

$$|-5| = 5$$

Algebra 1

2.5

$$\left| (3 + -4) \right|$$
$$|-1| = 1$$

$|-13| = 13$  Evaluate absolute value expressions  
Solve absolute value equations

distance from zero

absolute value

$$|5| = 5$$

activ: floor graphs

$$|-3| = 3$$



**1 Absolute Value Expressions** Expressions with absolute values define an upper and lower range in which a value must lie. Expressions involving absolute value can be evaluated using the given value for the variable.



### Example 1 Expressions with Absolute Value

Evaluate  $|m + 6| - 14$  if  $m = 4$ .

$$|10| - 14$$

A yellow arrow points from the value 10 to the first absolute value symbol. Another yellow arrow points from the value -14 to the second absolute value symbol.

$$10 + -14 = -4$$

› **Guided Practice**

1. Evaluate  $23 - |(3 - 4)|$  if  $x = 2$ .

$$\begin{aligned}23 - |(3 - 8)| &\quad \cancel{23 - 3 + 8} \\23 - |-5| &\quad \cancel{23 + 5} \\23 - 5 &= 18 \quad \cancel{23 + 5}\end{aligned}$$

 **KeyConcept** Absolute Value Equations

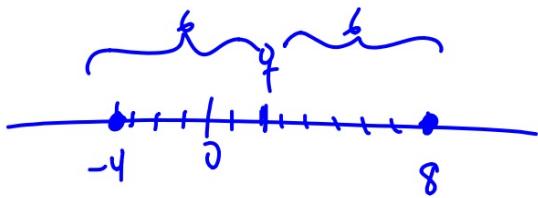
**Words** When solving equations that involve absolute values, there are two cases to consider.

**Case 1** The expression inside the absolute value symbol is positive or zero.

**Case 2** The expression inside the absolute value symbol is negative.

**Symbols** For any real numbers  $a$  and  $b$ , if  $|a| = b$  and  $b \geq 0$ , then  $a = b$  or  $a = -b$ .

**Example**  $|d| = 10$ , so  $d = 10$  or  $d = -10$ .



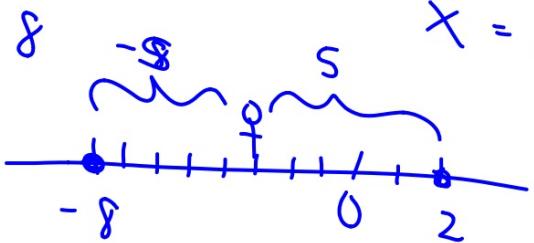
Whiteboards:  
practice

$$\begin{array}{r}
 |x-2| = 6 \\
 x-2 = -6 \\
 \hline
 x = -4
 \end{array}
 \qquad
 \begin{array}{r}
 -4+8 = 4 \\
 \hline
 2 = 2
 \end{array}
 \qquad
 \begin{array}{r}
 x-2 = 6 \\
 +2 +2 \\
 \hline
 x = 8
 \end{array}$$

$$|x+3| = 5$$

$$\begin{array}{rcl} x+3 & = & -5 \\ -3 & & -3 \\ \hline x & = & -8 \end{array}$$

$$\begin{array}{rcl} x+3 & = & 5 \\ -3 & & -3 \\ \hline x & = & 2 \end{array}$$

$$\begin{array}{l} -\frac{8+2}{2} = -\frac{6}{2} = -3 \\ \hline x = -8 \qquad \qquad \qquad x = 2 \end{array}$$


Absolute value equations occur in real-world situations that describe a range within which a value must lie.



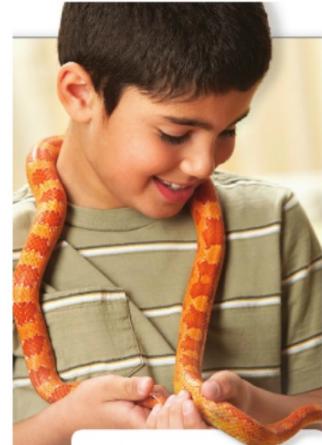
### Real-World Example 3 Solve an Absolute Value Equation

**SNAKES** The temperature of an enclosure for a pet snake should be about  $80^{\circ}\text{F}$ , give or take  $5^{\circ}$ . Find the maximum and minimum temperatures.

$\pm 5$

$$80 \pm 5$$

$$75 - 85$$

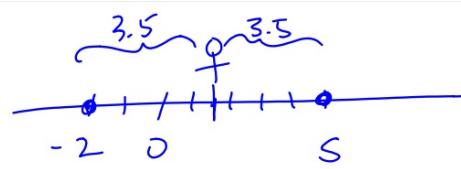


#### Real-World Link

In 2001, the number of households in the U.S. that had either a turtle, snake, lizard, or other reptile as a pet was 1,678,000.

Solve

$$\underline{2x - 3} = 7$$



$$\begin{array}{rcl} 2x - 3 & = & -7 \\ +3 & & +3 \\ \hline 2x & = & -\frac{7}{2} \\ \frac{2x}{2} & & \\ x & = & -2 \end{array}$$

$$\begin{array}{rcl} 2x - 3 & = & 7 \\ +3 & & +3 \\ \hline 2x & = & 10 \\ \frac{2x}{2} & & \\ x & = & 5 \end{array}$$

$$-\frac{2+5}{2} = \frac{3}{2} = 1.5$$