

Algebra 2 7.5

Simplify and evaluate expressions using the properties of logarithms

Solve logarithmic equations

Compute pH from logarithms

logarithm = exponent

product rule

quotient rule

power^{power}

log = expon.
 $x^3 x^4$

$$\frac{x^5}{x^2}$$

$$(x^3)^4$$

4B. $\log_6(x+4) + \log_6(x+5) = 2$

$$\log_6 x(x+5) = 2$$

$$\log_6 (x^2 + 5x) = 2$$

~~$x = -9$ $x = 4$~~
 ~~$=$~~
 ~~-2~~

1 36
2 18
3 12
4 9
6 6

~~-36~~
 ~~9~~ ~~-4~~
 ~~5~~

$$x^2 + 5x = 6^2$$

$-36 \quad -36$

$$x^2 + 5x - 36 = 0$$

$$(x+9)(x-4) = 0$$

\downarrow \downarrow
 $x+9=0$ $x-4=0$

~~$x = -9$ $x = 4$~~

Solve each equation. Check your solutions.

8. $\log_4 48 - \log_4 n = \log_4 6$

$$\log_4 \left(\frac{48}{n} \right) = \log_4 6$$

$$\frac{48}{n} = \frac{6}{1}$$

$$\frac{6n}{6} = 48 \frac{1}{6} \quad n = 8$$

How is this problem different?

9. $\log_3 2x + \log_3 7 = \log_3 14$

10. ③ $\log_2 x = \log_2 8$

Whiteboards

$$\log_2 x^3 = \log_2 8$$

$$x^3 = 8$$

$$x = 2$$

$$3 \log_2 x = 1$$

$$\log_2 x^3 = 1$$

$$\sqrt[3]{2} = \sqrt[3]{x^3}$$

$$\sqrt[3]{2} = x$$

11. $\log_{10} a + \log_{10} (a - 6) = 2$

$$\log_{10} a^2 - 6a = 2$$

23. $\log_3 56 - \log_3 n = \log_3 7$

26. $\log_{10} a + \log_{10} (a + 21) = 2$

25. $5 \log_2 x = \log_2 32$

When we are multiplying...

State whether each equation is *true* or *false*.

51. $\log_8(x - 3) = \log_8 x - \log_8 3$

Explain your reasoning

$$\log_8(x-3) \neq \log_8 \frac{x}{3}$$

52. $\log_5 22x = \log_5 22 + \log_5 x$

$$\log_5 22x = \log_5 22x$$

55. $\log_7 \frac{x}{3} = \log_7 x - \log_7 3$

$$\frac{x}{3}$$

$$\begin{aligned} 58. \log_9 \frac{x^2 y^3}{z^4} &= 2 \log_9 x + 3 \log_9 y - 4 \log_9 z \\ &= \log_9 x^2 + \log_9 y^3 - \log_9 z^4 \\ &= \log_9 \frac{x^2 y^3}{z^4} \end{aligned}$$

