

Algebra 2 8.1
Simplify rational expressions
Simplify complex fractions

rational
simplify (a fraction)
GCF

$$\frac{1}{x-3}$$

~~X~~ Is it ever OK to divide by zero?
complex fraction
whiteboards

Answer when undefined only if they ask (for now...)

• **Guided Practice**

Simplify each expression.

3A. $\frac{(xz - 4z)}{z^2(4 + x)}$

$\uparrow$

$\frac{\cancel{z}(x - 4)}{\cancel{z} \cdot \cancel{z}(-1)(x - 4)}$

$$\frac{1}{-z} = \frac{-1}{z}$$

—

► **Guided Practice**

4A. $\frac{12c^3d^2}{21ab} \cdot \frac{14a^2b}{8c^2d}$

$$\begin{array}{r} \cancel{2} \cancel{2} \cancel{3} \quad \quad \quad \cancel{2} \cancel{7} \\ 12 \cancel{c} \cancel{c} \cancel{c} \cancel{d} \cancel{2} \cancel{1} \cancel{4} \cancel{a} \cancel{a} \cancel{b} \\ \hline 2 \cancel{1} \cancel{a} \cancel{b} \quad 8 \cancel{c} \cancel{c} \cancel{d} \\ \cancel{3} \cancel{7} \quad \quad \quad \cancel{2} \cancel{2} \cancel{2} \end{array}$$

4B. $\frac{6xy}{15ab^2} \cdot \frac{21a^3}{18x^4y}$

$$4C. \frac{16mt^2}{21a^4b^3} \div \frac{24m^3}{7a^2b^2}$$

$$\frac{16mt^2}{21a^4b^3} \cdot \frac{7a^2b^2}{24m^3}$$

$$\frac{16 \cancel{m} t^2}{3 \cancel{7} a^{\cancel{4}2} \cancel{b}^{\cancel{3}1}} \cdot \frac{\cancel{7}^1 a^2 \cancel{b}^{\cancel{2}1}}{\cancel{24}^3 m^{\cancel{3}1}}$$

$$\frac{2 t^2}{9 a^2 m b}$$

$$4D. \frac{12x^4y^2}{40a^4b^4} \div \frac{6x^2y^4}{16a^2x}$$

$$\frac{12x^4y^2}{40a^4b^4} \cdot \frac{16a^2x}{6x^2y^4}$$

$$\frac{2x^{\cancel{4}2} t^2}{5 a^{\cancel{4}2} m^{\cancel{4}2} b^4}$$

$$\frac{2}{5} \frac{t^2}{a^2 m^2 b^4}$$

Example 5 Polynomials in the Numerator and Denominator

Simplify each expression.

a. $\frac{x^2 - 6x - 16}{x^2 - 16x + 64} \cdot \frac{x - 8}{x^2 + 5x + 6}$

$$\frac{1}{3} \cdot \frac{2}{5}$$

$$\frac{(\cancel{x-8})(\cancel{x+2})}{(\cancel{x-8})(\cancel{x-8})} \cdot \frac{(\cancel{x-8})}{(\cancel{x+3})(\cancel{x+2})} = \frac{1}{x+3}$$

b. $\frac{x^2 - 16}{12y + 36} \div \frac{x^2 - 12x + 32}{y^2 - 3y - 18}$

Guided Practice

5A. $\frac{8x - 20}{x^2 + 2x - 35} \cdot \frac{x^2 - 7x + 10}{4x^2 - 16}$

5B. $\frac{x^2 - 9x + 20}{x^2 + 10x + 21} \div \frac{x^2 - x - 12}{6x + 42}$

$$\frac{1}{4} \div \frac{3}{8}$$

Multiply by recip (why does that work?)

Example 6 Simplify Complex Fractions

Simplify each expression.

a.
$$\frac{\frac{a+b}{4}}{\frac{a^2+b^2}{4}}$$

b. $\frac{\frac{x^2}{x^2 - y^2}}{\frac{4x}{y - x}}$

Guided Practice

Simplify each expression.

6A.
$$\frac{\frac{(x-2)^2}{2(x^2-5x+4)}}{\frac{x^2-4}{4x-10}}$$

6B. $\frac{\frac{x^2 - y^2}{y^2 - 49}}{\frac{y - x}{y + 7}}$