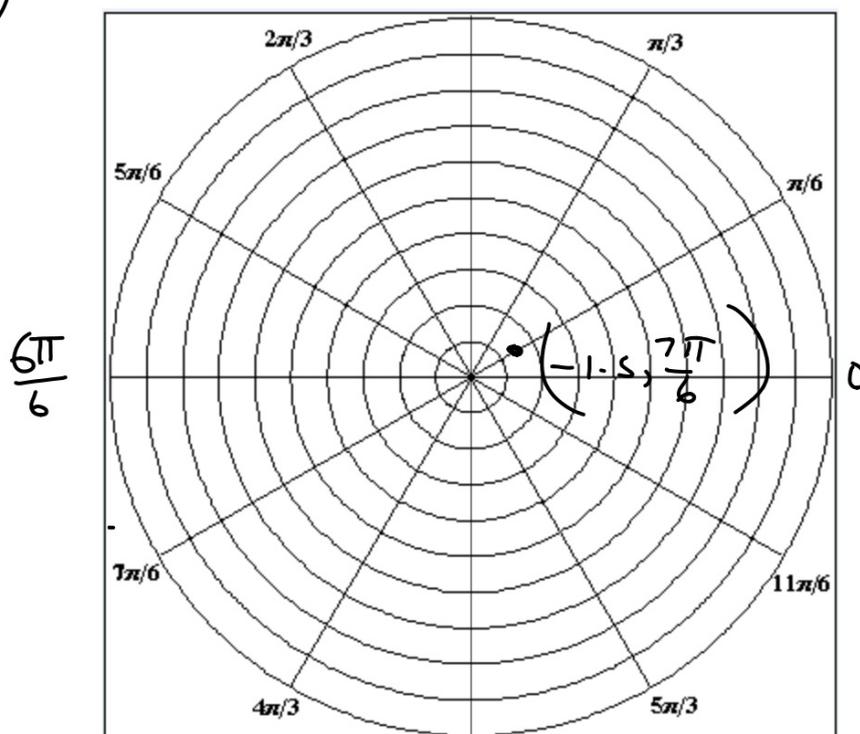
What if the distance is negative?

*back up*

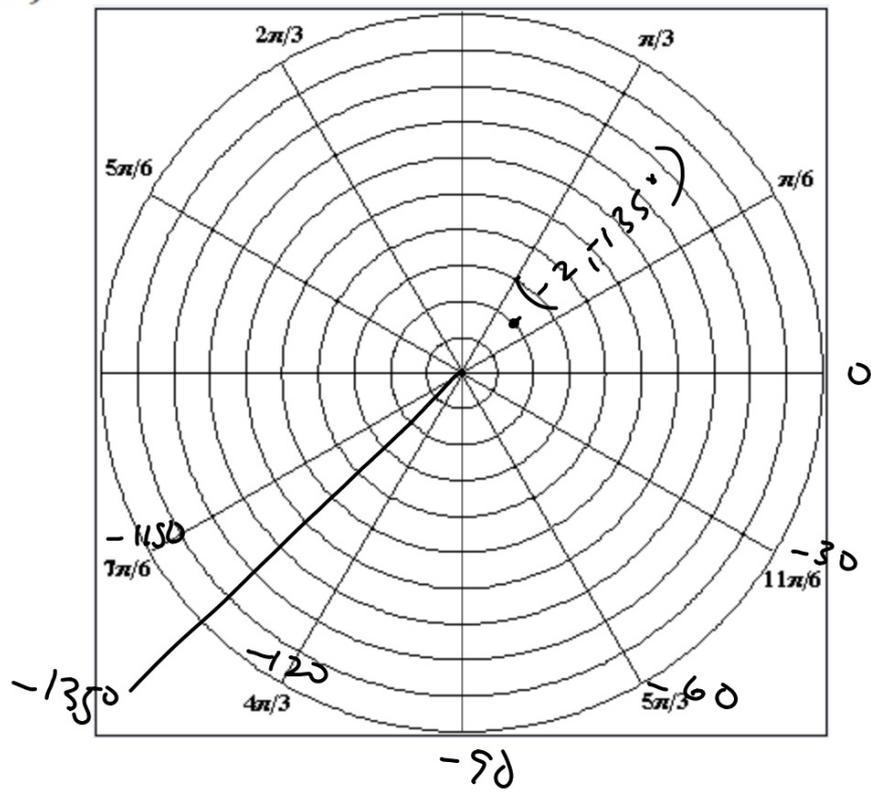
- 1 Graph each point.  
a.  $P(3, 60^\circ)$



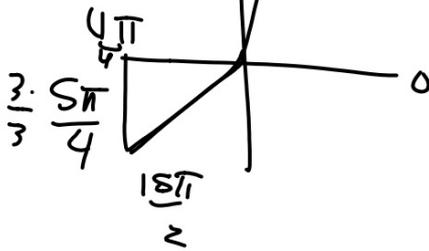
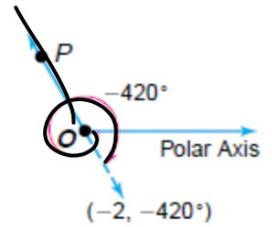
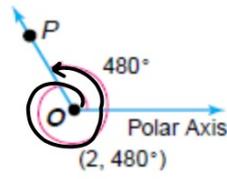
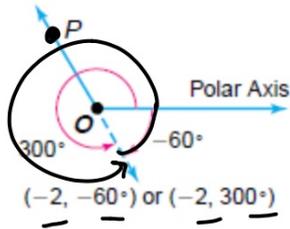
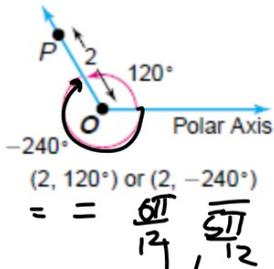
b.  $Q\left(\underline{-1.5}, \frac{7\pi}{6}\right)$



2 Graph  $R(-2, -135^\circ)$ . CW

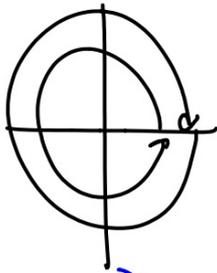


Name the point 4 ways:  
Floor graphs

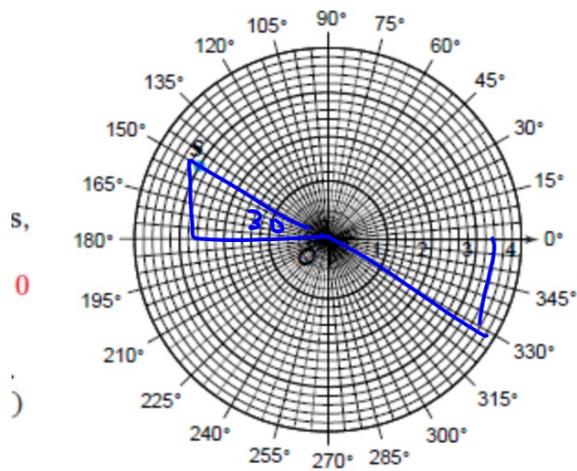


$$\begin{matrix} -360 \\ -60 \\ (-2, -420^\circ) \end{matrix}$$

- 3 Name four different pairs of polar coordinates that represent point  $S$  on the graph with the restriction that  $-360^\circ \leq \theta \leq 360^\circ$ .

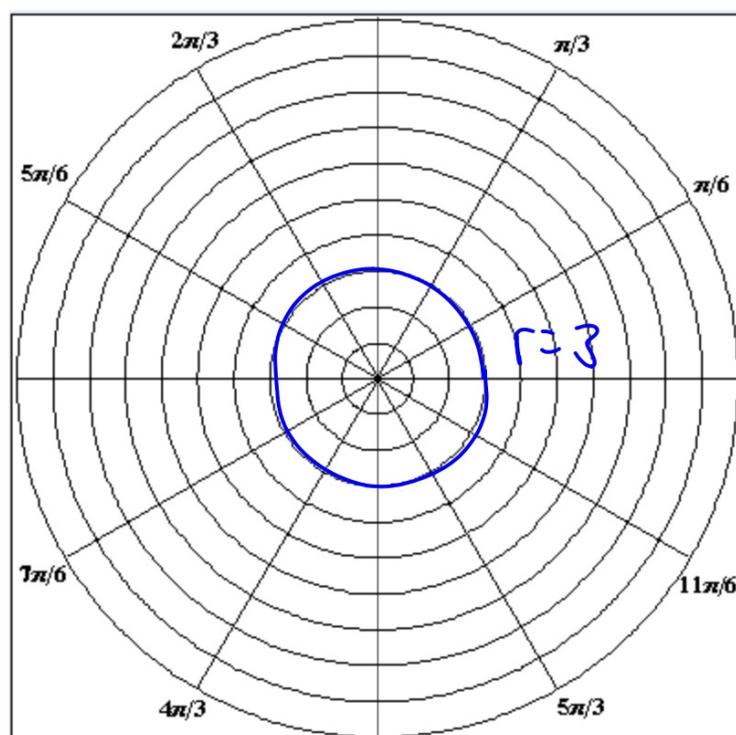


$$\begin{aligned} & (3, 150^\circ) \\ & (3, -210^\circ) \\ & (-3, -30^\circ) \\ & (-3, 330^\circ) \end{aligned}$$



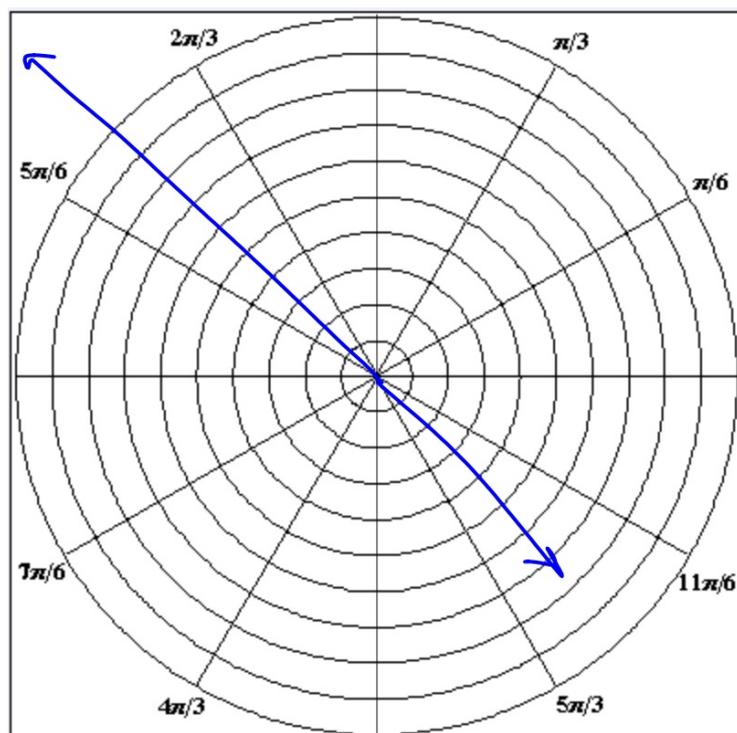
**4** Graph each polar equation.

a.  $r = 3$



b.  $\theta = \frac{3\pi}{4}$

$\theta = 135^\circ$



L.O.C.  $a^2 = b^2 + c^2 - 2bc \cos A$

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Distance  
Formula in  
Polar Plane

If  $P_1(r_1, \theta_1)$  and  $P_2(r_2, \theta_2)$  are two points in the polar plane, then

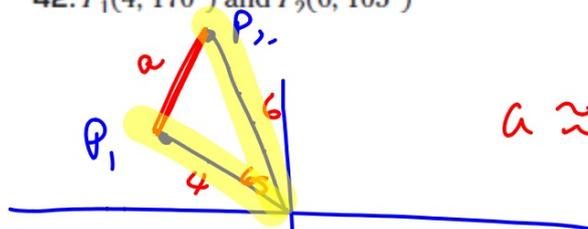
$$P_1P_2 = \sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos(\theta_2 - \theta_1)}$$

Not sure this formula is worthy: comes from law of cosines

Find the distance between the points with the given polar coordinates.

Why  $x_2 - x_1$ ?

42.  $P_1(4, 170^\circ)$  and  $P_2(6, 105^\circ)$



$a \approx 5.6$

$$a^2 = 4^2 + 6^2 - (2 \cdot 4 \cdot 6 \cos 65)$$

$$a^2 = 16 + 36 - 20.2857$$

$$\underline{a^2 = 31.7143}$$

