

\geq \leq

Algebra 1

5.3

Solve multi-step linear inequalities*

Use the distributive property to solve linear inequalities*

$$\begin{aligned} 3(x+2) \\ 3 \cdot x + 3 \cdot 2 \\ 3x + 6 \end{aligned}$$

*7th grade standard

order of operations

distributive property

inequality

empty set

all real numbers

$$\begin{aligned} x + 3 &= 5 \\ -3 \quad -3 \\ \hline x &= 2 \end{aligned}$$

$$\begin{aligned} 2x &= 10 \\ \frac{2x}{2} &= \frac{10}{2} \\ x &= 5 \end{aligned}$$

Whiteboards

Triangle puzzle

$$\begin{aligned} 2x + 1 &= 7 \\ -1 \quad -1 \\ \hline 2x &= 6 \\ \frac{2x}{2} &= \frac{6}{2} \\ x &= 3 \end{aligned}$$

What are steps to solve a multi-step EQUATION?

± zero pair

X ÷ solve

X =

What would you do to solve an equation?

Example 2 Inequality Involving a Negative Coefficient

Solve $-11y - 13 > 42$. Graph the solution on a number line.

$$\begin{array}{r} -11y - 13 = 42 \\ + 13 + 13 \\ \hline -11y = 55 \\ \div -11 \div -11 \\ y = -5 \end{array}$$

$$\begin{array}{r} -11y - 13 > 42 \\ + 13 + 13 \\ \hline -11y > 55 \\ \div -11 \div -11 \\ y < -5 \end{array}$$



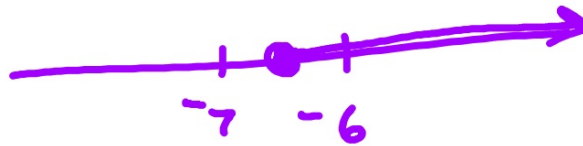
$$2A. 23 \geq 10 - 2w$$

$$\frac{-10}{-2} \quad \frac{-10}{-2}$$

$$\frac{13}{-2} \geq \frac{-2w}{-2}$$

$$-\frac{13}{2} \leq w$$

$$-6.5$$



$$2B. 43 > -4y + 11$$

$$\begin{array}{r} -11 \\ -11 \end{array}$$

$$\frac{+32}{-4} > \frac{-4y}{-4}$$

$$-8 < y$$

$$43 > -4y + 11$$

$$\begin{array}{r} -11 \\ -11 \end{array}$$

$$\frac{32}{-4} > \frac{-4y}{-4}$$

$$-8 < y$$



Triangle puzzle

Example 3 Write and Solve an Inequality



Define a variable, write an inequality, and solve the problem.

Five minus 6 times a number is more than four times the number plus 45.

$$\begin{array}{r} 5 - 6n > 4n + 45 \\ -45 + 6n \quad +6n - 45 \\ \hline -40 > 10n \\ \frac{-40}{10} > \frac{10n}{10} \\ -4 > n \end{array}$$

GuidedPractice

3. *Two more than half of a number is greater than twenty-seven.*

Example 4 Distributive Property

Solve $4(3t - 5) + 7 \geq 8t + 3$. Graph the solution on a number line.

$$4 \cdot 3t \quad 4 \cdot 5$$

$$12t - 20 + 7 \geq 8t + 3$$

$$\begin{array}{r} 12t + 13 \geq 8t + 3 \\ -8t \quad +13 \quad -8t \quad +13 \end{array}$$

$$\frac{4t}{4} \geq \frac{16}{4}$$

$$t \geq 4$$

4A. $6(5z - 3) \leq 36z$

4B. $2(h + 6) > -3(8 - h)$

What does it look like when there is no solution to an equation?

What does it look like when the solution is all real numbers?

Example 5 Empty Set and All Reals

Solve each inequality. Check your solution.

a. $9t - 5(t - 5) \leq 4(t - 3)$

b. $3(4m + 6) \leq 42 + 6(2m - 4)$

Solve each inequality. Check your solution.

5A. $18 - 3(8c + 4) \geq -6(4c - 1)$

5B. $46 \leq 8m - 4(2m + 5)$