

Geometry 8.4

Use right triangles to find trigonometric ratios

Use trig ratios to find angle measures in right triangles

opposite

adjacent

trigonometry

ratio

trig ratio

sine

cosine

tangent

inverse function (algebra 1)

SohCahToa

~~Soh~~ Cah ~~Toa~~

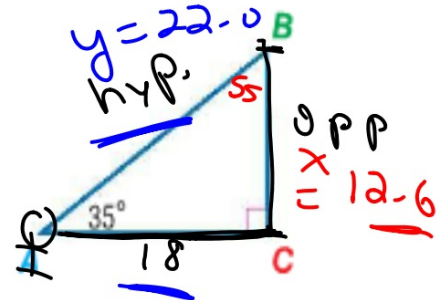
$$\tan = \frac{\text{opp}}{\text{adj}}$$

$$\tan 35^\circ = \frac{x}{18}$$

$$x = \cos = \frac{\text{adj}}{\text{hyp}}$$

$$\cos 35^\circ = \frac{18}{y}$$

$$\frac{18}{0.8192} = \frac{y}{0.8192}$$



KeyConcept Trigonometric Ratios		
Words	Symbols	
<p>If $\triangle ABC$ is a right triangle with acute $\angle A$, then the sine of $\angle A$ (written $\sin A$) is the ratio of the length of the leg opposite $\angle A$ (opp) to the length of the hypotenuse (hyp).</p>	$\sin A = \frac{\text{opp}}{\text{hyp}} \text{ or } \frac{a}{c}$ $\sin B = \frac{\text{opp}}{\text{hyp}} \text{ or } \frac{b}{c}$	
<p>If $\triangle ABC$ is a right triangle with acute $\angle A$, then the cosine of $\angle A$ (written $\cos A$) is the ratio of the length of the leg adjacent $\angle A$ (adj) to the length of the hypotenuse (hyp).</p>	$\cos A = \frac{\text{adj}}{\text{hyp}} \text{ or } \frac{b}{c}$ $\cos B = \frac{\text{adj}}{\text{hyp}} \text{ or } \frac{a}{c}$	
<p>If $\triangle ABC$ is a right triangle with acute $\angle A$, then the tangent of $\angle A$ (written $\tan A$) is the ratio of the length of the leg opposite $\angle A$ (opp) to the length of the leg adjacent $\angle A$ (adj).</p>	$\tan A = \frac{\text{opp}}{\text{adj}} \text{ or } \frac{a}{b}$ $\tan B = \frac{\text{opp}}{\text{adj}} \text{ or } \frac{b}{a}$	

Douglas Peebles Photography/Alamy

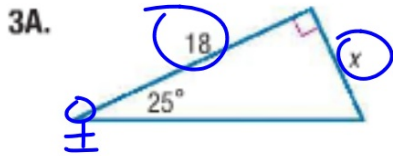
SohCahToa

Make sure your calculator is set to DEGREES

Whiteboards

Guided Practice Soh Cah Toa $\cos = \frac{\text{adj}}{\text{hyp}}$

Find x to the nearest hundredth.



$$\tan 25 = \frac{x}{18}$$
$$x = 18 \tan 25$$
$$\approx 8.39$$



$$\cos 70 = \frac{15}{x}$$
$$x(0.3420) = 15$$
$$\approx 43.86$$

sine=ratio
inverse sine=angle

Key Concept Inverse Trigonometric Ratios	
Words	If $\angle A$ is an acute angle and the sine of A is x , then the inverse sine of x is the measure of $\angle A$.
Symbols	If $\sin A = x$, then $\sin^{-1} x = m\angle A$.
Words	If $\angle A$ is an acute angle and the cosine of A is x , then the inverse cosine of x is the measure of $\angle A$.
Symbols	If $\cos A = x$, then $\cos^{-1} x = m\angle A$.
Words	If $\angle A$ is an acute angle and the tangent of A is x , then the inverse tangent of x is the measure of $\angle A$.
Symbols	If $\tan A = x$, then $\tan^{-1} x = m\angle A$.

Find angle ()⁻¹

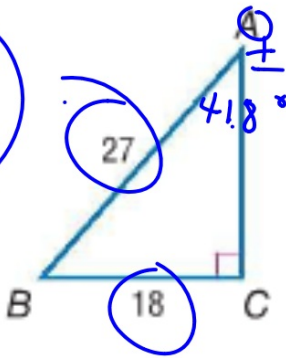
Example 4 Find Angle Measures Using Inverse Trigonometric Ratios

Use a calculator to find the measure of $\angle A$ to the nearest tenth.

Where are you?
What trig function applies?
Use inverse to find angles.

$$\cos^{-1}$$

$$\sin^{-1}\left(\frac{18}{27}\right)$$



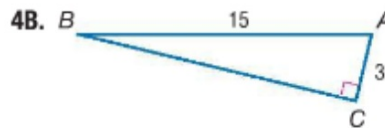
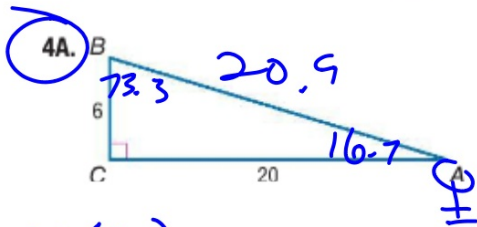
$$\sin^{-1}\left(\frac{18}{27}\right)$$

$$\sin^{-1}\left(\frac{2}{3}\right)$$

Guided Practice

Solve

Use a calculator to find the measure of $\angle A$ to the nearest tenth.



$$\tan^{-1}\left(\frac{6}{20}\right)$$

$$6^2 + 20^2 = h^2$$

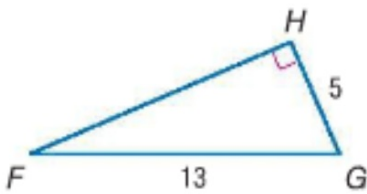
$$436$$

Solve the triangle: find all parts (6)

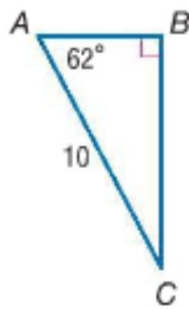
GuidedPractice

Solve each right triangle. Round side measures to the nearest tenth and angle measures to the nearest degree.

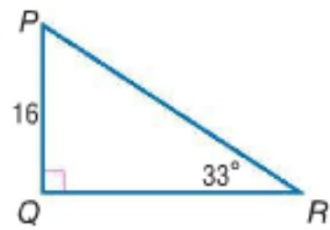
5A.



5B.



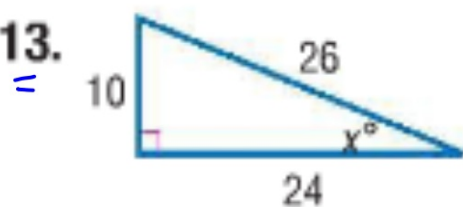
5C.



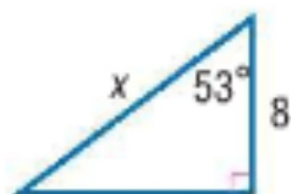
Find x . Round to the nearest tenth, if necessary.

(Lesson 8-4)

13.



14.



15. **SKATEBOARDING** Lindsey is building a skateboard ramp. She wants the ramp to be 1 foot tall at the end and she wants it to make a 15° angle with the ground. What length of board should she buy for the ramp itself? Round to the nearest foot. (Lesson 8-4)

