

Algebra 1 5.2

*6th grade standard

Solve linear inequalities by using multiplication*

Solve linear inequalities by using division*

multiplication property of (in)equality

$<$ \leq

division property of (in)equality

$>$ \geq

triangle puzzles (if time)

$$\begin{array}{l} 2 \cdot 5 > 3 \cdot 2 \\ 10 > 6 \end{array}$$

Mult by positive #

$$5 > 3$$

$$-2 < 0$$

Is it still true?

$$3 \cdot 10 > 7 \cdot 3$$

$$30 > 21$$

$$-2 \cdot 10 > 3 \cdot -2$$

$$-20 < -6$$

$$-5 \cdot 12 > -3 \cdot -5$$

$$-60 < 15$$

But....Mult by negative #

$$5 > 3$$

$$-2 < 0$$

Is it still true?

What must happen to make it work?

p292

These examples demonstrate the **Multiplication Property of Inequalities**.

KeyConcept Multiplication Property of Inequalities		
Words	Symbols	Examples
If both sides of an inequality that is true are multiplied by a positive number, the resulting inequality is also true.	For any real numbers a and b and any positive real number c , if $a > b$, then $ac > bc$. And, if $a < b$, then $ac < bc$.	$6 > 3.5$ $6(2) > 3.5(2)$ $12 > 7$ and $2.1 < 5$ $2.1(0.5) < 5(0.5)$ $1.05 < 2.5$
If both sides of an inequality that is true are multiplied by a negative number, the direction of the inequality sign is reversed to make the resulting inequality also true.	For any real numbers a and b and any negative real number c , if $a > b$, then $ac < bc$. And, if $a < b$, then $ac > bc$.	$7 > 4.5$ $7(-3) < 4.5(-3)$ $-21 < -13.5$ and $3.1 < 5.2$ $3.1(-4) > 5.2(-4)$ $-12.4 > -20.8$

The DIGITS get bigger as you move away from zero in either direction.

BUT:

Move to the right, the values *increase*.

Move to the left, the values *decrease*.

$$20 \cdot \frac{1}{5} m \geq -3$$

$$\frac{1}{5} \quad \frac{1}{5}$$

$$m \geq -15$$

$$20 \cdot \frac{3}{8} t < 5 \cdot \frac{8}{3}$$

$$\frac{3}{8} \quad \frac{3}{8}$$

$$t < \frac{40}{3}$$

Example 2 Solve by Multiplying

Solve $-\frac{3}{7}r < 21$. Graph the solution on a number line.

$$-\frac{7}{3} \cdot \frac{-3}{7}r < \frac{21}{7} \cdot -\frac{7}{3}$$

$$r > -49$$

whiteboards

$$2A. -\frac{n}{6} \leq 8$$

$$\begin{aligned} &-\frac{n}{6} \leq 8 \\ &\xrightarrow{-\frac{6}{1}} -\frac{1}{6}n \leq 8 \cdot \frac{-6}{1} \\ &n \geq -48 \end{aligned}$$

$$2B. \frac{-3}{4} \cdot \frac{-4}{3}p > -10 \cdot \frac{-3}{4}$$

$$p < \frac{30}{4}$$

$$p < \frac{15}{2}$$

Divide by positive

$$6 > 2$$

$$-40 < 10$$

Is it still true?

$$\frac{12}{2} > \frac{8}{2}$$

$$6 > 4$$

$$\frac{10}{-2} > \frac{6}{-2}$$

$$-5 < -3$$

Divide by negative

$$12 > 6$$

$$-4 < 20$$

Is it still true?

What do we need to do for it to work?

These examples demonstrate the **Division Property of Inequalities**.

KeyConcept Division Property of Inequalities		
Words	Symbols	Examples
If both sides of a true inequality are divided by a positive number, the resulting inequality is also true.	For any real numbers a and b and any positive real number c , if $a > b$, then $\frac{a}{c} > \frac{b}{c}$. And, if $a < b$, then $\frac{a}{c} < \frac{b}{c}$.	$4.5 > 2.1$ $1.5 < 5$ $\frac{4.5}{3} > \frac{2.1}{3}$ and $\frac{1.5}{0.5} < \frac{5}{0.5}$ $1.5 > 0.7$ $3 < 10$
If both sides of a true inequality are divided by a negative number, the direction of the inequality sign is reversed to make the resulting inequality also true.	For any real numbers a and b , and any negative real number c , if $a > b$, then $\frac{a}{c} < \frac{b}{c}$. And, if $a < b$, then $\frac{a}{c} > \frac{b}{c}$.	$6 > 2.4$ $-1.8 < 3.6$ $\frac{6}{-6} < \frac{2.4}{-6}$ and $\frac{-1.8}{-9} < \frac{3.6}{-9}$ $-1 < -0.4$ $0.2 > -0.4$

Same same...

Example 3 Divide to Solve an Inequality

Solve each inequality. Graph the solution on a number line.

a. $\frac{60t}{60} > \frac{8}{60}$ $\frac{4}{30} \geq \frac{2}{15}$

$$t > \frac{2}{15}$$

b. $\frac{-7d}{-7} \leq \frac{147}{-7}$

$$d \geq -21$$

$$\{ d \mid d \geq -21 \}$$

► **Guided**Practice

$$3A. \frac{8p}{8} \leq \frac{58}{8}$$

$$p \leq 7\frac{1}{4}$$

$$p \leq \frac{29}{4}$$

$$3B. \frac{-42}{6} \geq \frac{6r}{6}$$

$$-7 \geq r$$

3C. $-12h > 15$

3D. $-\frac{1}{2}n \leq 6$

Triangle puzzle



Real-World Example 1 Write and Solve an Inequality

SURVEYS Of the students surveyed at Madison High School, fewer than eighty-four said they have never purchased an item online. This is about one eighth of those surveyed. How many students were surveyed?

