

Algebra 1 3.1

Identify linear equations, intercepts, and zeros

Graph linear equations

integer - whole numbers + opposites

linear equation graph is a line

standard form $Ax + By = C$

constant numbers

variable change x, y

x-intercept cross x-axis

y-intercept cross y-axis

whiteboards

23.

* 12 ml. 5% 0.05

* ?x 30% 0.3

* 12 + ?x 20% 0.2

$$\begin{aligned} & (\text{Conc} \times \text{amt}) + (\text{Conc} \times \text{amt}) = (\text{Conc} \times \text{amt}) \\ & (0.05)(12) + 0.3x = 0.2(12+x) \end{aligned}$$

$$\begin{array}{rclcl} 0.6 + 0.3x & = & 2.4 + 0.2x \\ -0.6 & -0.2x & -0.6 & -0.2x & \\ \hline \end{array}$$

$$\begin{array}{rcl} 0.1x & = & 1.8 \\ \hline x & = & 18 \end{array}$$

 **KeyConcept** Standard Form of a Linear Equation

Words The standard form of a linear equation is $Ax + By = C$, where $A \geq 0$, A and B are not both zero, and A , B , and C are integers with a greatest common factor of 1.

Examples In $3x + 2y = 5$, $A = 3$, $B = 2$, and $C = 5$.
In $x = -7$, $A = 1$, $B = 0$, and $C = -7$.

tomorrow

Format
GCF
Pos x

Linear equations

$$4x - 5y = 16$$

$$x = 10$$

$$y = -\frac{2}{3}x - 1$$

$$y = \frac{1}{2}x$$

Nonlinear equations

$$2x + 6y^2 = -25$$

$$y = \sqrt{x} + 2$$

$$x + xy = -\frac{5}{8}$$

$$y = \frac{1}{x}$$

How can we tell by inspection?

linear no exponents
product $x \cdot y$
var. in denom
✓

Example 1 Identify Linear Equations



Determine whether each equation is a linear equation. Write the equation in ~~standard~~ form.

a. $y = 4 - 3x$

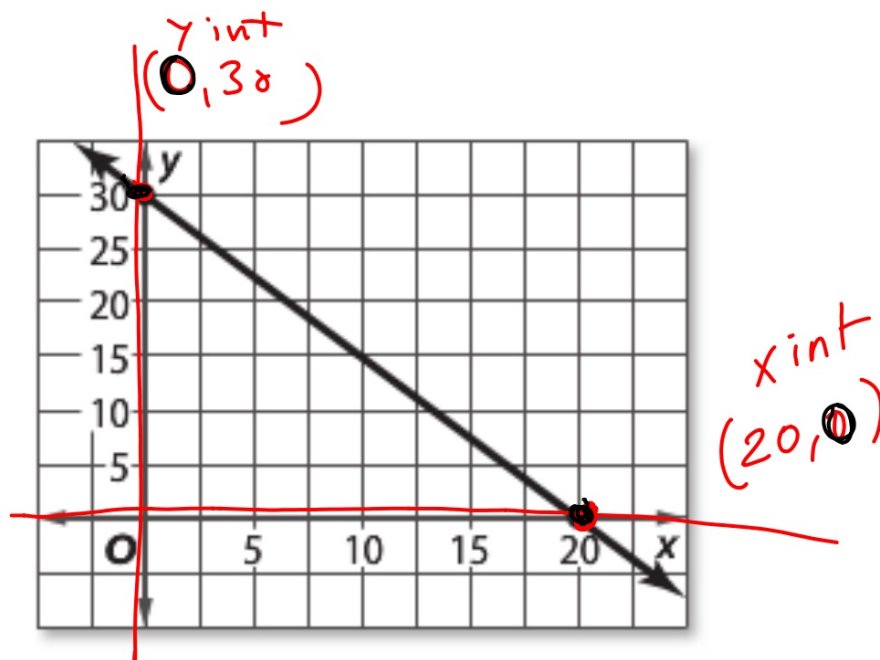
yes

b. $6x - xy = 4$

no

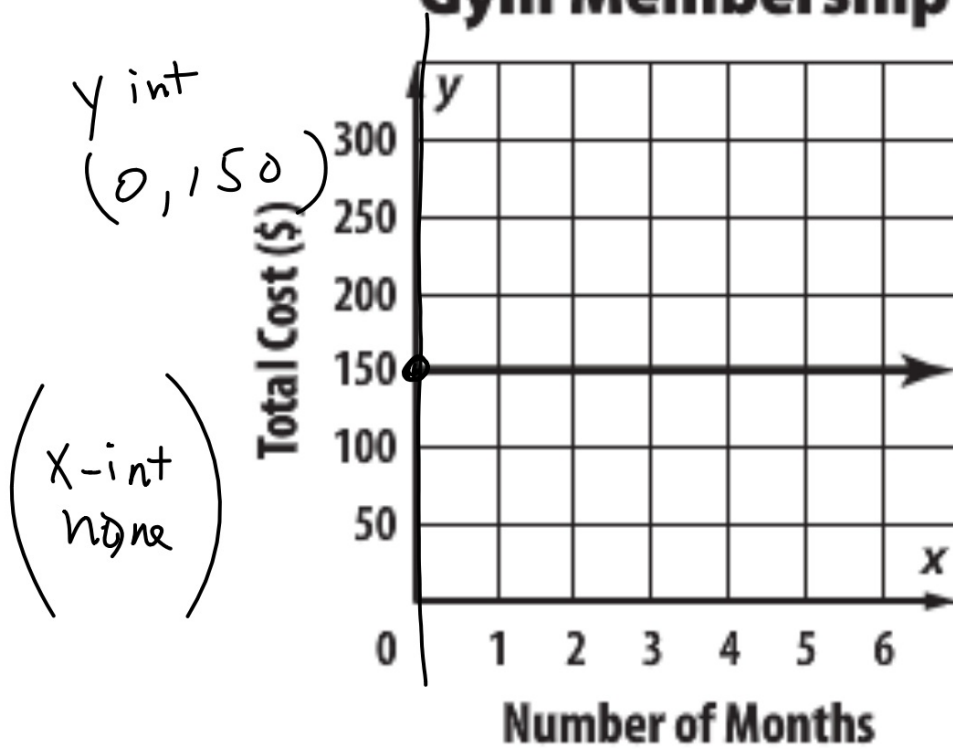
Standardized Test Example 2 Find Intercepts

Find the x - and y -intercepts of the line graphed at the right.



2. **HEALTH** Find the x - and y -intercepts of the graph.

Gym Membership



Real-World Example 3 Find Intercepts from a Table

SWIMMING POOL A swimming pool is being drained at a rate of 720 gallons per hour. The table shows the function relating the volume of water in a pool and the time in hours that the pool has been draining.

- a. Find the x - and y -intercepts of the graph of the function.

x -int $(14, 0)$

y -int $(0, 10,080)$

- b. Describe what the intercepts mean in this situation.

Draining a Pool	
Time (h)	Volume (gal)
x	y
0	10,080
2	8640
6	5760
10	2880
12	1440
14	0

Draining a Pool



Guided Practice

3. **DRIVING** The table shows the function relating the distance to an amusement park in miles and the time in hours the Torres family has driven. Find the x - and y -intercepts. Describe what the intercepts mean in this situation.

x -int $(4, 0)$
 y -int $(0, 248)$

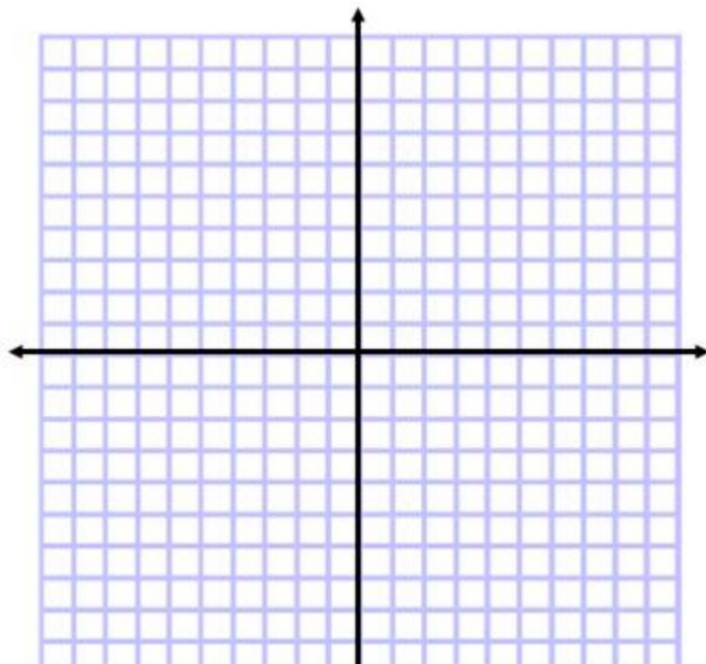
Time (h)	Distance (mi)
0	248
1	186
2	124
3	62
4	0

$$(\text{?}, 0) \rightarrow (x, 0)$$

When @ x-intercept, what is the y-coordinate?

When @ y-intercept, what is the x-coordinate?

$$(0, \text{?}) \rightarrow (0, y)$$



How can I use what I know about intercepts?

Example 4 Graph by Using Intercepts

Graph $2x + 4y = 16$ by using the x - and y -intercepts.

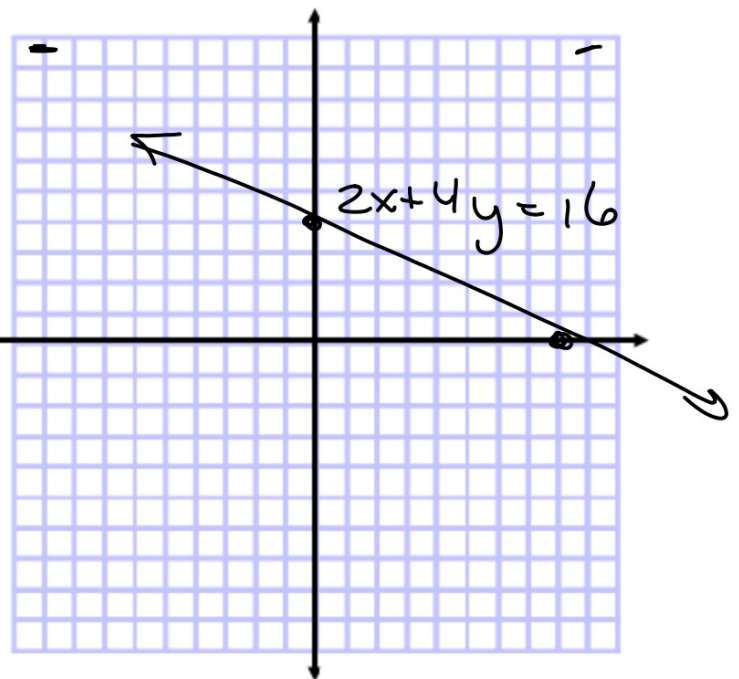


$$y = mx + B$$

-1 .

$$\begin{aligned} x\text{-int } (8, 0) \quad & \frac{2x}{2} = \frac{16}{2} \\ & x = 8 \end{aligned}$$

$$\begin{aligned} y\text{-int } (0, 4) \quad & \frac{4y}{4} = \frac{16}{4} \\ & y = 4 \end{aligned}$$



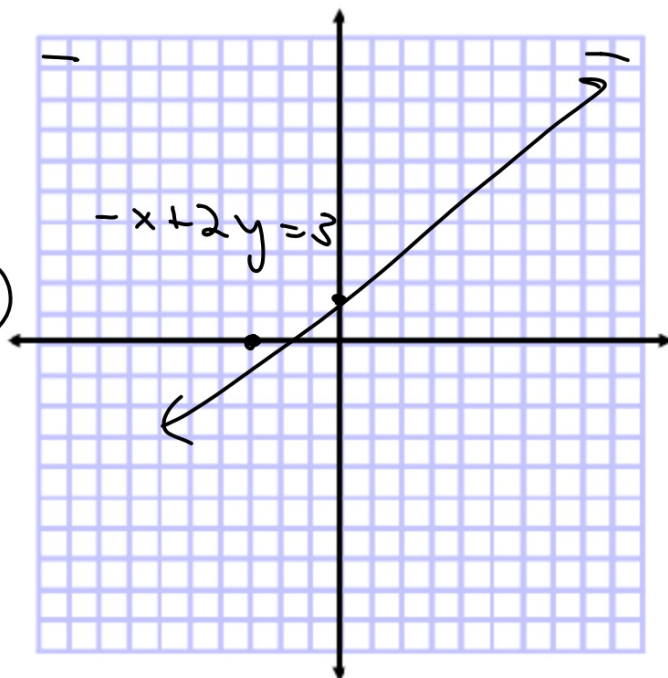
Graph each equation by using the x - and y -intercepts.

4A. $-x + 2y = 3$

4B. $y = -x - 5$

whiteboards

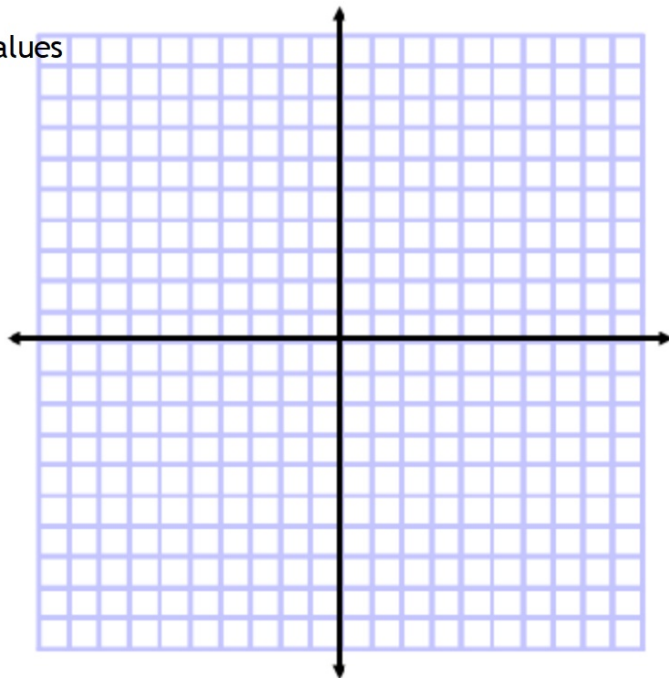
x -int $(-3, 0)$ $\frac{-x}{-1} = \frac{3}{-1}$
 y -int $(0, \frac{3}{2})$ $(0, 1.5)$
 $\frac{2y}{2} = \frac{3}{2}$



Graph by making a table of values
 $y = 2x + 1$

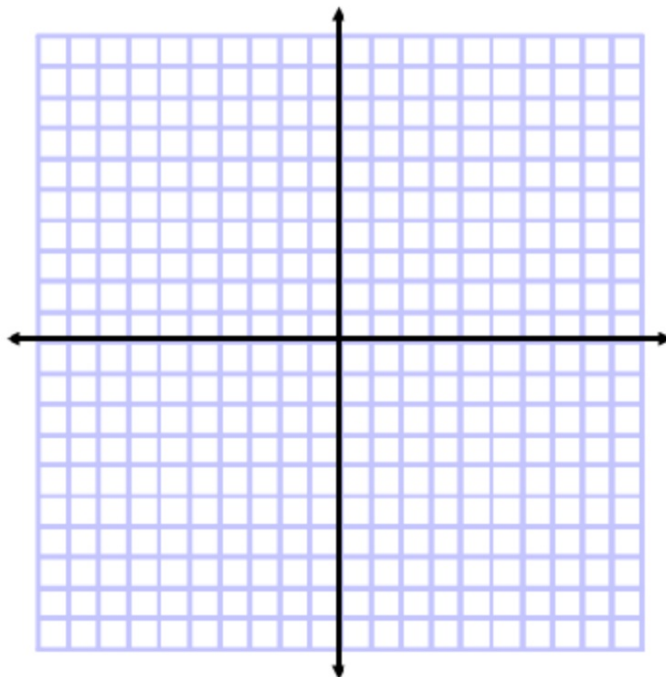
3.1 p.159

13-49 odd



Example 5 Graph by Making a Table

Graph $y = \frac{1}{3}x + 2$.

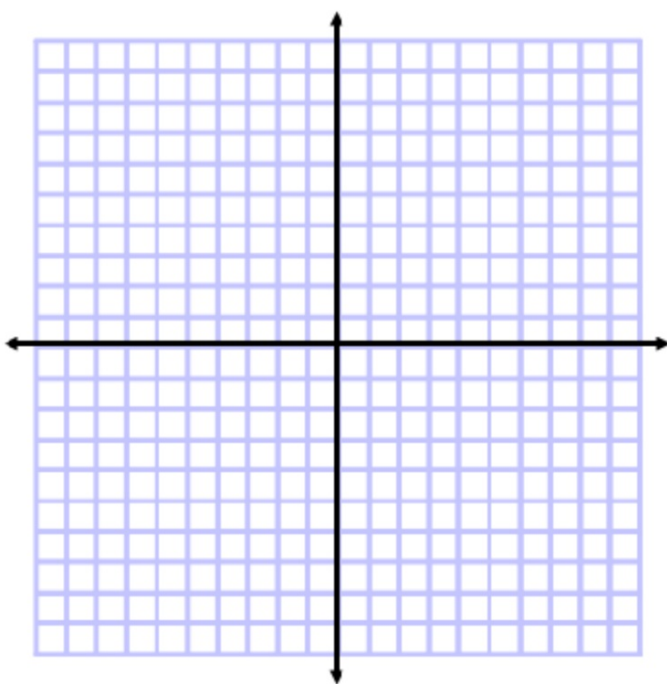


▸ **Guided**Practice

Graph each equation

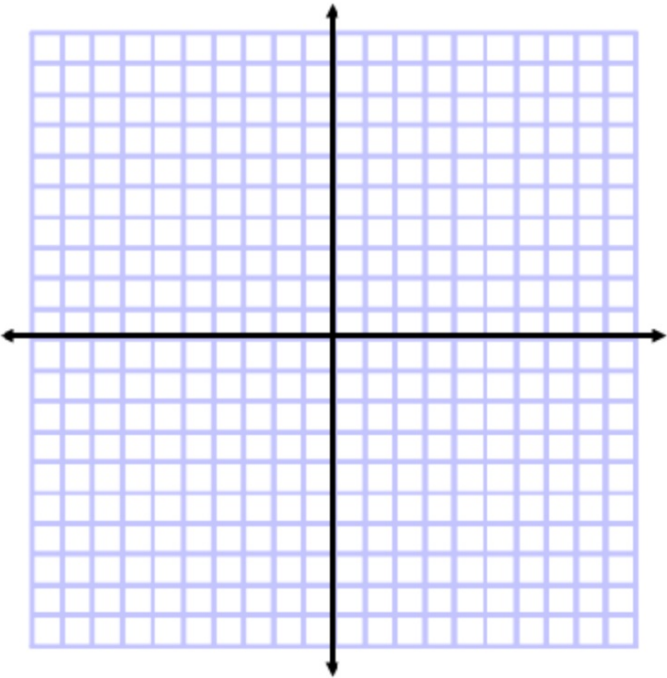
5A. $2x - y = 2$

Solve for y



You can only choose 3 for x

5B. $x = 3$



You will get -2 for y, no matter what...

5C. $y = -2$

