

Algebra 1 2.4

Solve equations with the variable on each side.  
Solve equations with grouping symbols.

identity  
no solution  
all real numbers

$$\begin{array}{r} 3x + 5 = 2x + 4 \\ -2x \quad -2x \\ \hline x + 5 = 4 \\ -5 \quad -5 \\ \hline x = -1 \end{array}$$

Algebra tiles

$$3x + 5 = 2x + 4$$

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$$\begin{array}{r} 2 + 5k = 3k + 6 \\ -3k \quad -3k \\ \hline 2 + 2k = -6 \\ -2 \quad -2 \\ \hline 2k = -8 \\ \frac{2k}{2} = \frac{-8}{2} \\ k = -4 \end{array}$$

**Example 1** Solve an Equation with Variables on Each Side

Solve  $2 + 5k = 3k - 6$ . Check your solution.

$$\begin{array}{r} 2 + 5k = 3k + 6 \\ -3k \quad -3k \\ \hline 2 + 2k = -6 \\ -2 \quad -2 \\ \hline 2k = -8 \\ \frac{2k}{2} = \frac{-8}{2} \\ k = -4 \end{array}$$

Solve each equation. Check your solution.

1A.  $3w + 2 = 7w$

1B.  $5a + 2 = 6 - 7a$

1C.  $\frac{x}{2} + 1 = \frac{1}{4}x - 6$

1D.  $1.3c = 3.3c + 2.8$

$$\begin{array}{r} 3w + 2 = 7w \\ -3w \quad -3w \\ \hline 2 = 4w \\ \frac{2}{4} = \frac{4w}{4} \end{array} \quad w = \frac{1}{2}$$

$$\begin{array}{r} 5a + 2 = 6 - 7a \\ -5a \quad -5a \\ \hline 2 = 6 - 12a \\ -6 \quad -6 \\ \hline -4 = -12a \\ \frac{-4}{-12} = \frac{-12a}{-12} \\ \frac{1}{3} = a \end{array}$$

1.  $3c = 3.3c + 2.8$

$$\begin{array}{r} 1.3c = 3.3c + 2.8 \\ -1.3c \quad -1.3c \\ \hline 0 = 2c + 2.8 \\ -2.8 \quad -2.8 \\ \hline 0 = 2c + 2.8 \\ \frac{-2.8}{2} = \frac{2c}{2} \\ c = -1.4 \end{array}$$

Solve each equation. Check your solution.

2A.  $8s - 10 = 3(6 + 2s)$

$$\begin{array}{r} 8s - 10 = 18 + -6s \\ +6s \qquad \qquad +6s \end{array}$$

$$\begin{array}{r} 14s - 10 = 18 \\ +10 \quad +10 \\ \hline 14s = 28 \\ \hline 14 \quad 14 \end{array}$$

$$s = 2$$

2B.  $7(n - 1) = -2(3 + n)$

$$\begin{array}{r} 7n - 7 = -6 + 2n \\ 2n \qquad \qquad 2n \end{array}$$

$$\begin{array}{r} 9n - 7 = -6 \\ +7 \quad +7 \end{array}$$

$$\frac{9n}{9} = \frac{1}{9}$$

$$n = \frac{1}{9}$$

**Example 3** Find Special Solutions

Solve each equation.

a.  $5x + 5 = 3(5x - 4) - 10x$

b.  $3(2b - 1) - 7 = 6b - 10$

**3A.**  $7x + 5(x - 1) = -5 + 12x$

**3B.**  $6(y - 5) = 2(10 + 3y)$

**ConceptSummary** Steps for Solving Equations



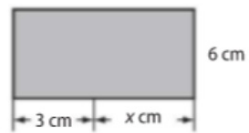
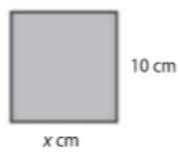
**Step 1** Simplify the expressions on each side. Use the Distributive Property as needed.

**Step 2** Use the Addition and/or Subtraction Properties of Equality to get the variables on one side and the numbers without variables on the other side. Simplify.

**Step 3** Use the Multiplication or Division Property of Equality to solve.

**Standardized Test Example 4 Write an Equation**

Find the value of  $x$  so that the figures have the same area.



A 3

B 4.5

C 6.5

D 7