

Algebra 1

6.2

Solve systems of equations using substitution method

Solve problems using substitution of equations

solve

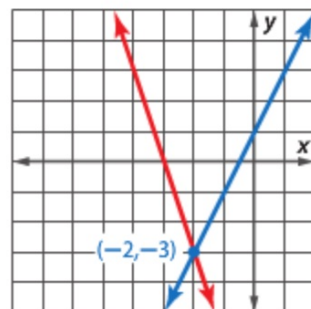
solve by graphing

substitution

substitution method

activity: cut & paste  
whiteboards

$(x, y)$



### Example 1 Solve a System by Substitution

Use substitution to solve the system of equations.

$$y = 2x + 1$$

$$3x + y = -9$$

Step 1 The first equation is already solved for  $y$ .

$(-2, -3)$

You are the coach...  
Who is on the sub  
list?

$$y = 2x + 1$$

$$y = 2 \cdot -2 + 1$$

$$y = -4 + 1$$

$$3x + (2x + 1) = -9 \quad y = -3$$

$$5x + 1 = -9$$

$$\frac{5x}{5} = \frac{-10}{5} \quad x = -2$$

$$3x + y = -9$$

$$3 \cdot -2 + y = -9$$

$$-6 + y = -9$$

$$+6 \quad +6$$

$$y = -3$$

### KeyConcept Solving by Substitution

- Step 1** When necessary, solve at least one equation for one variable.  $x =$   $y =$
- Step 2** Substitute the resulting expression from Step 1 into the other equation to replace the variable. Then solve the equation.
- Step 3** Substitute the value from Step 2 into either equation, and solve for the other variable. Write the solution as an ordered pair.

### Guided Practice

1A  $y = 4x - 6$   
 $5x + 3y = -1$

$$y = 4 \cdot 1 + -6$$
$$y = 4 + -6$$

$$(1, -2)$$

$$5x + 3(4x - 6) = -1$$

$$5x + 12x - 18 = -1$$

$$17x = \begin{array}{r} +18 \\ +18 \end{array}$$
$$\frac{17x}{17} = \frac{17}{17} \quad x = 1$$

**1B.**  $2x + 5y = -1$   
 $y = 3x + 10$

$(-3, 1)$

How is this problem different?

### Example 2 Solve and then Substitute

Use substitution to solve the system of equations.

$$\begin{array}{l} x + 2y = 6 \\ 3x - 4y = 28 \end{array}$$

↑

$$\begin{array}{r} x + 2y = 6 \\ -2y \quad -2y \\ \hline x = -2y + 6 \end{array}$$

$$\begin{aligned} 3(-2y + 6) - 4y &= 28 \\ -6y + 18 - 4y &= 28 \\ -10y + 18 &= 28 \\ -10y &= 10 \\ \frac{-10y}{-10} &= \frac{10}{-10} \\ y &= -1 \end{aligned}$$

$$(4, -1)$$

$$\begin{aligned} x &= -2 \cdot -1 + 6 \\ &= 2 + 6 \end{aligned}$$

**Guided**Practice

**2A.**  $4x + 5y = 11$

$$y - 3x = -13$$

$$+3x \quad +3x$$

$$y = 3x - 13$$

$$(4, -1)$$

2B.  $x - 3y = -9$

$5x - 2y = 7$

$$\begin{array}{r} x - 3y = -9 \\ + 3y \quad + 3y \\ \hline x = 3y - 9 \end{array}$$

$$5(3y - 9) - 2y = 7$$



$$\frac{2x}{2} = \frac{6y}{2} - \frac{14}{2} \quad x = 3y - 7$$
$$3y - x = 7$$

$$3y - 1(3y - 7) = 7$$

$$(3y - 3y) + 7 = 7$$

all numbers

$$7 = 7$$