

Geometry 5.1

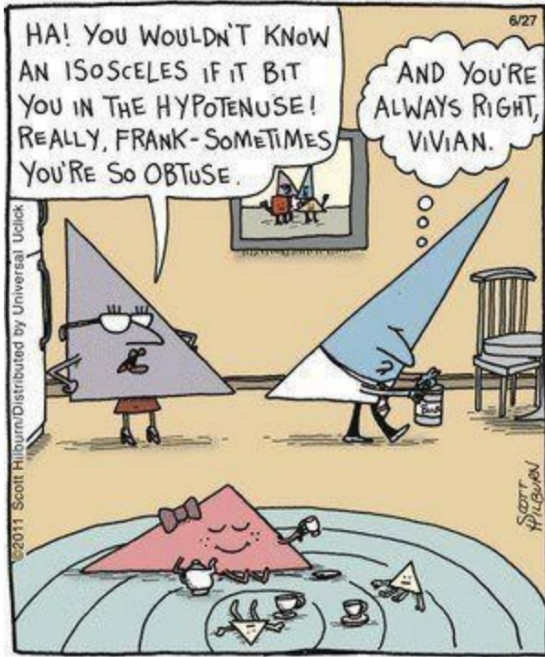
Identify and use perpendicular bisectors in triangles

Identify and use angle bisectors in triangles

perpendicular \perp 90°
bisector $2 = \text{parts}$

[concurrent lines
point of concurrency
circumcenter
incenter

activity: paper folding



MPQ

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Construction Perpendicular Bisector

Construct a perpendicular bisector of the side of a triangle.

Step 1



Draw, label, and cut out $\triangle MPQ$.

Step 2

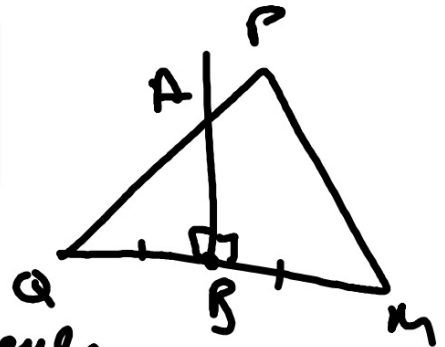


Fold the triangle in half along \overline{MQ} so that vertex M touches vertex Q .

Step 3



Use a straightedge to draw \overline{AB} along the fold. \overline{AB} is the perpendicular bisector of \overline{MQ} .



perpendicular
bisector

Construction Angle Bisector

Construct an angle bisector of a triangle.

Step 1



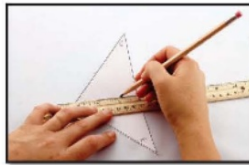
Draw, label, and cut out $\triangle ABC$.

Step 2

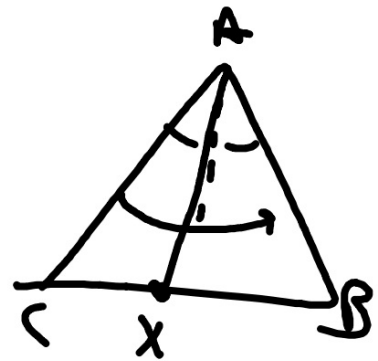


Fold the triangle in half through vertex A , such that sides \overline{AC} and \overline{AB} are aligned.

Step 3

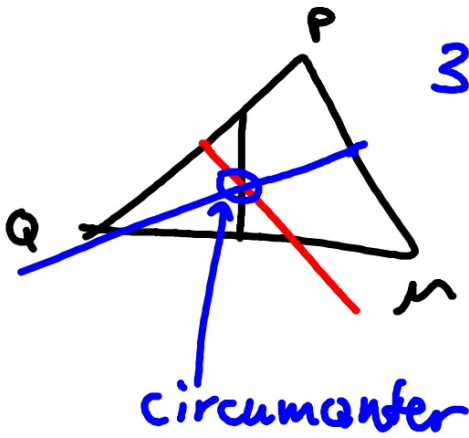


Label point L at the crease along edge \overline{BC} . Use a straightedge to draw \overline{AL} along the fold. \overline{AL} is an angle bisector of $\triangle ABC$.



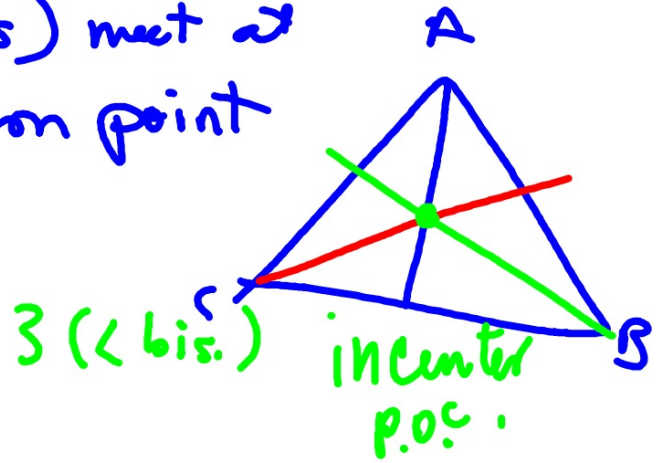
Model and Analyze

1. Construct the perpendicular bisectors and angle bisectors of the other two sides and angles of $\triangle MPQ$. What do you notice about their intersections?

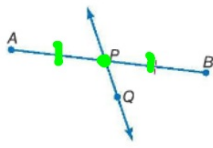


P.O.C.

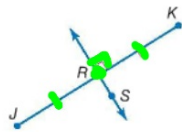
3 (\perp bis) meet at common point



1 Perpendicular Bisectors In Lesson 1-3, you learned that a segment bisector is any segment, line, or plane that intersects a segment at its midpoint. If a bisector is also perpendicular to the segment, it is called a **perpendicular bisector**.



\vec{PQ} is a bisector of \overline{AB} .



\vec{RS} is a perpendicular bisector of \overline{JK} .

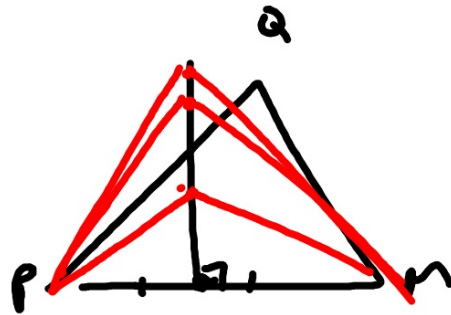
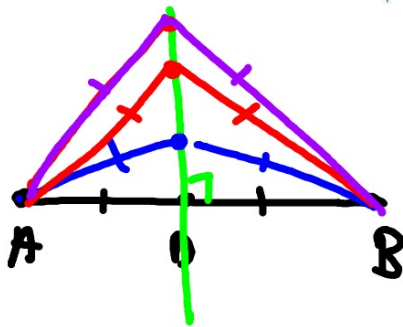
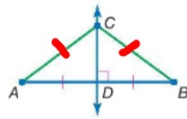
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Theorems Perpendicular Bisectors

5.1 Perpendicular Bisector Theorem

If a point is on the perpendicular bisector of a segment, then it is equidistant from the endpoints of the segment.

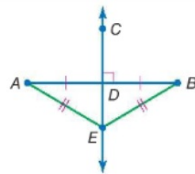
Example: If \overline{CD} is a \perp bisector of \overline{AB} , then $AC = BC$.

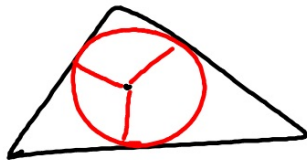


5.2 Converse of the Perpendicular Bisector Theorem

If a point is equidistant from the endpoints of a segment, then it is on the perpendicular bisector of the segment.

Example: If $AE = BE$, then E lies on \overline{CD} , the \perp bisector of \overline{AB} .



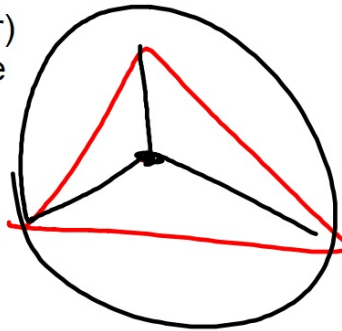


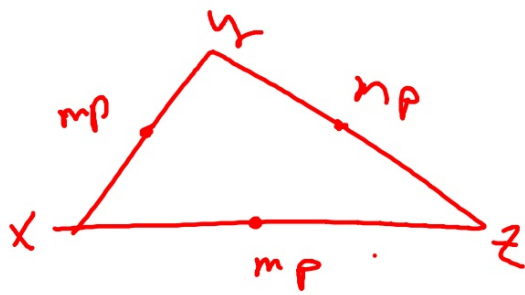
P.O.C.

POC:
Angle bisectors (incenter)
Center of inscribed circle
Equidistant from sides
(perp)

P.O.C.

Perp bisectors
(circumcenter)
Center of circumscribed
circle
Equidistant from vertices





measure (mm)