

Algebra 2            7.4  
Solve logarithmic equations  
Solve logarithmic inequalities  
domain  
     $x > 0$   
extraneous (solution)  
argument  
whiteboards

Quiz 7.3-7.4

e<sup>T</sup>

$$4) \log_2(8x+5) > \log_2(9x-18)$$

$$\begin{array}{r} 8x+5 > 9x-18 \\ -8x+18 \quad -8x+18 \\ \hline \end{array}$$

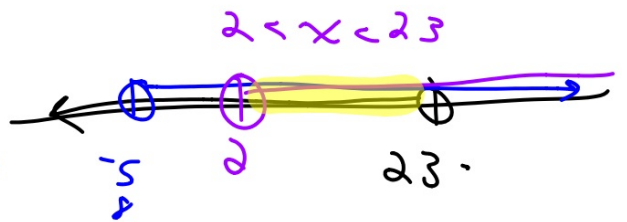
$$x < 23$$

$$23 > x$$

$$\begin{array}{l} 8x+5 > 0 \\ 8x > -5 \\ x > -\frac{5}{8} \end{array}$$


$$x > -625$$

$$\begin{array}{l} 9x-18 > 0 \\ 9x > 18 \\ x > 2 \end{array}$$



**1B.**  $\log_{16} x = \frac{5}{2}$

Try writing in exp form

 **KeyConcept** Property of Equality for Logarithmic Functions

**Symbols** If  $b$  is a positive number other than 1, then  $\log_b x = \log_b y$  if and only if  $x = y$ .

**Example** If  $\log_5 x = \log_5 8$ , then  $x = 8$ . If  $x = 8$ , then  $\log_5 x = \log_5 8$ .

2 different types of problems:      all logs same base (for now)  $b > 1$   
problem                                      only one log in the

11.  $\log_6 \frac{1}{36} = x$

14.  $\log_3(3x + 8) = \log_3(x^2 + x)$

check answers  
(argument (antilog) must be pos.)

**16.**  $\log_6 (x^2 - 6x) = \log_6 (-8)$

### Example 3 Solve a Logarithmic Inequality

Solve  $\log_3 x > 4$ .

Argument must be positive  
If = no problem.

My number vs  $3^4$

But if my exponent is bigger...



**Guided**Practice

Solve each inequality.

**3A.**  $\log_4 x \geq 3$

**3B.**  $\log_2 x < 4$

argument must be positive

### Guided Practice

4. Solve  $\log_5 (2x + 1) \leq \log_5 (x + 4)$ . Check your solution.

Solve each inequality.

4.  $\log_5 x > 3$

6.  $\log_4 (2x + 5) \leq \log_4 (4x - 3)$

7.  $\log_8 (2x) > \log_8 (6x - 8)$

28.  $\log_2(4x - 6) > \log_2(2x + 8)$

