

## Geometry 2.5

Identify and use basic postulates about points, lines, planes

Write paragraph proofs

postulate (axiom)

theorem

deductive argument

paragraph proof (informal)

2-column proof

working backward (CSI)




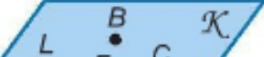
Reminder: projects due (APPS geometry) Tuesday EOD

reflections due Thurs. in class

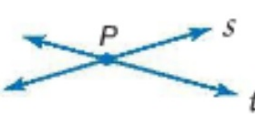
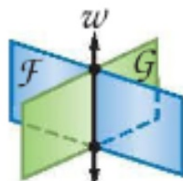
see Fri. notes for reflection requirements

Postulate: Self-evident  
 Basic idea/example about a  
 point, line, plane...  
 Sort of like a definition...  
 "...duh"  
 It just IS. Like gravity.

**1 Points, Lines, and Planes** A **postulate** or **axiom** is a statement that is accepted as true without proof. Basic ideas about points, lines, and planes can be stated as postulates.

Postulates Points, Lines, and Planes		
Words	Example	
<b>2.1</b> Through any two points, there is exactly one line.		Line $n$ is the only line through points $P$ and $R$ .
<b>2.2</b> Through any three noncollinear points, there is exactly one plane.		Plane $K$ is the only plane through noncollinear points $A$ , $B$ , and $C$ .
<b>2.3</b> A line contains at least two points.		Line $n$ contains points $P$ , $Q$ , and $R$ .
<b>2.4</b> A plane contains at least three noncollinear points.		Plane $K$ contains noncollinear points $L$ , $B$ , $C$ , and $E$ .

**KeyConcept** Intersections of Lines and Planes

Words	Example	
<b>2.6</b> If two lines intersect, then their intersection is exactly one point.		Lines $s$ and $t$ intersect at point $P$ .
<b>2.7</b> If two planes intersect, then their intersection is a line.		Planes $\mathcal{F}$ and $\mathcal{G}$ intersect in line $w$ .

## **Required** elements:

Given: *starting point*

Prove: *where you end up*

Drawing (if applicable):

→ Chain of reasoning (explain) using  
statements & reasons

WB 2.5 prac.

$$\text{Given: } 5x - 13 = 2$$

$$\text{To Prove: } x = 3$$

Given  $5x - 13 = 2$

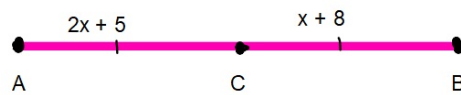
Prove  $x = 3$

Start with  $5x - 13 = 2$  and  
add 13 to both sides:  $\frac{5x}{5} = \frac{15}{5}$ .  
Divide both sides by 5 so  $x = 3$ .

Book

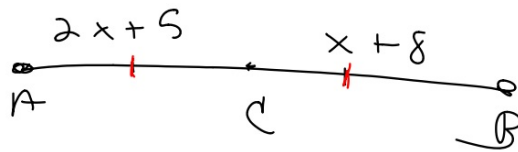
Given C is the midpoint of AB

Prove  $x=3$



Given C is mp of AB.

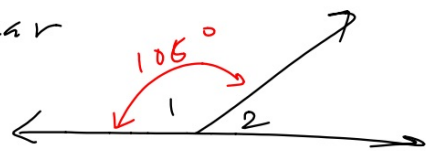
Prove  $x = 3$



If C is mp then  $AC = BC$  so  $2x + 5 = x + 8$ .

Zero pair X's so  $x + 5 = 8$ . add  $-5$  to both sides so  $x = 3$ .

Given  $\angle 1$  and  $\angle 2$  form linear pair.  
p.g.  $m\angle 1 = 105^\circ$



Prove  $m\angle 2 = 75^\circ$

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Since  $\angle 1$  &  $\angle 2$  are L.P. their sum is  $180^\circ$

So  $m\angle 1 + m\angle 2 = 180^\circ$ . If  $m\angle 1 = 105^\circ$  then

$105^\circ + m\angle 2 = 180^\circ$  Subtract 105 from both  
 $\begin{array}{r} 105^\circ + m\angle 2 = 180^\circ \\ -105 \quad \quad -105 \\ \hline \end{array}$

so  $m\angle 2 = 75^\circ$