

Geometry 12.4

Find volumes of prisms*

Find volumes of cylinders**

*6th grade standard

**8th grade standard

Quiz 12.1-12.2

$B \cdot h$
volume (capacity) ^{how does} _{it hold?}
units cubic

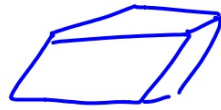
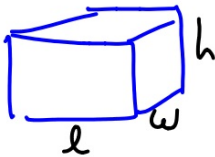
composite solid

oblique

Cavalieri's principle *deck of cards*

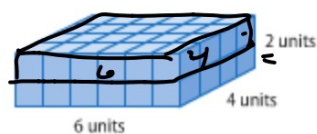
$$V = l \cdot w \cdot h$$

$$V = (B)h$$



1 Volume of Prisms Recall that the volume of a solid is the measure of the amount of space the solid encloses. Volume is measured in cubic units.

The rectangular prism at the right has $6 \cdot 4$ or 24 cubic units in the bottom layer. Since there are two layers, the total volume is $24 \cdot 2$ or 48 cubic units.

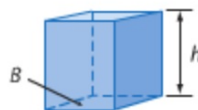


Key Concept Volume of a Prism

Words The volume V of a prism is $V = Bh$, where B is the area of a base and h is the height of the prism.

Symbols $V = Bh$

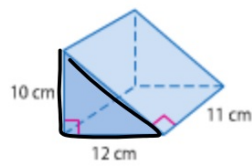
Model



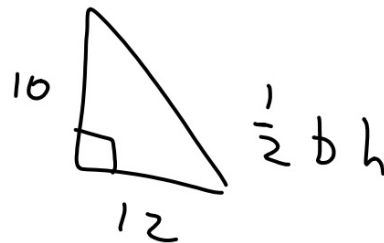
Which part is the base?

Example 1 Volume of a Prism

Find the volume of the prism.

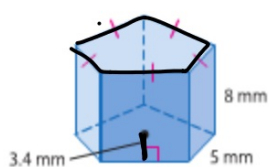


$$V = \frac{1}{2} (60) (11)$$
$$660 \text{ cm}^3$$

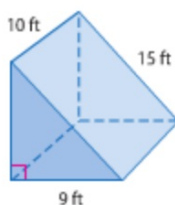


► Guided Practice

1A.

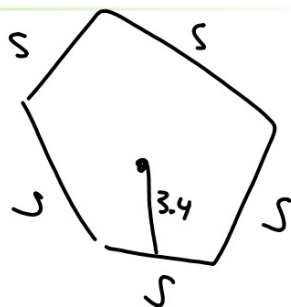


1B.



$$V = (42.5)(8)$$

$$V = 340 \text{ mm}^3$$



$$A = \frac{1}{2}ap$$

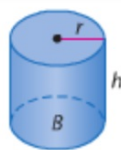
$$= \frac{1}{2}(34)25$$

$$= 42.5$$

Key Concept Volume of a Cylinder

Words The volume V of a cylinder is $V = Bh$ or $V = \pi r^2 h$, where B is the area of the base, h is the height of the cylinder, and r is the radius of the base.

Model



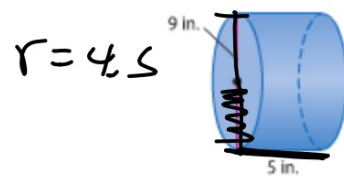
Symbols $V = Bh$

↑
circle
() ()

Example 2 Volume of a Cylinder

Find the volume of the cylinder at the right.

$$\begin{aligned} V &= (\pi \cdot 4.5^2)(5) \\ &= 318.1 \text{ in}^3 \end{aligned}$$

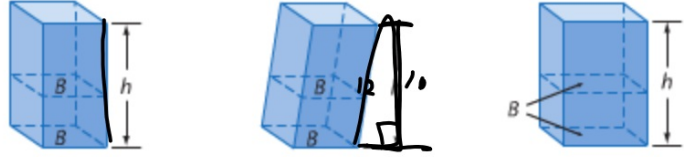


We can find volumes of oblique prisms/cylinders

Key Concept Cavalieri's Principle

Words If two solids have the same height h and the same cross-sectional area B at every level, then they have the same volume.

Models



These prisms all have a volume of Bh .

Javier Larreal/age fotostock

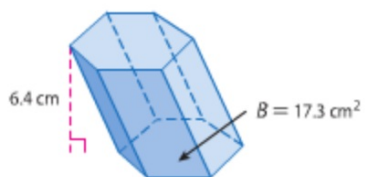
(X)

!

Example 3 Volume of an Oblique Solid



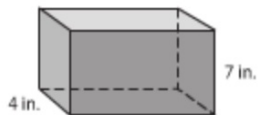
Find the volume of an oblique hexagonal prism if the height is 6.4 centimeters and the base area is 17.3 square centimeters.



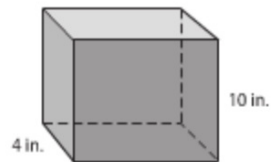


Standardized Test Example 4 Comparing Volumes of Solids

Prisms A and B have the same length and width, but different heights. If the volume of Prism B is 150 cubic inches greater than the volume of Prism A, what is the length of each prism?



Prism A



Prism B

A 10 in.

B $11\frac{1}{2}$ in.

C 12 in.

D $12\frac{1}{2}$ in.

Guided Practice

4. The containers at the right are filled with popcorn. About how many times as much popcorn does the larger container hold?

- F 1.6 times as much
- G 2.5 times as much
- H 3.3 times as much
- J 5.0 times as much

