

Precalc13.6

Use the binomial theorem to calculate probability

theoretical probability

experimental probability

activity: graphing calculator simulation

1 **LANDSCAPING** Refer to the application at the beginning of the lesson.
Five mahogany trees are planted. What is the probability that at least 2 trees die?

11. **Cooking** In cooking class, 1 out of 5 soufflés that Sabrina makes will collapse. She is preparing 6 soufflés to serve at a party for her parents. What is the probability that exactly 4 of them do not collapse?

$$\left(\frac{4}{5} + \frac{1}{5} \right)^6$$

89%

4 good

$$1 \left(\frac{4}{5} \right)^6 + 6 \left(\frac{4}{5} \right)^5 \left(\frac{1}{5} \right) + 15 \left(\frac{4}{5} \right)^4 \left(\frac{1}{5} \right)^2 + 20$$

15

6

1

$$26\% + 39\% + 15\% \left(\frac{1}{5} \right) = 24\%$$

Maura guesses at all 10 questions on a true/false test. Find each probability.

17. $P(7 \text{ correct})$

18. $P(\text{at least 6 correct})$

19. $P(\text{all correct})$

20. $P(\text{at least half correct})$

$$\begin{array}{c} C \quad T \\ \left(\frac{1}{2} + \frac{1}{2}\right)^{10} \end{array}$$

$$1 \binom{10}{0}$$

$$10 \binom{10}{1}$$

$$45 \binom{10}{2}$$

$$120 \binom{10}{3} \left(\frac{1}{2}\right)^7 \left(\frac{1}{2}\right)^3 = 10$$
$$12\%$$

Kyle guesses at all of the 10 questions on his multiple choice test. Find each probability if each question has 4 choices.

24. $P(6 \text{ correct answers})$

25. $P(\text{half answers correct})$

26. $P(\text{from 3 to 5 correct answers})$

$$\binom{C}{\frac{1}{4}} + \binom{I}{\frac{3}{4}} \quad '0$$

$$1 \binom{35}{\frac{1}{4}} \quad 10$$

45

120

$$210 \left(\frac{1}{4}\right)^5 \left(\frac{3}{4}\right)^5$$

5%

$$0.0001 \\ 1 \times 10^{-22}$$

Bobby wins 2 out of every 3 chess matches he plays with Marlene.
 What is the probability that he wins exactly 5 out of the next 6 matches?

Is this binary probability?

$$\left(\frac{2}{3} + \frac{1}{3}\right)^6$$

theoretical probability:

$$1 \binom{6}{5}$$

$$6 \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)^1 = 10$$

$$\frac{64}{243} \approx 26.3\%$$

experimental probability (simulation)

rndInt(1,3,6)

W L W
 1 2 3

111000100

$$\frac{5}{10} = 50\%$$

WB 13.6
project