

Algebra 1 8.5

Use the distributive property to factor polynomials

Solve quadratic equations by factoring

quadratic

factor

$$(\quad) \cdot (\quad) \quad (\quad)(\quad)$$

distributive property

greatest common factor (GCF)

* zero product property

$$\sim (\quad)(\quad)$$

whiteboards

$$(\quad) \cdot (\quad) = 0$$

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Factor each polynomial.

3A. $\left(\frac{c}{2} - \frac{2cd}{2} + \frac{8d}{-4} - \frac{4}{-4} \right)$

$$c(1-2d) + -4(-2d+1)$$

$$(1-2d)(c-4)$$

\checkmark \checkmark \checkmark
 $2x^3 + 8x^2 + 12x$
 $1 \begin{pmatrix} 2 \\ \times \times \end{pmatrix}$ $1 \begin{pmatrix} 8 \\ 2 \times \end{pmatrix}$ $1 \begin{pmatrix} 12 \\ 3 \times \end{pmatrix}$
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$$2x(x^2 + 4x + 6)$$

$2x \cdot x^2$	$2x \cdot 4x$	$2x \cdot 6$
$2x^3$	$8x^2$	$12x$

$$3B. \left(\frac{3p}{p} - \frac{2p^2}{p} \right) - \left(\frac{18p}{9} + \frac{27}{9} \right)$$

$$p(3-2p) + 9(-2p+3)$$

$$(3-2p)(p+9)$$

$$(\quad) \cdot (\quad) = 0$$

 **KeyConcept** Zero Product Property

Words If the product of two factors is 0, then at least one of the factors must be 0.

Symbols For any real numbers a and b , if $ab = 0$, then $a = 0$, $b = 0$, or both a and b equal zero.

Example 4 Solve Equations

Solve each equation. Check your solutions.

a. $(2d + 6)(3d - 15) = 0$

$$\begin{array}{r} 2d + 6 = 0 \\ -6 \quad -6 \\ \hline 2d = -6 \\ \frac{2d}{2} = \frac{-6}{2} \\ d = -3 \end{array}$$

$$\begin{array}{r} 3d - 15 = 0 \\ +15 \quad +15 \\ \hline 3d = 15 \\ \frac{3d}{3} = \frac{15}{3} \\ d = 5 \end{array}$$

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$$(10 + 6)(15 - 15) = 0$$
$$16 \cdot 0 = 0$$

$$(-6 + 6)(-18 - 15) = 0$$
$$0 \cdot 33 = 0$$

Guided Practice

4A. $(3n)(n + 2) = 0$

$$\begin{array}{l} \downarrow \qquad \qquad \downarrow \\ 3n = 0 \qquad n + 2 = 0 \\ \hline 3 \quad 3 \qquad -2 \quad -2 \\ \hline n = 0 \qquad n = -2 \end{array}$$

$$\begin{array}{l} x^2 + 3x = 0 \\ \frac{x^2}{x} + \frac{3x}{x} = 0 \\ x(x + 3) = 0 \\ \downarrow \qquad \qquad \downarrow \\ x = 0 \qquad x + 3 = 0 \\ \qquad \qquad \qquad x = -3 \end{array}$$

must=0 to factor

$$4B. \frac{8b^2}{8b} - \frac{40b}{8b} = 0$$

$$8b(b - 5) = 0$$

$$\begin{array}{l} \downarrow \qquad \qquad \downarrow \\ \frac{8b}{8} = \frac{0}{8} \qquad b - 5 = 0 \\ \qquad \qquad \qquad +5 \quad +5 \\ \qquad \qquad \qquad b = 5 \\ b = 0 \end{array}$$

Solve

$$c^2 = 3c$$

$-3c \quad -3c$

Must =0 to factor

$$c^2 - 3c = 0$$

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$$c(c-3) = 0$$

$$\begin{array}{l} \downarrow \qquad \downarrow \\ c=0 \qquad c-3=0 \\ \underline{\quad} \qquad \underline{\quad} \\ \qquad \qquad c=3 \\ \qquad \qquad \underline{\quad} \end{array}$$

4C. $x^2 = -10x$

WB skills
8.5 odds

