

Algebra 2 Ch. 5 Review
Quiz 5.7-5.8
Tomorrow: test Ch. 5

5-1 Operations with Polynomials

Simplify. Assume that no variable equals 0.

$$11. \frac{14x^4y}{2x^3y^5}$$

~~$x \times x \times x \times y$~~

~~$x \times x \times y \times y \times y \times y$~~

$$7 \frac{x}{y^4} \quad \cancel{x} \cancel{y}^{-4}$$

* Before Christmas

$$(m+p)(m^2-2mp+p^2) \qquad \qquad *$$

5-2 Dividing Polynomials

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Simplify.

$$17. \frac{12x^4y^5 + 8x^3y^7 - 16x^2y^6}{(4xy^5)}$$

$$\frac{12x^4y^5}{4xy^5} + \frac{8x^3y^7}{4xy^5} - \frac{16x^2y^6}{4xy^5}$$

$$3x^3 + 2x^2y^2 - 4xy$$

$$19. \frac{(a^4 + 5a^3 + 2a^2 - 6a + 4)(a + 2)^{-1}}{3a + 2} *$$



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5-3 Polynomial Functions

State the degree and leading coefficient of each polynomial in one variable. If it is not a polynomial in one variable, explain why.

22. $5x^6 - 3x^4 + x^3 - 9x^2 + 1$

Find $p(-2)$ and $p(x + h)$ for each function.

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25. $p(x) = x^2 + 2x - 3$

5-4 Analyzing Graphs of Polynomial Functions

Complete each of the following.

- a. Graph each function by making a table of values.
- b. Determine the consecutive integer values of x between which each real zero is located.
- c. Estimate the x -coordinates at which the relative maxima and minima occur.

28. $h(x) = x^3 - 4x^2 - 7x + 10$

$$x = -2$$

$$x = 1$$

$$x = 5$$

$$4 < x < 5$$

Use technology

Show ordered pairs on your graph

Make sure that you answer the question

R max $x = -1$
R min $x = 3$

5-5 Solving Polynomial Equations

Factor completely. If the polynomial is not factorable, write *prime*.

34. $a^4 - 16$

$$\mathbf{36.} \ 54x^3y - 16y^4$$

Solve each equation.

38. $x^3 + 2x^2 - 35x = 0$

5-6 The Remainder and Factor Theorems

Use synthetic substitution to find $f(-2)$ and $f(4)$ for each function.

41. $f(x) = x^2 - 3$

Given a polynomial and one of its factors, find the remaining factors of the polynomial.

45. $3x^3 + 20x^2 + 23x - 10$; $x + 5$

5-7 Roots and Zeros

State the possible number of positive real zeros, negative real zeros, and imaginary zeros of each function.

48. $f(x) = -2x^3 + 11x^2 - 3x + 2$

\oplus 3, 1

\ominus —

| | + | - | imag | total |
|---|---|---|------|-------|
| 3 | 0 | - | | 3 |
| 1 | 0 | 2 | | 3 |

5-8 Rational Zero Theorem

Find all of the zeros of each function.

53. $f(x) = x^3 + 4x^2 + 3x - 2$

(+) 1 $\frac{\pm 1, 2}{\sqrt{}}$

(-) 2, 0 $\begin{array}{r} -2 \\ \hline 1 \quad 4 \quad 3 \quad -2 \end{array}$

$$\begin{array}{r} x^2 + 2x - 1 \quad \begin{array}{r} \downarrow \quad -2 \quad -4 \quad 2 \\ \hline 1 \quad 2 \quad -1 \quad 0 \end{array} \end{array}$$

$$x = -2 \pm \sqrt{4 - 4 \cdot 1 \cdot -1}$$

$$x = -2 \pm \frac{\sqrt{8}}{2}$$

$$\begin{aligned} x &= -2 \\ x &= -1 + \sqrt{2} \\ x &= -1 - \sqrt{2} \end{aligned}$$

$$\begin{array}{r} 8 \\ 4^2 \\ 2^2 \end{array}$$

$$\begin{aligned} x &= \frac{-2 \pm 2\sqrt{2}}{2} \\ &= -1 \pm \frac{2\sqrt{2}}{2} \\ &= -1 \pm \sqrt{2} \end{aligned}$$

$$\begin{array}{r}
 x^2 + y \\
 x - 5 \\
 \hline
 -5x^2 - 20 \\
 x^3 \quad yx \\
 \hline
 (x-5)(x^2 + y) \\
 (x-5)(x-2i)(x+2i) = 0
 \end{array}
 \quad
 \begin{array}{r}
 x-2i \\
 x+2i \\
 \hline
 x^2 - 4i^2
 \end{array}$$