

Algebra 1 6.2

Solve systems of equations using substitution method

Solve problems using substitution of equations

solve

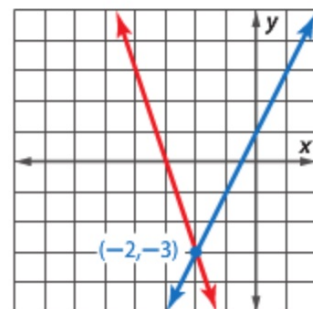
solve by graphing ||

substitution

“ substitution method “
replace with something =

activity: cut & paste

whiteboards



Are there ever any complications when solving by graphing?

• $x = 3$

•

recipe: if you run out of one ingredient...
coach: two players are equally skilled...

$$\begin{array}{l} 5x + y = 18 \\ 5 \cdot 3 + y = 18 \\ 15 + y = 18 \\ -15 \quad y \quad -15 \end{array}$$

Cut & paste activity

$$3x - y = 1$$

$$3 \cdot (-1) - (-4) = 1$$

$$-3 + 4 = 1$$

$$\text{☺}(-1, -4)\text{☺}$$

$$-4 = 4 \cdot (-1)$$

$$y = 4x$$

$$3x - 4x = 1$$

$$-1x = 1$$

$$x = -1$$

$$\begin{array}{l} 2 \cdot 5 - 5 = 5 \\ 10 - 5 = 5 \end{array} \quad \begin{array}{l} 2x - x = 5 \\ x = 5 \end{array} \quad \begin{array}{l} 5 = 5 \\ y = x \end{array}$$

$$2x - x = 5$$

$$x = 5$$

$$\Rightarrow (5, 5) \Rightarrow$$

$$\begin{array}{r} 2 \cdot 5 - y = 5 \\ 10 - y = 5 \\ -10 \quad \quad -10 \\ \hline -y = -5 \\ \frac{-y}{-1} = \frac{-5}{-1} \end{array}$$



Example 1 Solve a System by Substitution

Use substitution to solve the system of equations.

Step 1 The first equation is already solved for y .

$y = 2x + 1$
 $3x + y = -9$

$3 \cdot 2 + -3 = -9$
 $3x + 2x + 1 = -9$
 $5x + 1 = -9$
 $5x = -10$
 $x = -2$

$y = 2 \cdot -2 + 1$
 $y = -4 + 1$
 $y = -3$

$(-2, -3)$

You are the coach...
Who is on the sub list?

KeyConcept Solving by Substitution

Step 1 When necessary, solve at least one equation for one variable.

Step 2 Substitute the resulting expression from Step 1 into the other equation to replace the variable. Then solve the equation.

Step 3 Substitute the value from Step 2 into either equation, and solve for the other variable. Write the solution as an ordered pair.

Guided Practice

1A. $y = 4x - 6$
 $5x + 3y = -1$

$$\Rightarrow (1, -2) \Rightarrow$$

$$5x + 3(4x - 6) = -1$$

$$5x + 12x - 18 = -1$$

$$\begin{array}{r} 17x - 18 = -1 \\ +18 \quad +18 \end{array}$$

$$\hline \begin{array}{r} 17x = 17 \\ \underline{17} \quad \underline{17} \end{array}$$

$$-2 = 4 \cdot 1 - 6$$

$$-2 = 4 - 6$$

$$5 \cdot 1 + 3 \cdot -2 = -1$$

$$5 + -6 = -1$$

$$2 \cdot -3 + 5 \cdot 1 = -1 \quad \text{☺} (-3, 1) \text{☺}$$

$$-6 + 5 = -1$$

$$1B. 2x + 5y = -1$$

$$y = 3x + 10$$

$$1 = 3 \cdot -3 + 10$$

$$1 = -9 + 10$$

$$y = 3 \cdot -3 + 10$$

$$= -9 + 10$$

$$2x + 5(3x + 10) = -1$$

$$2x + 15x + 50 = -1$$

$$17x + 50 = -1$$

$$\begin{array}{r} -50 \quad -50 \\ \hline 17x = -51 \\ \frac{17x}{17} = \frac{-51}{17} \quad x = -3 \end{array}$$

How is this problem different?

Example 2 Solve and then Substitute

Use substitution to solve the system of equations.

$$\begin{aligned}x + 2y &= 6 \\ 3x - 4y &= 28\end{aligned}$$

$$\Rightarrow x = -2y + 6$$

$$(8, -1)$$

$$3(-2y + 6) - 4y = 28$$

$$8 + 2 \cdot -1 = 6$$

$$8 + -2 = 6$$

$$-6y + 18 - 4y = 28$$

$$x = -2 \cdot -1 + 6$$

$$-10y + 18 = 28$$

$$3 \cdot 8 - 4 = 1 = 28$$

$$24 + 4 = 28$$

$$x = 2 + 6$$

$$x = 8$$

$$\begin{array}{r} -10y + 18 = 28 \\ \hline -10y = 10 \\ y = -1 \end{array}$$

Guided Practice

2A. $4x + 5y = 11$

$y - 3x = -13$

$+3x \quad +3x$

$y = 3x - 13$

6.2 skills
1-11 odd

2B. $x - 3y = -9$
 $5x - 2y = 7$