

Algebra 2 4.8

Graph quadratic inequalities (functions)

Solve quadratic inequalities (equations) graphically

Solve quadratic inequalities (equations) algebraically

graph

solve

related function

vertex form

factored form

whiteboards

Quiz Fri. 4.7-4.8

$$0 \leq 0 + 0 + 4$$

Graph each inequality.

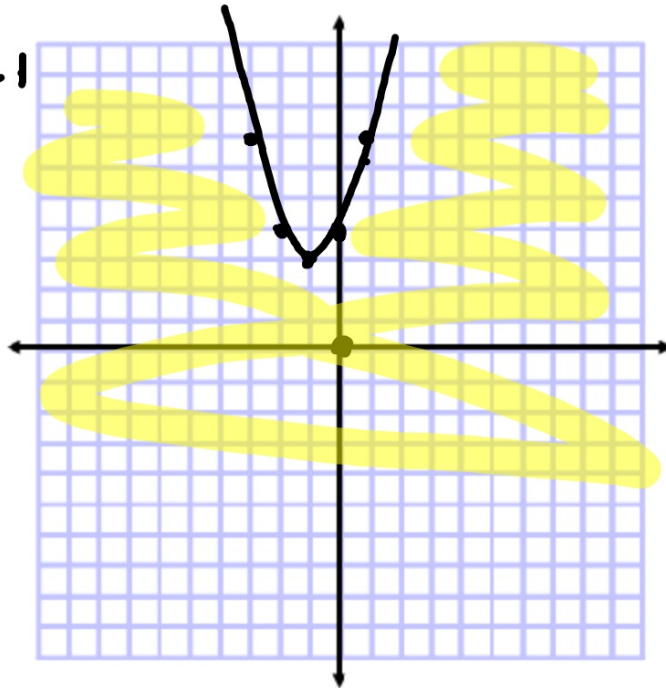
1A. $y \leq x^2 + 2x + 4$

$$y = x^2 + 2x + 4$$

$$y - 4 = (x + 1)^2$$

$$y - 3 = (x + 1)^2$$

$$y = (x + 1)^2 + 3$$



$$y = (x-h)^2 + k$$

Solve graphically

We need to know crossing points...how can we find them?

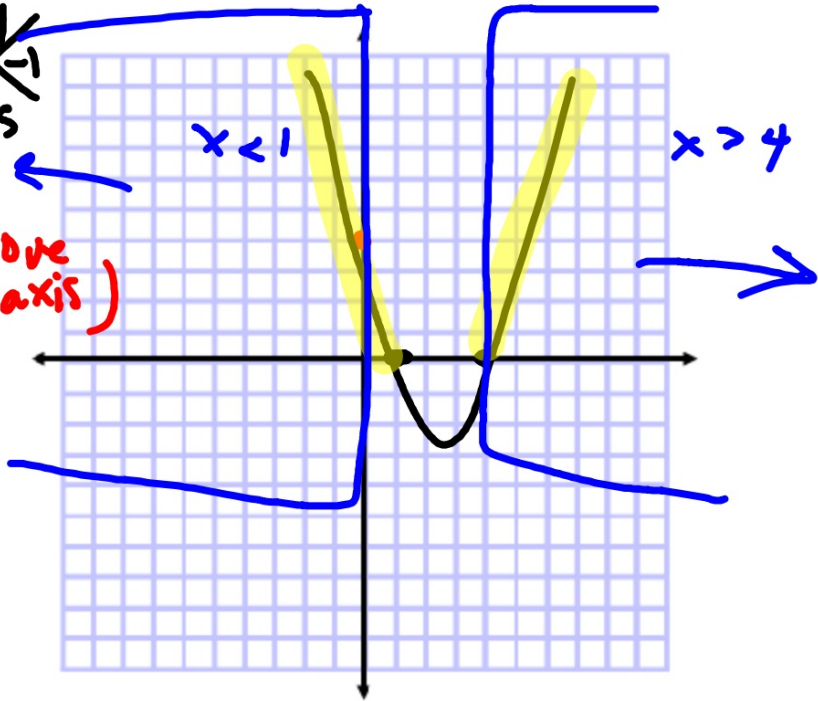
For which value(s) of x is the graph higher than zero?

4. $0 < x^2 - 5x + 4$

$\begin{array}{r} 4 \\ -5 \\ \hline -1 \end{array}$

$x^2 - 5x + 4 > 0$
pos. (above x-axis)

$y = x^2 - 5x + 4$
 $x = 4 \quad x = 1$



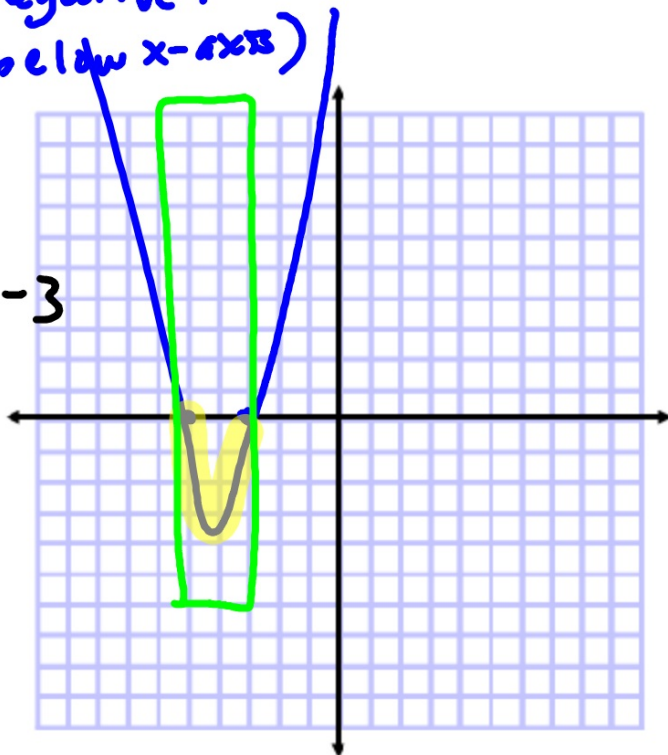
For which value(s) of x is the graph lower than zero?

5. $x^2 + 8x + 15 < 0$ negative?
(below x-axis)

$$y = x^2 + 8x + 15$$

$$\begin{array}{r} 15 \\ 5 \times 3 \\ \hline 8 \end{array} \quad -5 < x < -3$$

$$x = -5 \quad x = -3$$



Solve algebraically (another method):

Solve related equation

(Divides number line into zones)

Test a point from each zone

Answers are the same as if solved graphically

$$110 - 30 \leq 18$$

Example 5 Solve a Quadratic Inequality Algebraically

Solve $x^2 - 3x \leq 18$ algebraically.

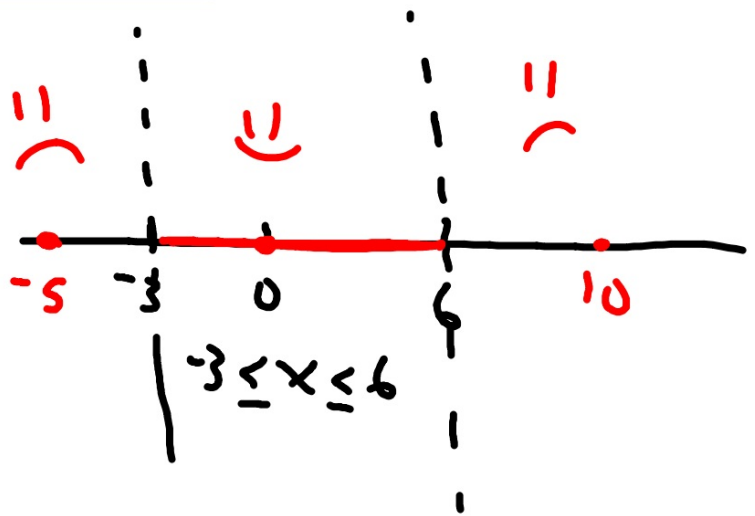
$$x^2 - 3x = 18$$

$$x^2 - 3x - 18 = 0$$

$$\begin{array}{r} -18 \\ -6 \quad 3 \\ \hline -3 \end{array}$$

$$(x-6)(x+3) = 0$$

$$x = 6 \quad x = -3$$



$$\begin{array}{l} 0+0 < -6 \\ 0 < -6 \end{array}$$

Guided Practice

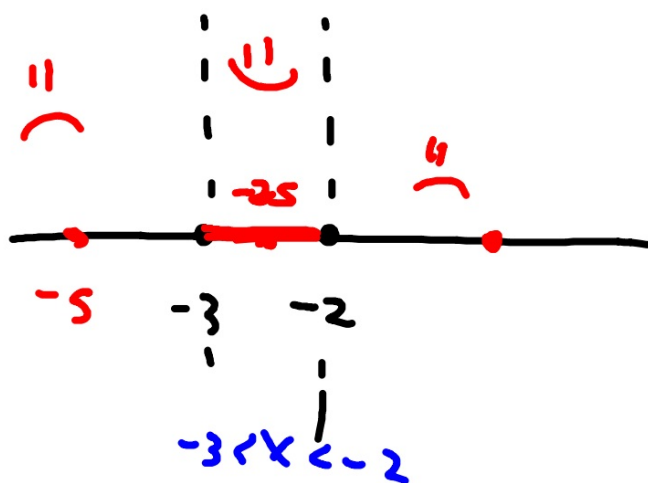
Solve each inequality algebraically.

5A. $x^2 + 5x < -6$

$$x^2 + 5x = -6$$

$$x^2 + 5x + 6 = 0$$

$$\begin{array}{c} \begin{array}{cc} 6 & \\ 3 & 2 \\ \hline 5 & \end{array} \\ (x+3)(x+2) = 0 \\ x = -3 \quad x = -2 \end{array}$$



$$100 + -110 + 30 \geq 0$$

$$5B. x^2 + 11x + 30 \geq 0$$

$$x^2 + 11x + 30 = 0$$

$$\begin{array}{r} 30 \\ \times \\ 6 \quad 5 \\ \hline 11 \end{array} \quad (x+6)(x+5) = 0$$

$x = -6 \quad x = -5$

