

Precalc 11.4

Evaluate expressions involving logarithms  
Solve equations and inequalities involving logarithms  
Graph logarithmic functions and inequalities

inverse function

logarithm

logarithmic function

base

exponent

properties of exponents  $x^2 \cdot x^3$ , etc.

$$10^2 = 100 \quad \log_{10} 100 = 2$$

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**Logarithmic  
Function**

The logarithmic function  $y = \log_a x$ , where  $a > 0$  and  $a \neq 1$ , is the inverse of the exponential function  $y = a^x$ . So,  $y = \log_a x$  if and only if  $x = a^y$ .

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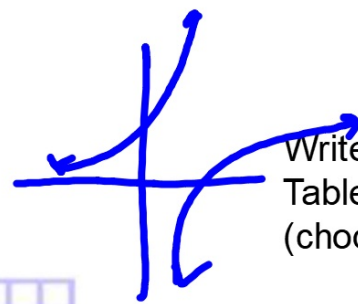
exponent =  $\log_{(\text{base})}$  number

Example:  $2 = \log_{10} 100$

6 Graph  $y = \log_3(x + 1)$ .

$3^y = x + 1$

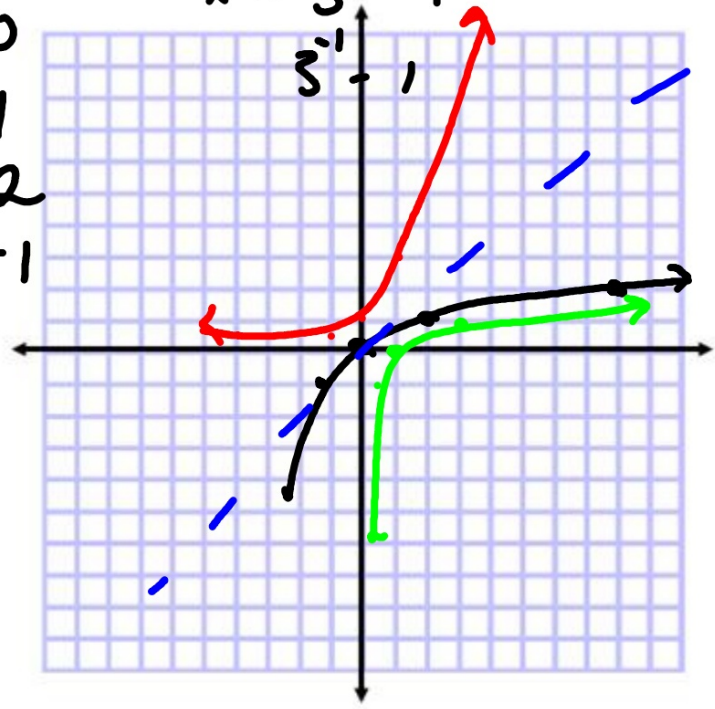
$x = 3^y - 1$



Write in exp form  
Table of values  
(choose y) ...why?

x	y
0	0
2	1
8	2
$-\frac{1}{3}$	-1

$y = 3^x$



$y =$

x	y

Graph  $y \leq \log_5 x - 2$ .

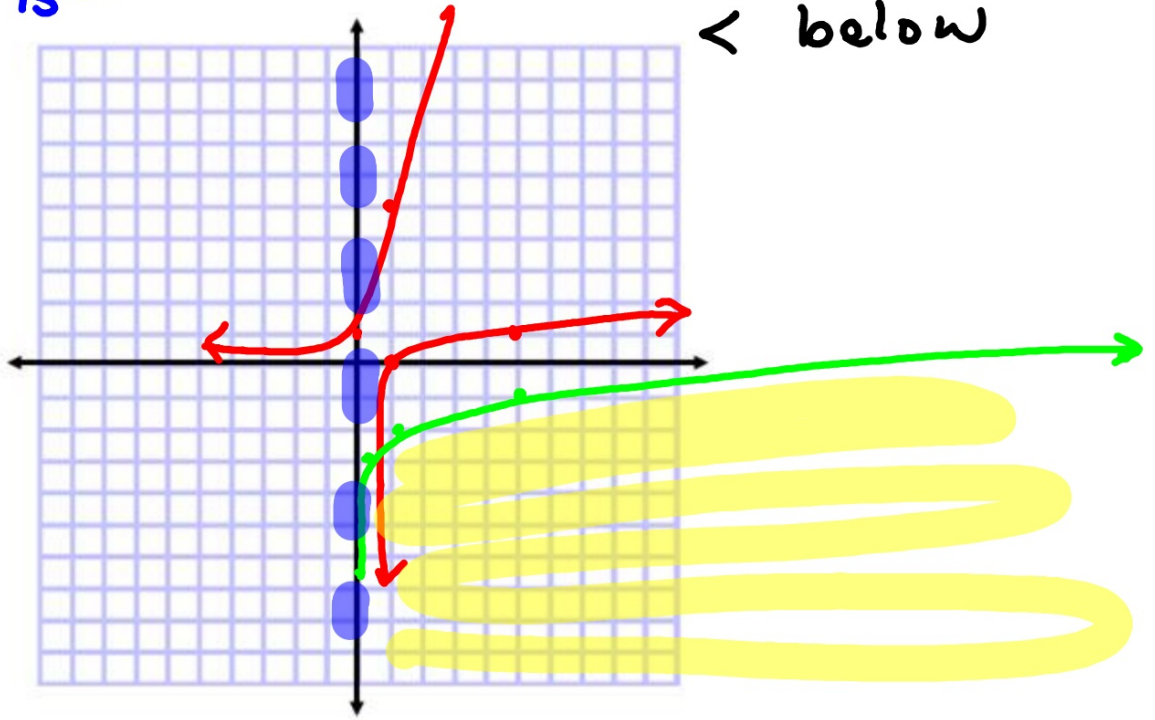
$$y = 5^x$$

$$y + 2 = \log_5 x$$

> above  
< below

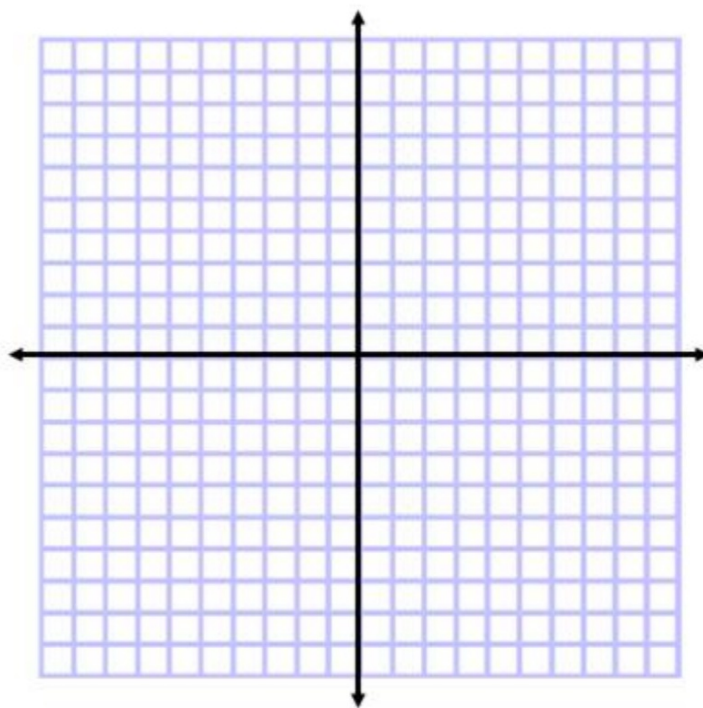
$$y+2 = \log_5 x$$
$$5 = x$$

$25$	$0$
$5$	$-1$
$1$	$-2$
$\frac{1}{5}$	$-3$

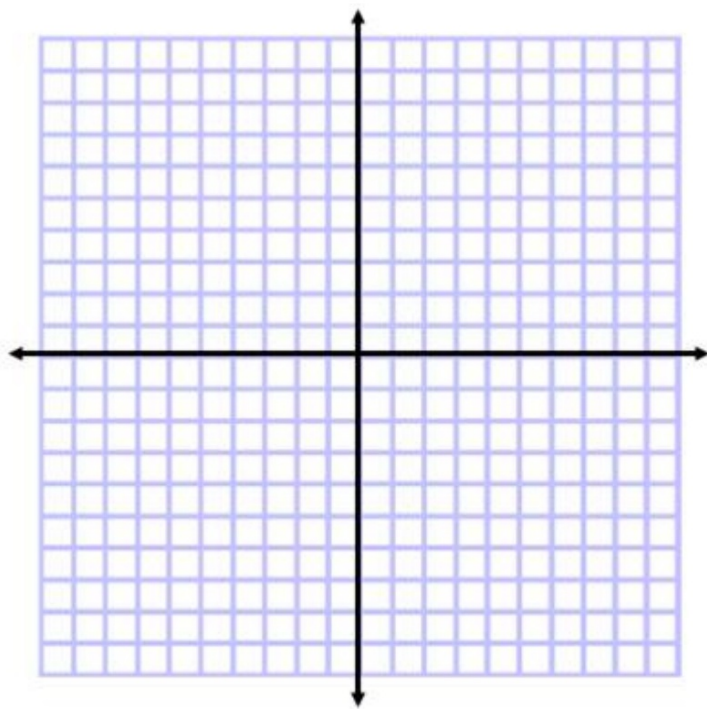


Graph each equation or inequality.

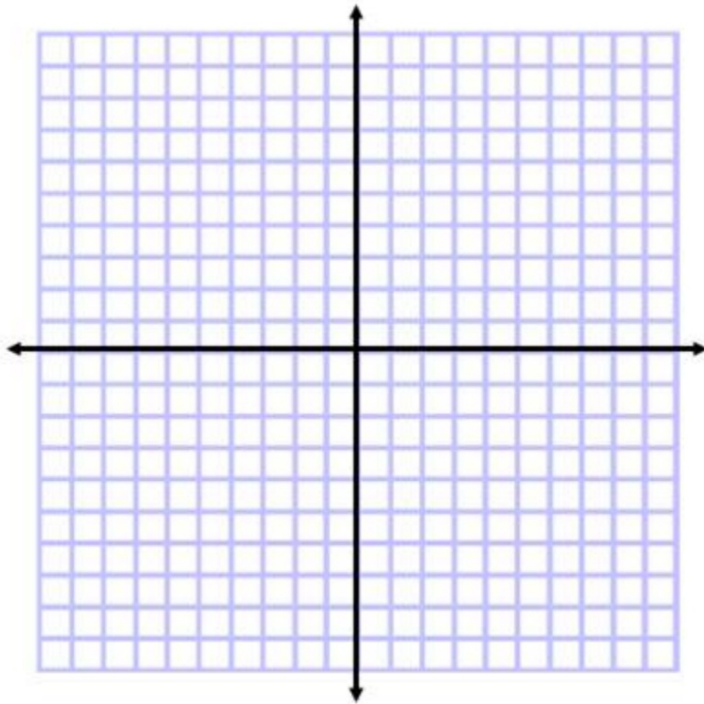
17.  $y = \log_2 x$



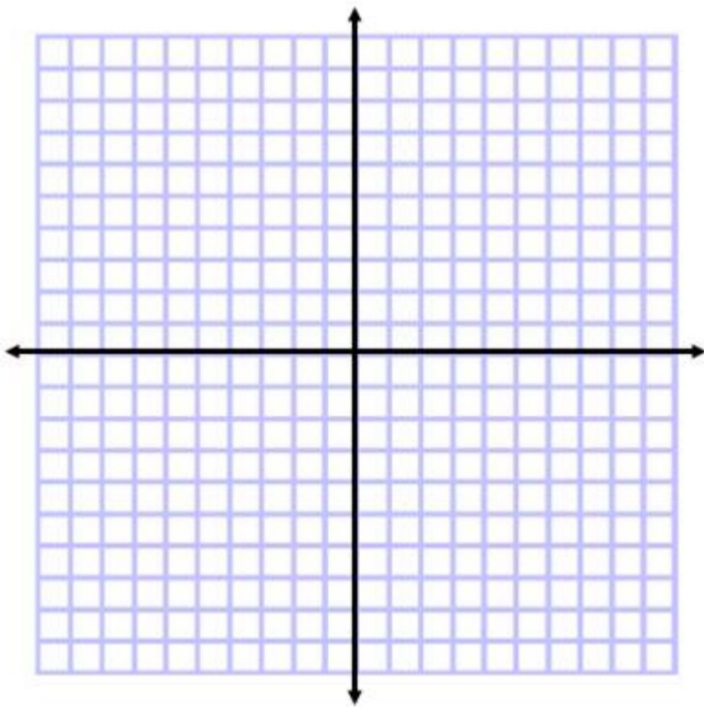
18.  $y \geq \log_6 x$



55.  $y = \log_5(x - 1)$



58.  $y > \log_{10}(x + 1)$





$$\log_4(2x-1) = \log_4 16$$

$$2x-1 = 16$$

$$\log_4 0.25 = x$$

$$4^x = \frac{1}{4} \quad 4^x = 4^{-1}$$

$$x = -1$$

