Geometry 8.2

Use the pythagorean theorem*

Use the converse of the pythagorean theorem

Prove the pythagorean theorem

leg

hypotenuse

converse ⟷

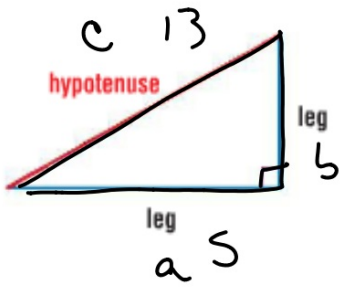
integer

pythagorean triple

*8th grade standard

$a^2 + b^2 = c^2$

$5^2 + b^2 = 13^2$

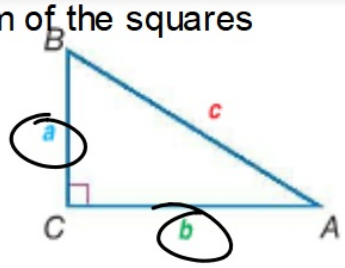


Theorem 8.4 Pythagorean Theorem

Words In a right triangle, the sum of the squares of the lengths of the legs is equal to the square of the length of the hypotenuse.

Symbols If $\triangle ABC$ is a right triangle with right angle C, then $a^2 + b^2 = c^2$.

Sum of the squares



$leg^2 + leg^2 = hyp^2$

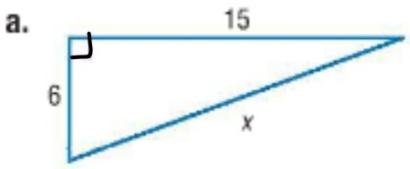
https://www.youtube.com/watch?v=m5Xy3_TOnbs

Exact value or round off?

Example 1 Find Missing Meast

Find x.

a.



$6^2+15^2=x^2$

$36+225=x^2$

$\sqrt{261}=\sqrt{x^2}$

261

$3 \wedge 87$

$3 \wedge 29$

$3\sqrt{29}$

$x=\sqrt{261}$ 16.16

$3\sqrt{29}$

$\sqrt{9.29}$

40

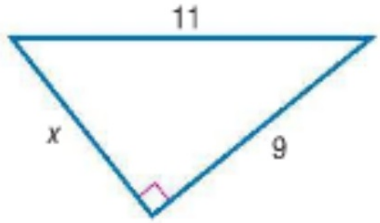
$4 \wedge 10$

$2 \wedge 2$ $2 \wedge 5$

$\sqrt{4.10}$

$2\sqrt{10}$

b.



$x^2+9^2=11^2$

$x^2+81=121$

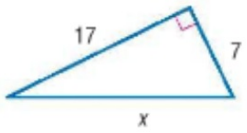
$-81 \quad -81$

$\sqrt{x^2}=\sqrt{40}$

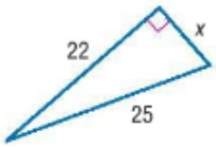
$x=\sqrt{40}$

GuidedPractice

1A.



1B.



$17^2+7^2=x^2$

$289+49=x^2$

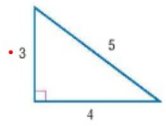
$\sqrt{338}=\sqrt{x^2}$

338

2 169

13 13

$\sqrt{(169)2}=13\sqrt{2}$



$3^2+4^2 \neq 5^2$

$9+16=25$

25

primitive (parent)
scale factor...
must be whole numbers

StudyTip

Pythagorean Triples

If the measures of the sides of any right triangle are *not* whole numbers, the measures do not form a Pythagorean triple.

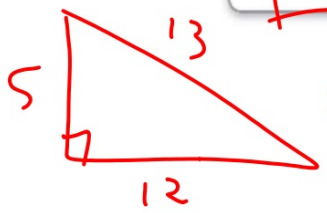
whole

primitive

KeyConcept Common Pythagorean Triples

3, 4, 5	5, 12, 13	8, 15, 17	7, 24, 25
6, 8, 10	10, 24, 26	16, 30, 34	14, 48, 50
9, 12, 15	15, 36, 39	24, 45, 51	21, 72, 75
$3x, 4x, 5x$	$5x, 12x, 13x$	$8x, 15x, 17x$	$7x, 24x, 25x$

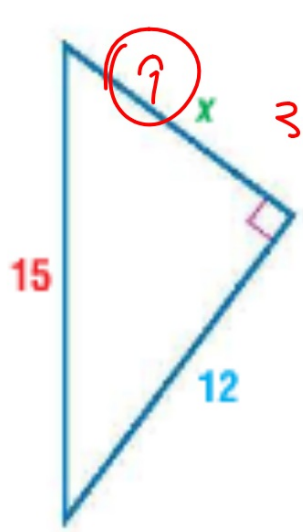
The largest number in each triple is the length of the hypotenuse.



$5^2+12^2=13^2$

Example 2 Use a Pythagorean Triple

Use a Pythagorean triple to find x. Explain your reasoning.



?, 12, 15

3·3 3·4 3·5

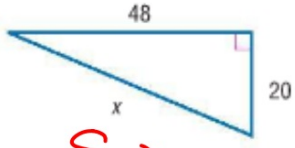
Maybe it is a PT.

Try factoring out a GCF

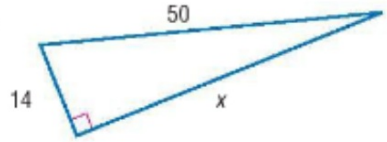
Try dividing out GCF to find the primitive (parent)...

20, 48 ? 52
4.5 4.12 4.13

2A.



2B.



14 ? 50
2.7 2.24 2.25
48

Standardized Test Example 3 Use the Pythagorean Theorem

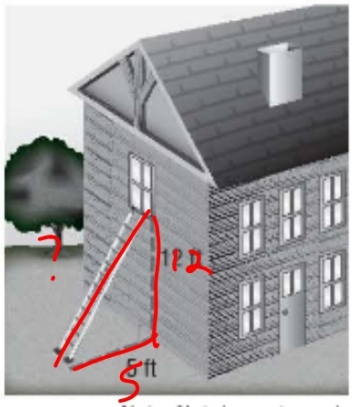
Damon is locked out of his house. The only open window is on the second floor, which is 12 feet above the ground. He needs to borrow a ladder from his neighbor. If he must place the ladder 5 feet from the house to avoid some bushes, what length of ladder does Damon need?

A 7 feet

C 13 feet

B 11 feet

D 17 feet



Note: Not drawn to scale

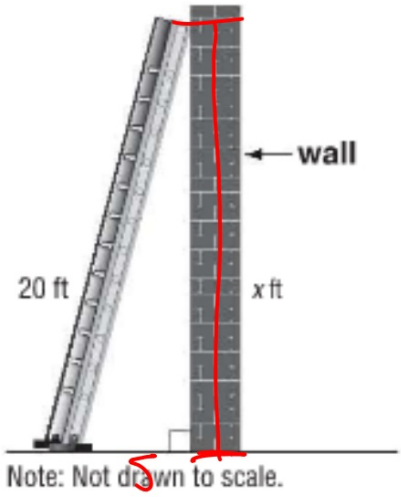
GuidedPractice

$5^2 + x^2 = 20^2$

$25 + x^2 = 400$

$x^2 = 375$

3. According to your company's safety regulations, the distance from the base of a ladder to a wall that it leans against should be at least one fourth of the ladder's total length. You are given a 20-foot ladder to place against a wall at a job site. If you follow the company's safety regulations, what is the maximum distance x up the wall the ladder will reach, to the nearest tenth?



Note: Not drawn to scale.

F 12 feet

G 19.4 feet

H 20.6 feet

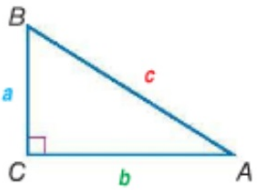
J 30.6 feet

2 Converse of the Pythagorean Theorem The converse of the Pythagorean Theorem also holds. You can use this theorem to help you determine whether a triangle is a right triangle given the measures of all three sides.

Theorem 8.5 Converse of the Pythagorean Theorem

Words If the sum of the squares of the lengths of the shortest sides of a triangle is equal to the square of the length of the longest side, then the triangle is a right triangle.

Symbols If $a^2 + b^2 = c^2$, then $\triangle ABC$ is a right triangle.



You will prove Theorem 8.5 in Exercise 35.

StudyTip

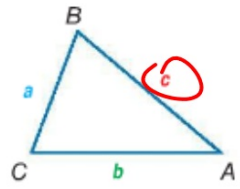
Determining the Longest Side If the measures of any of the sides of a triangle are expressed as radicals, you may wish to use a calculator to determine which length is the longest.

You can also use side lengths to classify a triangle as acute or obtuse.

Theorems Pythagorean Inequality Theorems

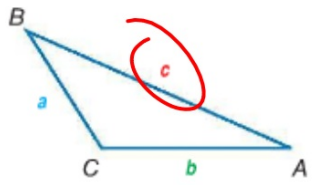
8.6 If the square of the length of the longest side of a triangle is less than the sum of the squares of the lengths of the other two sides, then the triangle is an acute triangle.

Symbols If $c^2 < a^2 + b^2$, then $\triangle ABC$ is acute.



8.7 If the square of the length of the longest side of a triangle is greater than the sum of the squares of the lengths of the other two sides, then the triangle is an obtuse triangle.

Symbols If $c^2 > a^2 + b^2$, then $\triangle ABC$ is obtuse.



You will prove Theorems 8.6 and 8.7 in Exercises 36 and 37, respectively.

a^2+b^2 = perfect amount: right triangle
If longest side is less than perfect: acute
If longest side is more than perfect: obtuse

1. figure out p
2. compare

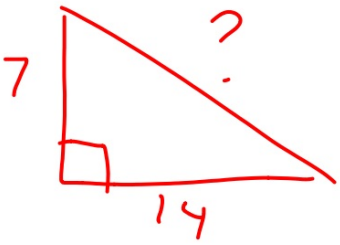
Is it a triangle at all?
What kind of triangle?

Example 4 Classify Triangles

Determine whether each set of numbers can be the measures of the sides of a triangle. If so, classify the triangle as *acute*, *right*, or *obtuse*. Justify your answer.

a. 7, 14, 16

Obtuse



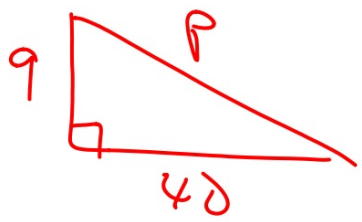
$7^2+14^2=p^2$

$49+196=$

$\sqrt{245}=p$

$p \approx 15.65$

b. 9, 40, 41



$9^2 + 40^2 = p^2$

$1681 = p^2$

41

L: 3.46 L: 5.66 6.71

GuidedPractice

4A. 11, 60, 61

4B. $2\sqrt{3}, 4\sqrt{2}, 3\sqrt{5}$

4C. 6.2, 13.8, 20

44

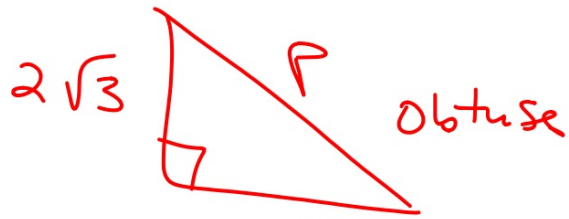
4 ^ 11

2 2

$\sqrt{4 \cdot 11}$

$2\sqrt{11}$

6.6.3



$(2\sqrt{3})^2 + (4\sqrt{2})^2 = p^2$

$2 \cdot \sqrt{3} \cdot 2\sqrt{3}$ $\quad 4\sqrt{2} \cdot 4\sqrt{2}$

$4 \cdot 3$ $\quad 16 \cdot 2$

$\sqrt{44} = p^2$ $\quad 12 + 32 = p^2$

$44 = p^2$

pss2

9-33 odd

38-40