

Algebra 2

7.1

Graph exponential growth functions

Graph exponential decay functions

base

exponent

asymptote

domain

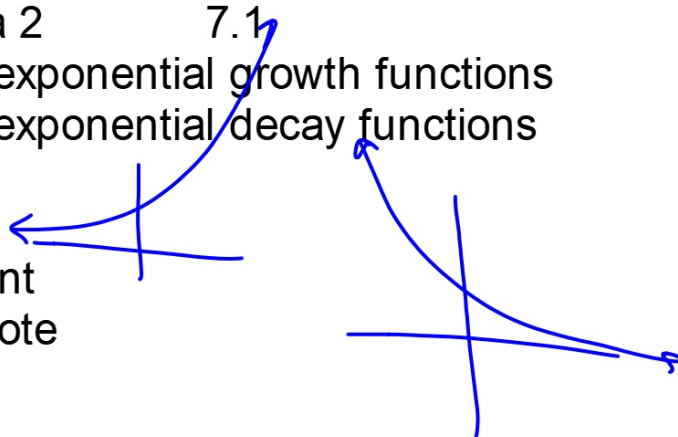
range

growth factor

decay factor

whiteboards

graph matching



## KeyConcept Parent Function of Exponential Growth Functions

Parent Functions:  $f(x) = b^x, b > 1$

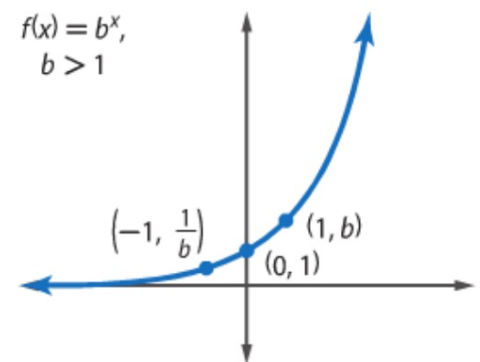
Type of graph: continuous, one-to-one, and increasing

Domain: all real numbers

Range: all positive real numbers

Asymptote:  $x$ -axis

Intercept:  $(0, 1)$



## Decay or Decrease

### KeyConcept Parent Function of Exponential Decay Functions



Parent Functions:  $f(x) = b^x, 0 < b < 1$

Type of graph: continuous, one-to-one, and decreasing

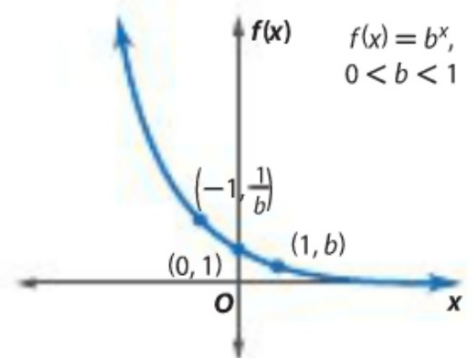
Domain: all real numbers

Range: positive real numbers

Asymptote:  $x$ -axis

Intercept:  $(0, 1)$

Model



 **KeyConcept** Transformations of Exponential Functions

$$f(x) = a b^{x-h} + k$$

**$h$  – Horizontal Translation**

$h$  units right if  $h$  is positive  
 $|h|$  units left if  $h$  is negative

**$k$  – Vertical Translation**

$k$  units up if  $k$  is positive  
 $|k|$  units down if  $k$  is negative

**$a$  – Orientation and Shape**

If  $a < 0$ , the graph is reflected in the  $x$ -axis.

If  $|a| > 1$ , the graph is stretched vertically.  
If  $0 < |a| < 1$ , the graph is compressed vertically.

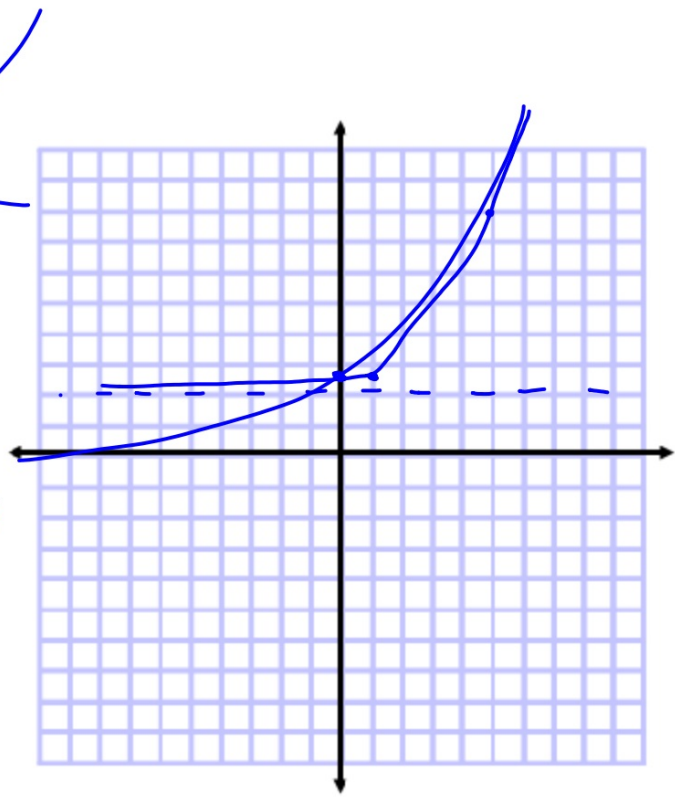
$$y = 3(2^{(x-4)}) + 2$$

↓

$$y = -3(2^{(x-4)}) + 2$$

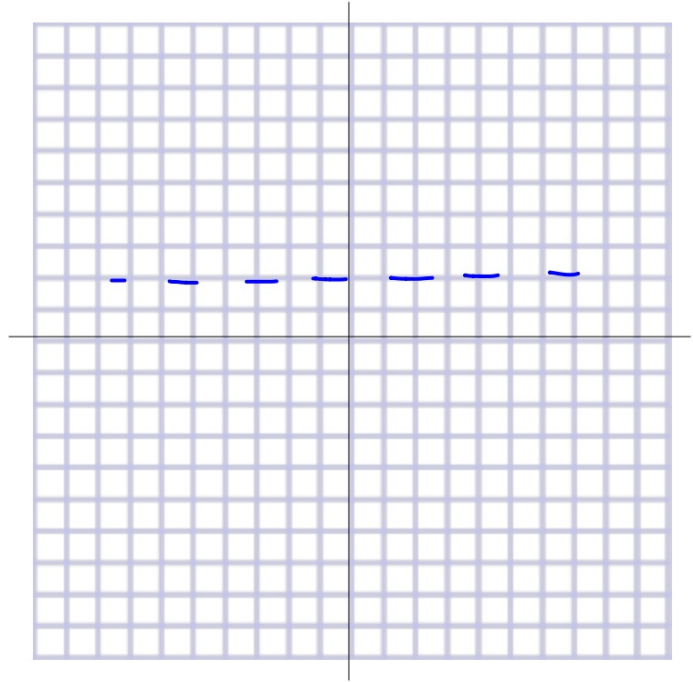
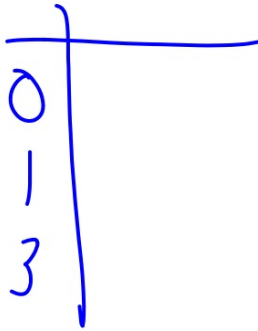
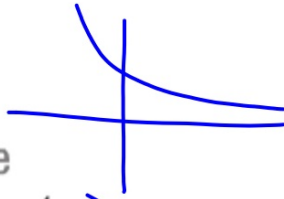
0	$3(2^{-4}) + 2$
1	$3(2^{-3}) + 2$
5	$3(2^1) + 2$

Move left/right, up/down (axis...)  
 Consider steepness (parent)  
 Use (a few) ordered pairs if needed



**Guided Practice**

4A.  $y = 3\left(\frac{2}{5}\right)^{x-4} + 2$




$$A(t) = a(1+r)^t$$

time

finke  
orb g  
% → dec.

1+r growth factor

$$A(t) = a(1-r)^t$$


1-r decay factor



6ema  
Exponential decrease...

### Real-World Example 5 Graph Exponential Decay Functions

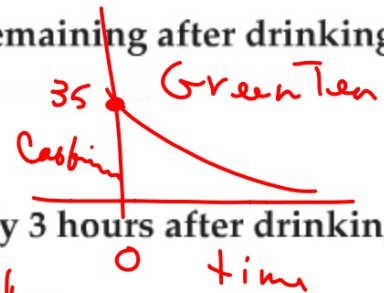


**TEA** A cup of green tea contains 35 milligrams of caffeine. The average teen can eliminate approximately 12.5% of the caffeine from their system per hour.

a. Draw a graph to represent the amount of caffeine remaining after drinking a cup of green tea.

$$35(1 - 0.125)^t$$

0.125  
0.875



b. Estimate the amount of caffeine in a teenager's body 3 hours after drinking a cup of green tea.

$$35(0.875)^3 \approx 23.4 \text{ mg}$$

**Guided Practice**

68

-12.5%

5. A cup of black tea contains about 68 milligrams of caffeine. Draw a graph to represent the amount of caffeine remaining in the body of an average teen after drinking a cup of black tea. Estimate the amount of caffeine in the body 2 hours after drinking a cup of black tea.

$$68 \left( 1 - 0.125 \right)^2$$

0.875

