Geometry 2.3

Quiz 2.1-2.2

Analyze statements in if-then form Write the converse, inverse, and contrapositive of conditional statements

conditional statement if ... then...

hypothesis if "

Conclusion Activ: If you give a mouse a cookie

related conditional

converse

inverse

It isn't about the order in the sentence...it's about what it *means*!

Words	Symbols
An <mark>if-then statement</mark> is of the form if <i>p, then q.</i>	$p \rightarrow q$ read if p then q, or p implies q
The hypothesis of a conditional statement is the phrase immediately following the word <i>if</i> .	p
The conclusion of a conditional statement is the phrase immediately following the word then.	q

If it is Christmas, then it is December.

Christinas, then it is becomber

It is December, if it's Christmas.

Are these statements the same?

Example 1 Identify the Hypothesis and Conclusion



Identify the hypothesis and conclusion of each conditional statement.

a. If the forecast is rain, then I will take an umbrella.

(m)

b. A number is divisible by 10 if its last digit is a 0.

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- 1A. If a polygon has six sides, then it is a hexagon.
- Another performance will be scheduled if the first one is sold out.

Where is the "if" (cause)? Where is the "then" (effect)?

(note: might be at the beginning, middle, or end of the sentence)

effect cause

Points will be deducted from any paper turned in after Wednesday's deadline.

Conclusion Hypothesis

If a paper is turned in after Wednesday's deadline, then points will be deducted.

Remember, the conclusion depends upon the hypothesis.

conclusion (outcome)
depends on hypothesis (cause)

Example 2 Write a Conditional in If-Then Form



Identify the hypothesis and conclusion for each conditional statement. Then write the statement in if-then form.

a. A mammal is a warm-blooded animal.

If mammel than worm 6101dod.

Note: Try writing in if/then format mathematical definitions will often work both ways "iff"

b. A prism with bases that are regular polygons is a regular prism.

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2A. Four quarters can be exchanged for a \$1 bill.

2B. The sum of the measures of two supplementary angles is 180.

if 4 gtrs can trade for \$1 if sum 180 then supp.
If supp then 180

Example 3 Truth Values of Conditionals



Determine the truth value of each conditional statement. If *true*, explain your reasoning. If *false*, give a counterexample.

a. If you divide an integer by another integer, the result is also an integer.

b. If next month is August, then this month is July.



c. If a triangle has four sides, then it is concave.





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3A. If $\angle A$ is an acute angle, then $m \angle A$ is 35.

3B. If
$$\sqrt{x} = -1$$
, then $(-1)^2 = -1$.

Notice that a conditional is false only when its hypothesis is true and its conclusion is false.

Conditional Statements				
р	q	p → q		
T	1	1		
1	F	7		
F	T	T 4		
F	F	TE		

Notice too that when a hypothesis is false, the conditional will always be considered true, regardless of whether the conclusion is true or false.

P.109

To show that a conditional is true, you must show that for each case when the hypothesis is true, the conditional is also true. To show that a conditional is false, you only need to find one counterexample.

WatchOut!

Analyzing Conditionals When analyzing a conditional, do not try to determine whether the argument makes sense. Instead, analyze the form of the argument to determine whether the conclusion follows logically from the hypothesis.

The hypothesis and the conclusion of a conditional statement can have a truth value of true or false, as can the conditional statement itself. Consider the following conditional.

If Tom finishes his homework, then he will clean his room.

Hypothesis	Conclusion	Conditional		
Tom finishes his homework.	Tom cleans his room.	If Tom finishes his homework, then he will clean his room.		
Т	Т	If Tom <i>does</i> finish his homework and he does clean his room, then the conditional is true.		
Т	F	If Tom does <i>not</i> clean his room after he does finish his homework, then he has not fulfilled his promise and the conditional is false.		
F	T	The conditional only indicates what will		
F	F	happen if Tom does finish his homework. He could clean his room or not clean his room if he does not finish his homework.		

benefit of the doubt"

When the hypothesis of a conditional is not met, the truth of a conditional cannot be determined. When the truth of a conditional statement cannot be determined, it is considered true by default.

Related Conditionals There are other statements that are based on a given conditional statement. These are known as related conditionals.

KeyConcept Related Conditionals		0.109
Words	Symbols	If Finales - Du
A conditional statement is a statement that can be written in the form if p, then q.	$p \rightarrow q$	If $M \angle A$ is 35, then $\angle A$ is an acute angle.
The converse is formed by exchanging the hypothesis and conclusion of the conditional.	$q \rightarrow p$	If A is Greeute angle, then <i>m∠A</i> is 35.
The inverse is formed by negating both the hypothesis and conclusion of the conditional.	~p → ~q	If for this that 85, Names A is not an acult angle.
The contrapositive is formed by negating both the hypothesis and the conclusion of the converse of the conditional.	~q → ~p	That Dec the if ∠A is not an acute angle, then m∠A is not 35.

If it is Christmas, then it is December. p q

(Da)

A conditional and its contrapositive are either both true or both false. Similarly, the converse and inverse of a conditional are either both true or both false. Statements with the same truth values are said to be **logically equivalent**.

KeyConcept Logically Equivalent Statements

· A conditional and its contrapositve are logically equivalent.

The converse and inverse of a conditional are logically equivalent.

Write the converse, inverse, and contrapositive of each true conditional statement. Determine whether each related conditional is *true* or *false*. If a statement is false, find a counterexample.

- 4A. Two angles that have the same measure are congruent.
- 4B. A hamster is a rodent.

-; if hunster then rodent T com if rosent then hunster. F inv. if not hunter then not rodent I Contra 1 f not redent then not housten T

