

Algebra 2

6.5

$\sqrt{\quad} \quad (\quad)^{\frac{1}{2}}$

Simplify radical expressions

Add subtract multiply & divide radical expressions

index

like terms

radical expression

denominators

rationalizing the denominator

conjugate (4.4)

EWE

FOIL

whiteboards

$\sqrt{36}$

$\sqrt[3]{8}$

$\sqrt[4]{81}$

$\frac{2}{2} \cdot \frac{1}{2}$

$+$

$\frac{3}{4}$

$=$

$\frac{2}{4}$

$+$

$\frac{3}{4}$

$=$

$\frac{5}{4}$

$2 + \sqrt{3}$

$2 - \sqrt{3}$

$5 + i$

$5 - i$

KeyConcept Product Property of Radicals

Words For any real numbers a and b and any integer $n > 1$, $\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b}$, if n is even and a and b are both nonnegative or if n is odd.

Examples $\sqrt{2} \cdot \sqrt{8} = \sqrt{16}$ or 4 and $\sqrt[3]{3} \cdot \sqrt[3]{9} = \sqrt[3]{27}$ or 3

$\sqrt[3]{81}$ $\sqrt[3]{9} \sqrt[3]{9}$ $\sqrt{5} \sqrt{4} = \sqrt{20}$ $\sqrt[4]{5}$

$\sqrt[3]{3}$ $\sqrt[3]{3} \sqrt[3]{3}$ $2\sqrt{5}$ $\sqrt[2]{2} \sqrt[2]{5}$

(Handwritten annotations: In the first example, 81 is written above the radical, and two 3s are circled below the radical. In the second example, 20 is written above the radical, and two 2s are circled below the radical.)

Must have same index
 Take out groups of
 What to do if some are left over?

index...

Simplify is not asking for a decimal answer...take out pairs, or triplets, etc.

Example 1 Simplify Expressions with the Product Property

Simplify.

a. $\sqrt{32x^9}$

$$16^2$$

$$4^4$$

$$4x^4\sqrt{2x}$$

b. $\sqrt[4]{16a^2b^{13}}$ $\frac{2^4}{4}$ $\frac{13}{4}$ 12 R 1

$\begin{matrix} \swarrow & \searrow \\ 4 & 4 \end{matrix}$
 $\begin{matrix} \swarrow & \searrow \\ 2 & 2 \end{matrix}$ $\begin{matrix} \swarrow & \searrow \\ 2 & 2 \end{matrix}$

$$2a^b b^3 \sqrt[4]{b}$$

$$3\sqrt[3]{\quad}$$

1A. $\sqrt{17c^6d^3}$

$6 \div 2$
 $3 \div 2$

1B. $\sqrt[3]{27y^{12}z^7}$

$2c^3d\sqrt{3d}$

You can join or separate if same index

Key Concept Quotient Property of Radicals

Words For any real numbers a and $b \neq 0$ and any integer $n > 1$,

$$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}, \text{ if all roots are defined.}$$

Examples

$$\frac{\sqrt{27}}{\sqrt{3}} = \sqrt{9} \text{ or } 3 \quad \frac{\sqrt[3]{x^6}}{\sqrt[3]{8}} = \frac{\sqrt[3]{x^6}}{\sqrt[3]{8}} x^2 \text{ or } \frac{1}{2}x^2$$

$$\frac{\sqrt{27}}{\sqrt{3}} = \sqrt{9} = 3$$

$$\frac{\sqrt{27}}{\sqrt{3}}$$

$$\frac{x^2}{2} = \frac{1}{2}x^2$$

Example 2 Simplify Expressions with the Quotient Property

Simplify.

$$\begin{aligned} \text{a. } \sqrt{\frac{x^6}{y^7}} &= \frac{\sqrt{x^6}}{\sqrt{y^7}} = \frac{x^3}{y^3 \sqrt{y}} \left(\frac{\sqrt{y}}{\sqrt{y}} \right) \\ &= \frac{x^3 \sqrt{y}}{y^3 \cdot y} = \frac{x^3 \sqrt{y}}{y^4} \end{aligned} \quad \text{b. } \sqrt[4]{\frac{6}{5x}} = \frac{\sqrt[4]{6}}{\sqrt[4]{5x}} = \frac{\sqrt[4]{125x^3}}{\sqrt[4]{125x^3}} = \frac{\sqrt[4]{750x^3}}{5x}$$

Guided Practice

$$2A. \frac{\sqrt{a^9}}{\sqrt{b^5}} = \frac{a^4 \sqrt{a}}{b^2 \sqrt{b}} \cdot \frac{\sqrt{b}}{\sqrt{b}}$$

$$= \frac{a^4 \sqrt{ab}}{b^2 \cdot b}$$

$$= \frac{a^4 \sqrt{ab}}{b^3}$$

$$2B. \sqrt[5]{\frac{3}{4y}}$$

$$\frac{\sqrt[5]{3}}{\sqrt[5]{2 \cdot 2 \cdot 2y^4}}$$

$$\frac{\sqrt[5]{24y^4}}{2^2}$$

$$x^{\frac{2}{4}}$$

$$x^{\frac{1}{2}}$$

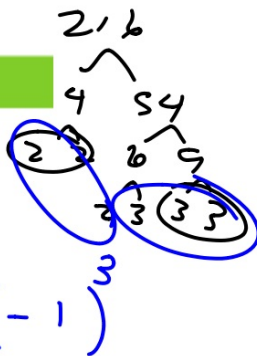
ConceptSummary Simplifying Radical Expressions

A radical expression is in simplified form when the following conditions are met.

- The index n is as small as possible. talk later...
- The radicand contains no factors (other than 1) that are n th powers of an integer or polynomial. take out pairs, etc. ...
- The radicand contains no fractions.
- No radicals appear in a denominator.

Example 3 Multiply Radicals

Simplify $5\sqrt[3]{-12ab^4} \cdot 3\sqrt[3]{18a^2b^2}$.



Must be same index to multiply
(are they?)
Multiply
Simplify your answer

$$15\sqrt[3]{-216a^3b^6} \quad (-1)^3$$

$$15\sqrt[3]{-1 \cdot 216a^3b^6}$$

$$15 \cdot 2 \cdot 3 \\ -90ab^2$$

· **Guided Practice**

Simplify.

3A. $6\sqrt{8c^3d^5} \cdot 4\sqrt{2cd^3}$

3B. $2\sqrt[4]{8x^3y^2} \cdot 3\sqrt[4]{2x^5y^2}$

$$24\sqrt{16c^4d^8}$$

$$24 \cdot 4c^2d^4$$

$$96c^2d^4$$

Like: $\sqrt{3b}$ and $4\sqrt{3b}$

Unlike: $\sqrt{3b}$ and $\sqrt[3]{3b}$

Unlike: $\sqrt{2b}$ and $\sqrt{3b}$

$$5\sqrt{3b}$$

Like: Same index & same radicand



Simplify first...they **might** be like terms...

Are they like terms????

Example 4 Add and Subtract Radicals

Simplify $\sqrt{98} - 2\sqrt{32}$.

$$\begin{aligned} & 98 \quad 7\sqrt{2} - 2 \cdot 4\sqrt{2} \\ & 49 \cdot 2 \quad -1\sqrt{2} \\ \Rightarrow & \quad 3\sqrt{2} = -\sqrt{2} \\ & 16 \cdot 2 \\ & 4 \cdot 4 \end{aligned}$$

Like: index, radicand
Guided Practice combine coeff

4A. $4\sqrt{8} + 3\sqrt{50}$

$$\begin{array}{l} 8 \\ 4 \wedge 2 \\ 2 \wedge 2 \end{array} \quad \begin{array}{l} 50 \\ 25 \wedge 2 \\ 5 \wedge 2 \end{array} \quad \begin{array}{l} 128 \\ 64 \wedge 2 \\ 8 \wedge 2 \end{array}$$

$$\begin{array}{l} 4 \cdot 2\sqrt{2} \quad 3 \cdot 5\sqrt{2} \\ 8\sqrt{2} + 15\sqrt{2} \\ 23\sqrt{2} \end{array}$$

4B. $5\sqrt{12} + 2\sqrt{27} - \sqrt{128}$

$$\begin{array}{l} 12 \\ 4 \wedge 3 \\ 2 \wedge 2 \end{array} \quad \begin{array}{l} 27 \\ 3 \wedge 3 \\ 3 \wedge 3 \end{array} \quad \begin{array}{l} 128 \\ 64 \wedge 2 \\ 8 \wedge 2 \end{array}$$

$$\begin{array}{l} 5 \cdot 2\sqrt{3} \quad 2 \cdot 3\sqrt{3} \\ 10\sqrt{3} + 6\sqrt{3} - 8\sqrt{2} \\ 16\sqrt{3} - 8\sqrt{2} \end{array}$$

EWE

Example 5 Multiply Radicals

Simplify $(4\sqrt{3} + 5\sqrt{2})(3\sqrt{2} - 6)$.

EWE

$$\begin{array}{r} 4\sqrt{3} + 5\sqrt{2} \\ 3\sqrt{2} - 6 \\ \hline \cdot \quad -24\sqrt{3} \quad -30\sqrt{2} \\ 12\sqrt{6} \quad \cancel{15\sqrt{4}} \\ \quad \quad \quad 30 \\ \hline 12\sqrt{6} + 30 - 24\sqrt{3} - 30\sqrt{2} \end{array}$$

Guided Practice

Simplify.

5A. $(6\sqrt{3} - 5)(2\sqrt{5} + 4\sqrt{2})$

5B. $(7\sqrt{2} - 3\sqrt{3})(7\sqrt{2} + 3\sqrt{3})$

$$\begin{array}{r} 6\sqrt{3} - 5 \\ 2\sqrt{5} + 4\sqrt{2} \\ \hline 12\sqrt{15} \quad 24\sqrt{6} \quad -20\sqrt{2} \\ \quad \quad \quad -10\sqrt{5} \\ \hline \end{array}$$

19-39 or 2

