

Trig 6.7

$\left. \begin{array}{l} \tan \\ \cot \end{array} \right\}$

Graph secant and cosecant

Write equations of trig functions

$\cos = 0 \leftarrow$
secant undef \downarrow

$\sin = 0 \leftarrow$
cosecant undef \downarrow

reciprocal

asymptote

Just fell asleep at the beach and woke up with a hideous tan line

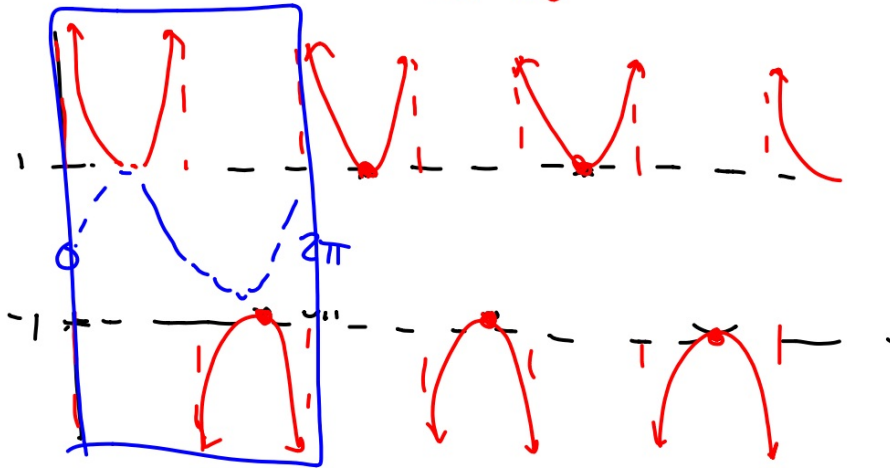


100 10

$$y = \csc x \quad -10 \quad -100$$

$\frac{1}{100} \frac{1}{10}$ Parent graph: $y = \sin x$

$$-\frac{1}{10} \quad -\frac{1}{100}$$



Where sine has a zero...
Also: what is the reciprocal of one?

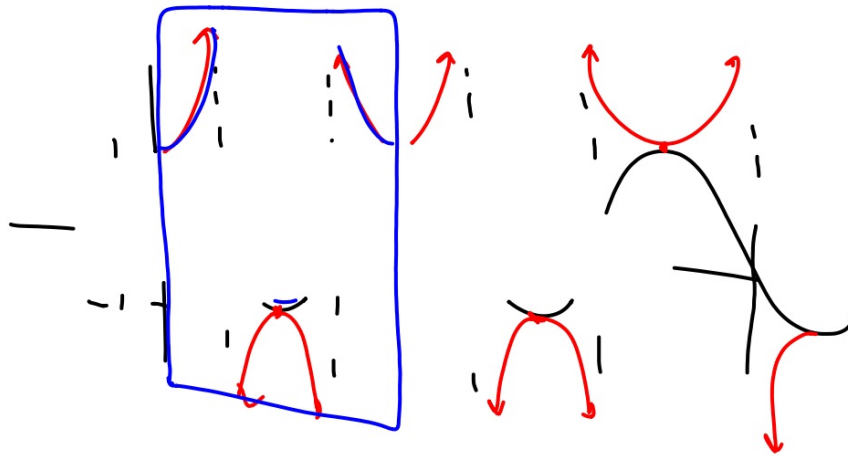


Properties of
the Graph of
 $y = \csc x$

1. The period is 2π .
2. The domain is the set of real numbers except πn , where n is an integer.
3. The range is the set of real numbers greater than or equal to 1 or less than or equal to -1 .
4. There are no x -intercepts.
5. There are no y -intercepts.
6. The asymptotes are $x = \pi n$, where n is an integer.
7. $y = 1$ when $x = \frac{\pi}{2} + 2\pi n$, where n is an integer.
8. $y = -1$ when $x = \frac{3\pi}{2} + 2\pi n$, where n is an integer.

p. 397

Where cos has a zero...
 What is the reciprocal of one?



↑ ↑↑ y ↑ ↑↑ ↑↑

p. 397

Properties of
the Graph of
 $y = \sec x$

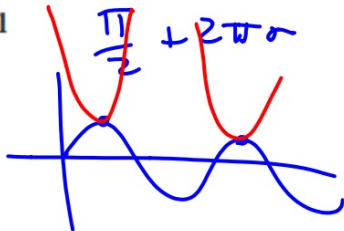
1. The period is 2π .
2. The domain is the set of real numbers except $\frac{\pi}{2}n$, where n is an odd integer.
3. The range is the set of real numbers greater than or equal to 1 or less than or equal to -1 .
4. There are no x -intercepts.
5. The y -intercept is 1.
6. The asymptotes are $x = \frac{\pi}{2}n$, where n is an odd integer.
7. $y = 1$ when $x = \pi n$, where n is an even integer.
8. $y = -1$ when $x = \pi n$, where n is an odd integer.

What is the reciprocal of 1?

2 Find the values of θ for which each equation is true.

$$\frac{1}{\sin \theta}$$

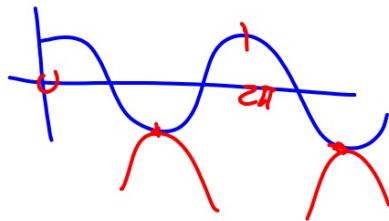
a. $\csc \theta = 1$



$$\frac{1}{\cos}$$

b. $\sec \theta = -1$

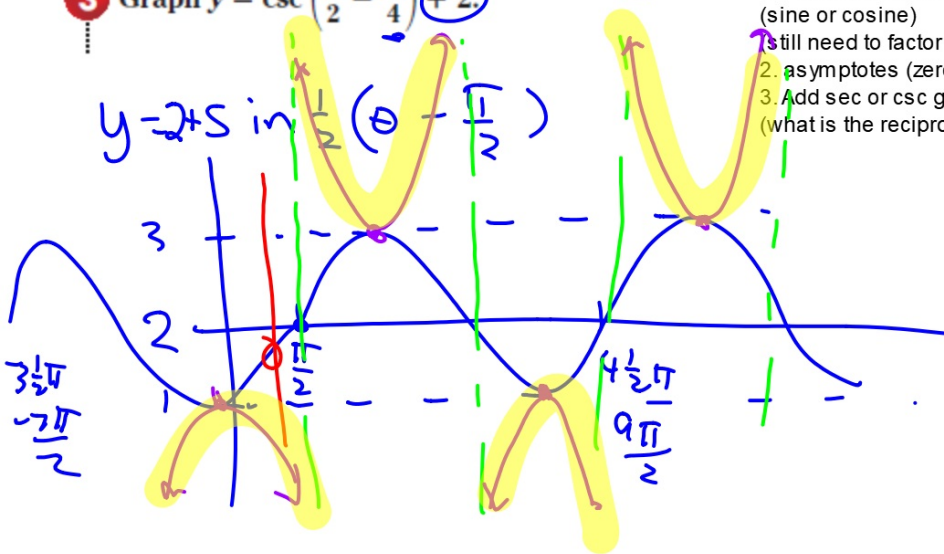
$$\pi + 2\pi n$$



$$\frac{1}{2} \left(\theta - \frac{\pi}{2} \right) \xrightarrow{\frac{2}{1} \cdot \frac{2\pi}{2}} = \text{new}$$

3 Graph $y = \csc \left(\frac{\theta}{2} - \frac{\pi}{4} + 2 \right)$

1. Graph the corresponding parent graph (sine or cosine)
2. still need to factor to see period & phase shift, etc.)
3. asymptotes (zeros)
4. Add sec or csc graphs (what is the reciprocal of 1?)



5 Write an equation for a secant function with period π , phase shift $\frac{\pi}{3}$, and vertical shift -3 .

$$y = -3 + \sec 2 \left(\theta - \frac{\pi}{3} \right)$$

$$\frac{2\pi}{n} = \pi$$

$$\frac{\pi n}{\pi} = \frac{2\pi}{\pi}$$

