

Precalc15.3

Find values of integrals

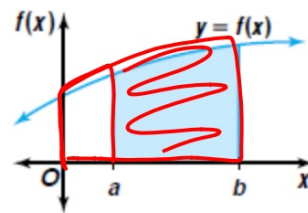
Find the area under the curve of polynomial graphs

antiderivative

integral

definite integral

integration



p. 962

$$1 + 2 + 3 + \cdots + n = \frac{n(n+1)}{2}$$

$$1^2 + 2^2 + 3^2 + \cdots + n^2 = \frac{n(n+1)(2n+1)}{6}$$

$$1^3 + 2^3 + 3^3 + \cdots + n^3 = \frac{n^2(n+1)^2}{4}$$

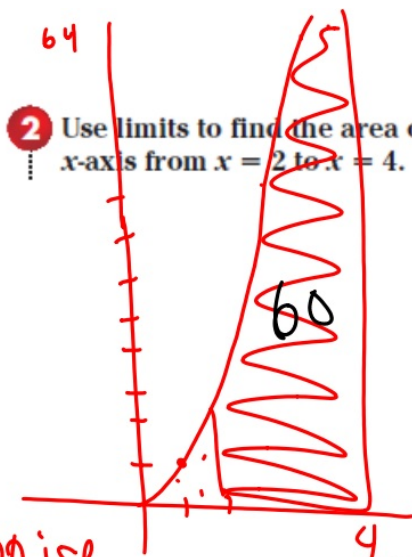
$$1^4 + 2^4 + 3^4 + \cdots + n^4 = \frac{6n^5 + 15n^4 + 10n^3 - n}{30}$$

$$1^5 + 2^5 + 3^5 + \cdots + n^5 = \frac{2n^6 + 6n^5 + 5n^4 - n^2}{12}$$

y * width

**Definite
Integral**

$$\int_a^b f(x) \, dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i) \Delta x \text{ where } \Delta x = \frac{b-a}{n}.$$



2 Use limits to find the area of the region between the graph of $y = x^3$ and the x -axis from $x = 2$ to $x = 4$.

Strategy?

$$\int_0^4 - \int_0^2$$

$$\frac{x}{n} \quad 0 + \frac{4}{n}i \quad \frac{x}{n} \quad 0 + \frac{2}{n}i$$

100 ish

(0-4) $\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{4i}{n} \right)^3 \left(\frac{4}{n} \right)$

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{256 i^3}{n^4}$$

$$\lim_{n \rightarrow \infty} \frac{256 (1^3 + 2^3 + 3^3 \dots)}{n^4}$$

$$\lim_{n \rightarrow \infty} \frac{256 \left(\frac{n^2 (n+1)^2}{4} \right)}{n^4}$$

$$\lim_{n \rightarrow \infty} \frac{64 (n^2 + 2n + 1)}{n^2}$$

64

(0-2)

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{2i}{n} \right)^3 \cdot \frac{2}{n}$$

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{16 i^3}{n^4}$$

$$\lim_{n \rightarrow \infty} \frac{16 (1^3 + 2^3 + 3^3 \dots)}{n^4}$$

$$\frac{16 (n^2 (n+1)^2)}{n^4}$$

$$\frac{16 (n^2 + 2n + 1)}{n^2}$$

4

23. $\int_3^5 8x^3 dx$

$$8 \int_3^5 x^3 dx$$

$$8 \int_0^5 \left(\frac{5i}{n}\right)^3 \left(\frac{5}{n}\right)$$

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{625i^3}{n^4}$$

$$\lim_{n \rightarrow \infty} \frac{625(1^3 + 2^3 + \dots)}{n^4} \left(\frac{625}{n^4} (n^2(n+1)^2) \right)$$

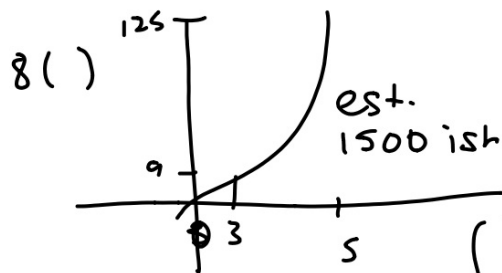
$$\lim_{n \rightarrow \infty} 186.25 (n^2 + 2n + 1)$$

$$(1250)$$

$$1250 - 162$$

$$1088$$

$$8(20.25)$$



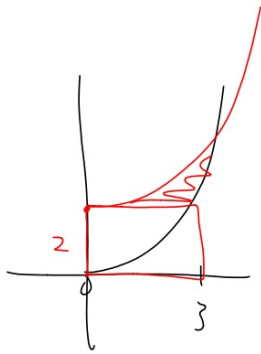
$$\int_0^3 \left(\frac{3i}{n}\right)^3 \left(\frac{3}{n}\right)$$

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{81i^3}{n^4}$$

$$\frac{81}{n^4} (n^2(n+1)^2)$$

$$\frac{81}{4} = 20.25$$

WB 15.3



$$y = x^2 + 2$$

$$y = x^2 + 6$$