

Algebra 1 6.4 ^{adv.} ↙
Solve systems by elimination
Solve problems using elimination

solve
elimination
zero pairs
multiplication property of equality
whiteboards

$$(-2, 5)$$

$$\begin{array}{rcl} x + 2y = 8 & & x + 2y = 8 \\ x + y = 3 & \xrightarrow{\quad} & -x - y = -3 \\ \hline & & y = 5 \end{array}$$

$$\begin{array}{rcl} x + 2 \cdot 5 = 8 & & \\ x + 10 = 8 & \text{Elimination (so far)} & \\ \hline -10 & -10 & \end{array}$$

$$x = -2$$

What is the goal?

What if they don't "match up?"

$$\begin{array}{rcl} 6 + y = 7 & & \\ -6 & & \\ \hline y = 1 & & \end{array}$$

$$x + y = 7$$

$$x - y = 5$$

$$2x = 12$$

$$\frac{2x}{2} = \frac{12}{2}$$

$$x = 6$$

$$(6, 1)$$

If I multiply all terms by the same amount, is it still equal?

$$3 = 3$$

$$4 \cdot 2x = 8 \cdot 4$$

$$8x = 32$$

Goal: make zero pairs...

Example 1 Multiply One Equation to Eliminate a Variable

Use elimination to solve the system of equations.

$$5x + 6y = -8$$

$$2x + 3y = -5$$

\Rightarrow

$$5x + 6y = -8$$

$$-4x + -6y = 10$$

$$\begin{array}{l} 5 \cdot 2 + 6 \cdot y = -8 \\ 10 + 6y = -8 \\ (2, -3) \end{array}$$

$$\begin{array}{r} 6y = -18 \\ \underline{6} \quad \underline{6} \\ y = \end{array}$$

$$x = 2$$

$$\begin{array}{l} 2 \cdot 2 + 3 \cdot -3 = -5 \\ 4 + -9 = -5 \quad \checkmark \end{array}$$

KeyConcept Solving by Elimination

- Step 1** Multiply at least one equation by a constant to get two equations that contain opposite terms.
- Step 2** Add the equations, eliminating one variable. Then solve the equation.
- Step 3** Substitute the value from Step 2 into one of the equations and solve for the other variable.
Write the solution as an ordered pair.

Goal: make zero pairs

Example 2 Multiply Both Equations to Eliminate a Variable

Use elimination to solve the system of equations.

$$\begin{array}{rcl} 4x + 2y = 8 & \xrightarrow{\cdot 3} & 12x + 6y = 24 \\ 3x + 3y = 9 & \xrightarrow{\cdot 2} & -6x - 6y = -18 \end{array}$$

$$\begin{array}{rcl} 4x + 2y = 8 & \xrightarrow{\cdot 6} & 24x + 12y = 48 \\ 3x + 3y = 9 & \xrightarrow{\cdot 4} & -12x - 12y = -36 \end{array}$$

$$\begin{array}{r} 24x + 12y = 48 \\ -12x - 12y = -36 \\ \hline 12x = 12 \\ \frac{12}{12} \quad \frac{12}{12} \quad x = 1 \end{array}$$

$$x = 1 \quad (1, 2)$$

$$\begin{array}{rcl} 4 \cdot 1 + 2y & = & 8 \\ 4 + 2y & = & 8 \\ -4 & & -4 \\ \hline 2y & = & 4 \\ \frac{2y}{2} & = & \frac{4}{2} \end{array}$$

Guided Practice

$$\begin{array}{l} 1A. \quad 6x - 2y = 10 \xrightarrow{\times 2} 6x - 2y = 10 \\ \quad \quad 3x - 7y = -19 \xrightarrow{\times -2} -6x + 14y = 38 \end{array}$$

$$(3, 4)$$

$$6x - 2 \cdot 4 = 10$$

$$\begin{array}{r} 6x - 8 = 10 \\ + 8 \quad + 8 \end{array}$$

$$\hline 6x = 18$$

$$\frac{6}{6} \quad \frac{18}{6} \quad x = 3$$

$$\begin{array}{r} 12y = 48 \\ \hline 12 \quad 12 \end{array}$$

(q, r)

1B. $9r + q = 13$
 $3r + 2q = -4$

GuidedPractice

2A. $5x - 3y = 6$
 $2x + 5y = -10$

2B. $6a + 2b = 2$
 $4a + 3b = 8$

1. $2x - y = 4$
 $7x + 3y = 27$

2. $2x + 7y = 1$
 $x + 5y = 2$