

Precalc 10.5

Use and determine standard and general forms of the equation of a parabola

Graph parabolas

parent graph  $y=x^2$   $x^2=y$   $y^2=x$

- p
- focus
- directrix
- axis of symmetry
- vertex
- latus rectum

↳ right

$$x^2 = 4py$$

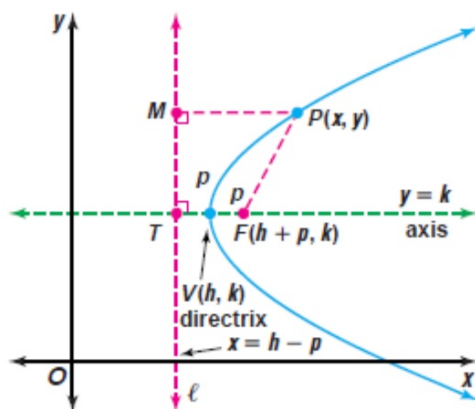
$$y^2 = 4px$$

eccentricity

light bulbs

<https://www.youtube.com/watch?v=Vq7xXUaCDI4>

p (parabola constant)



$$x^2=4py \quad \text{or} \quad y^2=4px$$

For the equation of each parabola, find the coordinates of the vertex and focus, and the equations of the directrix and axis of symmetry. Then graph the equation.

6.  $x^2 = 12(y - 1)$

7.  $y^2 - 4x + 2y + 5 = 0$

8.  $x^2 + 8x + 4y + 8 = 0$

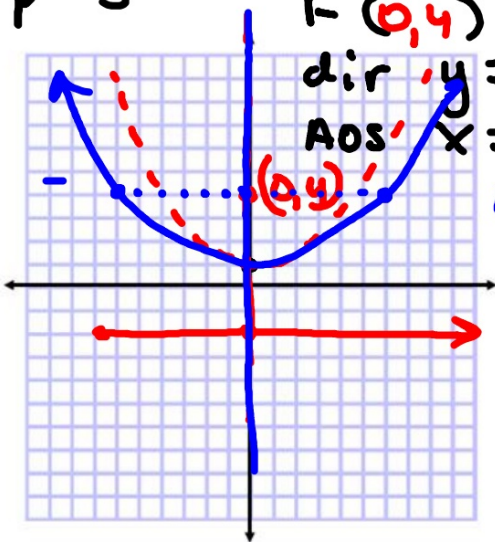
$4p = 12$   
 $p = 3$

$v(0, 1)$   
 $F(0, 4)$

dir:  $y = -2$

AoS:  $x = 0$

$LR = 4p$



Standard form or...  
Complete the square...

$x =$

$y =$

$$x^2 = 4py \quad \underline{\underline{y^2 = 4px}}$$

$$y^2 - 4x + 2y + 5 = 0$$

$$(y^2 + 2y + 1) = 4x - 5 + 1$$

$$(y+1)^2 = 4x - 4$$

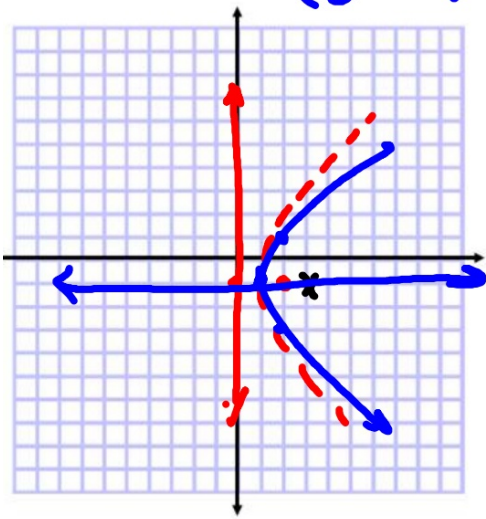
$$= \textcircled{4}(x-1) \quad \begin{matrix} 4p=4 \\ p=1 \end{matrix} \quad V(1, -1)$$

$$(y+1)^2 = 4(x-1) \quad F(2, -1)$$

$$\text{dir } x=0$$

$$\text{ADS } y=-1$$

$$LR = 4 \cdot 1 = 4$$



$$x^2 = 4py$$

$$x^2 + 8x + 4y + 8 = 0$$

$$x^2 + 8x + 16 = -4y - 8 + 16$$

$$(x+4)^2 = -4y + 8$$

$$(x+4)^2 = -4(y-2)$$

$$V(-4, 2)$$

$$F(-4, 1)$$

$$\text{dir } y = 3$$

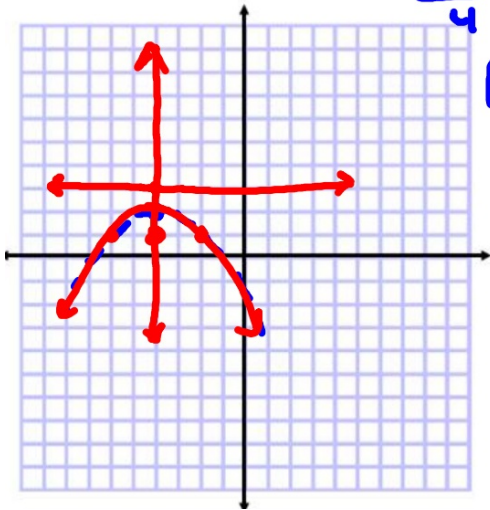
$$\text{AOS } x = -4$$

LR

$$\frac{4p}{4} = -4$$

$p = -1$

$$4(-1) = -4$$



General Form  
for the  
Equation of  
a Parabola

The general form of the equation of a parabola is  
 $y^2 + Dx + Ey + F = 0$ , when the directrix is parallel to the y-axis, or  
 $x^2 + Dx + Ey + F = 0$ , when the directrix is parallel to the x-axis.

A handwritten diagram consisting of a large left-facing curly bracket that encompasses the equations  $x^2 = 4pY$  and  $y^2 = 4pX$ . A horizontal wavy line is drawn above the top equation. Below the bottom equation, the term  $+Cx^2$  is written in red ink and is partially enclosed by the bottom curve of the bracket.

$$x^2 = 4pY$$
$$y^2 = 4pX$$
$$Ax^2 + By^2 + Cx^2 + Dx + Ey + F = 0$$

18.  $x^2 + 10x + 25 = -8y + 24$

$$x^2 = 4py$$

3 Consider the equation  $2x^2 - 8x + y + 6 = 0$ .

- Write the equation in standard form.
- Find the coordinates of the vertex and focus and the equations for the directrix and the axis of symmetry.
- Graph the equation of the parabola.

$$\frac{4p}{4} = \frac{-1}{2} \cdot \frac{1}{4}$$

$$p = -\frac{1}{8}$$

$$(x-2)^2 = -\frac{1}{2}(y-4)$$

factor  
complete the square  
solve for  $x^2 = 4py$

$$-2(x-2)^2 = y-4$$

$$y = -2(x-2)^2 + 4$$

$$V(2, 4)$$

$$F(2, 3\frac{7}{8})$$

$$\text{dir } y = 4\frac{1}{8}$$

$$\text{AOS } x = 2$$

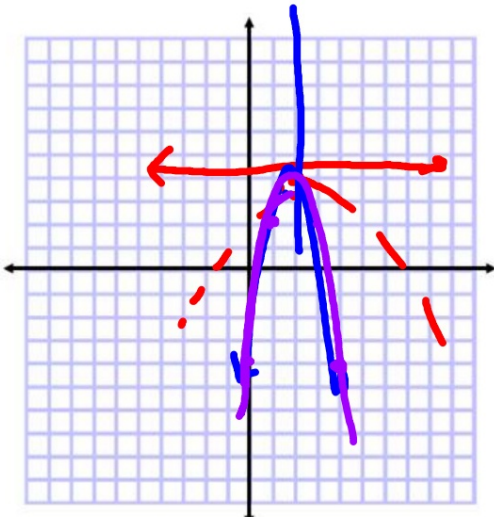
$$\text{LR } = -\frac{1}{2}$$

$$2(x^2 - 4x + 4) = -y - 6 + 8$$

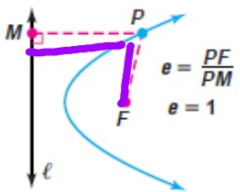
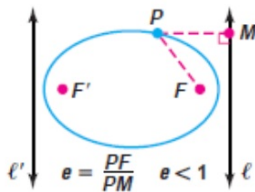
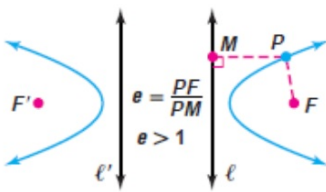
$$\frac{2(x-2)^2}{2} = \frac{-y+2}{2}$$

$$(x-2)^2 = -\frac{1}{2}(y-4)$$

$$4 \cdot -\frac{1}{8}$$





parabola	ellipse	hyperbola
$e = 1$	$e < 1, e \neq 0$	$e > 1$
 <p> <math>e = \frac{PF}{PM}</math>  <math>e = 1</math> </p>	 <p> <math>e = \frac{PF}{PM}</math>  <math>e &lt; 1</math> </p>	 <p> <math>e = \frac{PF}{PM}</math>  <math>e &gt; 1</math> </p>

$e = 1$        $\frac{c}{a} = e < 1$        $e > 1$

Write the equation of the parabola that meets each set of conditions. Then graph the equation.

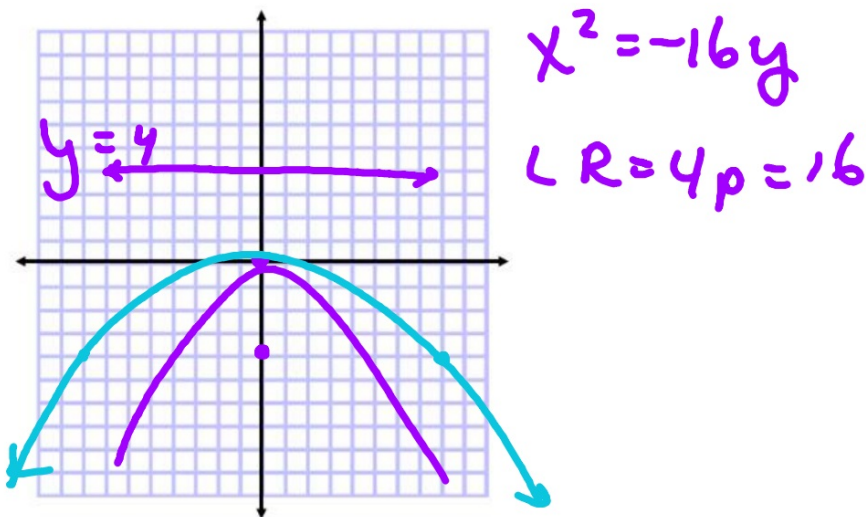
9. The vertex is at the origin, and the focus is at  $(0, -4)$ .

$$x^2 = 4py$$
$$(x-0)^2 = \underline{16}(y-0) \quad p=4$$

If you can determine  $p$ , the problem will unravel from there.

$p$ =distance:  
vertex to focus=vertex to directrix

hint: always sketch first



Write the equation:

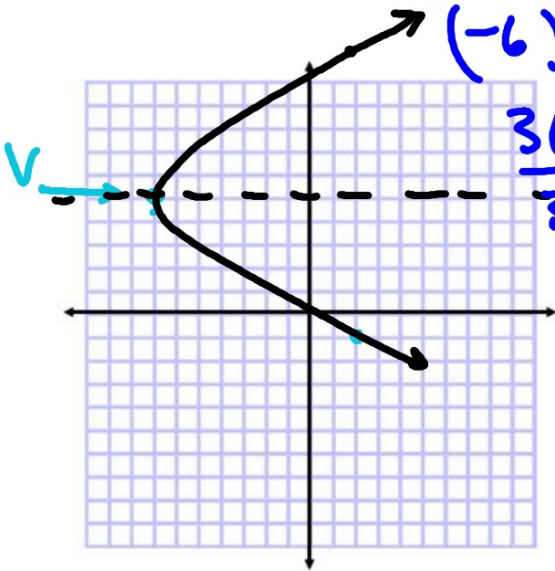
10. The parabola passes through the point  $(2, -1)$ , has its vertex at  $(-7, 5)$ , and opens to the right.

$$(y - 5)^2 = 4(x + 7)$$

$$(-1 - 5)^2 = 4p(2 + 7)$$

$$(-6)^2 = 4p(9)$$

$$\frac{36}{36} = \frac{36p}{36} \quad p = 1$$



What is the sign of  $p$ ?  
 $\oplus$

Consider  $x^2 =$  and  $y^2 =$  equations. Which one is a function?

1 Consider the equation  $y^2 = 8x + 48$ .

- Find the coordinates of the focus and the vertex and the equations of the directrix and the axis of symmetry.
- Graph the equation of the parabola.

$$y^2 = 8(x+6)$$

↑  
 $4p = 8$

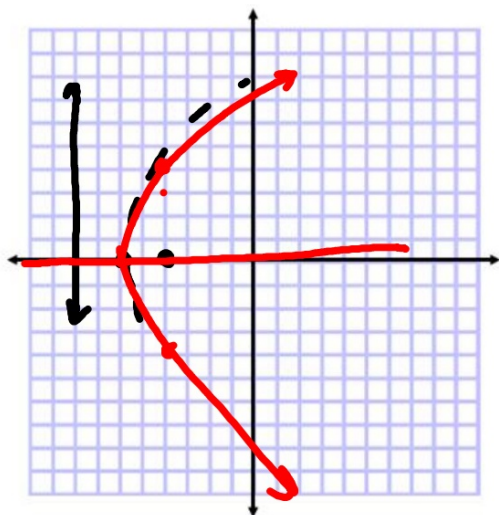
factor to find p

$$F(-4, 0)$$

$$V(-6, 0)$$

$$\text{dir } x = -8$$

$$\text{AOS } y = 0$$



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