

$$|-5| = 5$$

Algebra 1

2.5

$$|(3 + -4)|$$

$$|-1| = 1$$

$$|-13| = 13$$

Evaluate absolute value expressions

Solve absolute value equations

distance *from zero*
absolute value

$$|5| = 5$$

activ: floor graphs

$$|-3| = 3$$



1 Absolute Value Expressions Expressions with absolute values define an upper and lower range in which a value must lie. Expressions involving absolute value can be evaluated using the given value for the variable.



Example 1 Expressions with Absolute Value

Evaluate $|m + 6| - 14$ if $m = 4$.

$$\begin{array}{l} |10| - 14 \\ \downarrow \\ 10 + (-14) = -4 \end{array}$$

► **Guided Practice**

1. Evaluate $23 - |3 - 4x|$ if $x = 2$.

$$\begin{array}{ll} 23 - |3 - 8| & \cancel{23 - 3 + 8} \\ 23 - |-5| & \cancel{23 + 5} \\ \downarrow & \\ 23 - 5 = 18 & \cancel{23 + 5} \end{array}$$

KeyConcept Absolute Value Equations

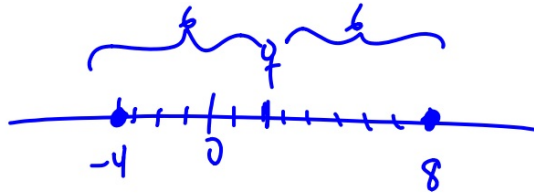
Words When solving equations that involve absolute values, there are two cases to consider.

Case 1 The expression inside the absolute value symbol is positive or zero.

Case 2 The expression inside the absolute value symbol is negative.

Symbols For any real numbers a and b , if $|a| = b$ and $b \geq 0$, then $a = b$ or $a = -b$.

Example $|d| = 10$, so $d = 10$ or $d = -10$.



Whiteboards:
practice

$$|x - 2| = 6$$

$$\frac{-4 + 8}{2} = \frac{4}{2} = 2$$

$$\begin{array}{rcl} x - 2 & = & -6 \\ + 2 & & + 2 \\ \hline x & = & -4 \end{array}$$

$$\begin{array}{rcl} x - 2 & = & 6 \\ + 2 & & + 2 \\ \hline x & = & 8 \end{array}$$

$$|x+3| = 5$$

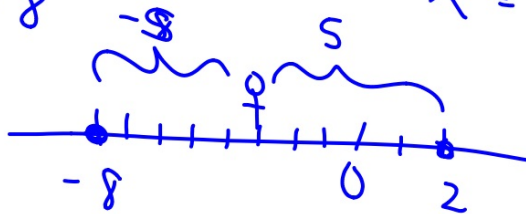
$$\begin{array}{rcl} x+3 & = & -5 \\ -3 & & -3 \end{array}$$

$$x = -8$$

$$\begin{array}{rcl} x+3 & = & 5 \\ -3 & & -3 \end{array}$$

$$x = 2$$

$$\frac{-8+2}{2} = \frac{-6}{2} = -3$$



Absolute value equations occur in real-world situations that describe a range within which a value must lie.



Real-World Example 3 Solve an Absolute Value Equation

SNAKES The temperature of an enclosure for a pet snake should be about 80°F , give or take 5° . Find the maximum and minimum temperatures.

$$\pm 5$$

$$80 \pm 5$$

$$75 - 85$$

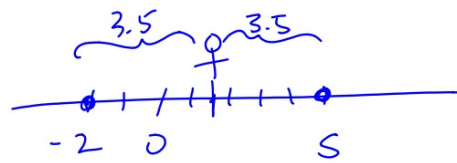


Real-WorldLink

In 2001, the number of households in the U.S. that had either a turtle, snake, lizard, or other reptile as a pet was 1,678,000.

Solve

$$|2x - 3| = 7$$



$$\begin{array}{r} 2x - 3 = -7 \\ +3 \quad +3 \\ \hline 2x = -4 \\ \frac{2x}{2} = \frac{-4}{2} \\ x = -2 \end{array}$$

$$\begin{array}{r} 2x - 3 = 7 \\ +3 \quad +3 \\ \hline 2x = 10 \\ \frac{2x}{2} = \frac{10}{2} \\ x = 5 \end{array}$$

$$\frac{-2 + 5}{2} = \frac{3}{2} = 1.5$$