

Algebra 1      7.7

Identify and generate geometric sequences

Relate geometric sequences to exponential functions  
sequence

arithmetic sequence (3.5)    +

geometric sequence    X

common ratio    r

whiteboards

Quiz 7.5-7.6

**KeyConcept**  $n$ th term of a Geometric Sequence

The  $n$ th term  $a_n$  of a geometric sequence with first term  $a_1$  and common ratio  $r$  is given by the following formula, where  $n$  is any positive integer and  $a_1, r \neq 0$ .

$$a_n = a_1 r^{n-1}$$

(first)(1 less r)



**Example 3** Find the  $n$ th Term of a Geometric Sequence

a. Write an equation for the  $n$ th term of the sequence  $-6, 12, -24, 48, \dots$

$$-6(?)=12$$

find  $a_1$   
find  $r$   
answer the question

$$a_n = (-6)(-2)^{n-1}$$

$$\begin{aligned} a_{10} &= (-6)(-2)^9 \\ &= (-6) \cdot (-2)^9 \\ &= 3072 \end{aligned}$$

### Guided Practice

3. Write an equation for the  $n$ th term of the geometric sequence 96, 48, 24, 12, ... .  
Then find the tenth term of the sequence.

$\div 2$

$\times \frac{1}{2}$

find  $a_1$   
find  $r$   
answer the question

$$= (\text{first}) (r^{n-1})$$

$$a_n = 96 \left(\frac{1}{2}\right)^{n-1}$$

$$a_{10} = 96 \left(\frac{1}{2}\right)^9 = 0.1875$$

$$a_7 = 96 \left(\frac{1}{2}\right)^6$$

28. What is the 15th term of the geometric sequence  $-9, 27, -81, \dots$ ?

find  $a_1$

find  $r$

write an equation

answer the question

$$r = -3$$

$$a_n = (-9)(-3)^{n-1}$$

$$\begin{aligned} a_{15} &= -9(-3)^{14} \\ &= -43046721 \end{aligned}$$

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$( \quad )( \quad )^{1 \text{ less}}$

WB 1-14