

Algebra 1

4.7

Quiz 4.5-4.6

Find the inverse of a relation

Find the inverse of a linear function

relation

inverse

function

inverse function

domain  $x$

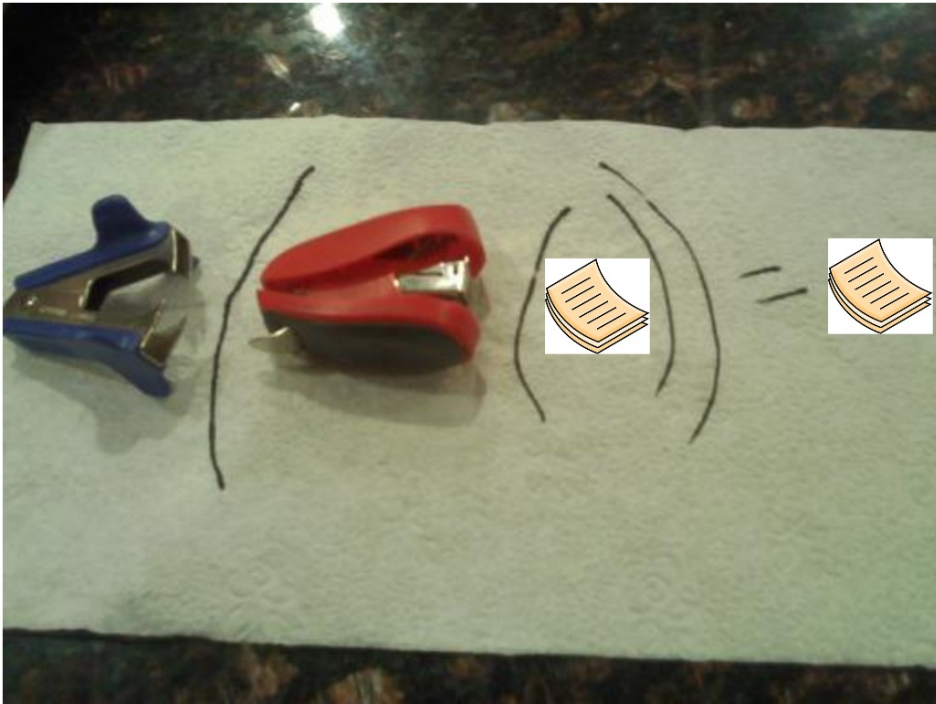
range  $y$

whiteboards

$$x \leftrightarrow y$$

$$f(x) = 2x + 3$$

$$y = 2x + 3$$

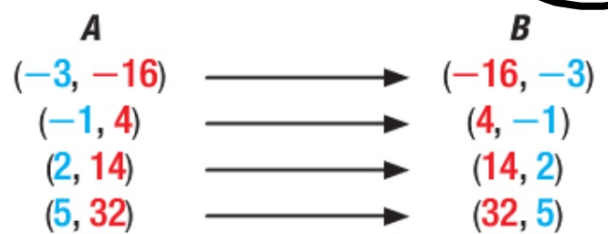


They do the opposite **thing**.... like multiplying and dividing  
...not the same as negative...

### KeyConcept Inverse Relations

**Words** If one relation contains the element  $(a, b)$ , then the inverse relation will contain the element  $(b, a)$ .

**Example**  $A$  and  $B$  are inverse relations.



### Example 1 Inverse Relations

Find the inverse of each relation.

a.  $\{(4, -10), (7, -19), (-5, 17), (-3, 11)\}$

$(-10, 4)$   $(-19, 7)$   $(17, -5)$   $(11, -3)$

b.

<b>x</b>	-4	-1	5	9
<b>y</b>	-13	-8.5	0.5	6.5

$(-4, -13)$   $(-1, -8.5)$

### Guided Practice

1A.  $\{(-6, 8), (-15, 11), (9, 3), (0, 6)\}$

1B.

$x$	-10	-4	-3	0
$y$	5	11	12	15

$(-10, 5)$   
 $(-4, 11)$   
 $(-3, 12)$   
 $(0, 15)$

$(5, -10)$

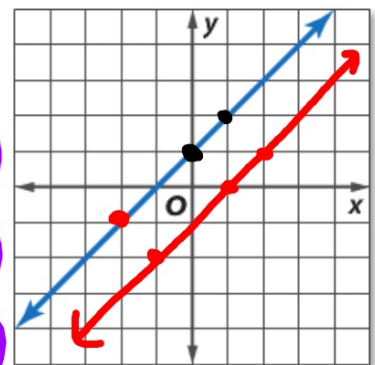
## Example 2 Graph Inverse Relations

Graph the inverse of the relation.

$(1, 2)$   
 $(0, 1)$   
 $(-2, -1)$

$(2, 1)$   
 $(4, 0)$   
 $(-1, -2)$

$(6, 0)$   
 $(4, 2)$   
 $(2, 4)$   
 $(0, 6)$



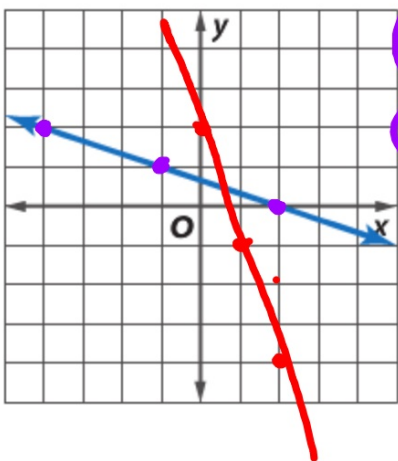
Exchange ordered pairs  
How can I get some from the graph?

Line of symmetry

## Guided Practice

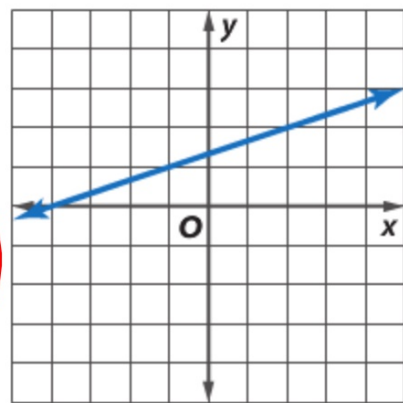
Graph the inverse of each relation.

2A.



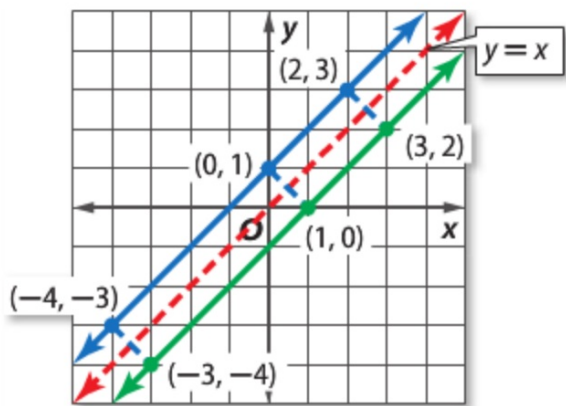
$(2, 0)$   $(0, 2)$   
 $(-1, 1)$   $(1, -1)$   
 $(-4, 2)$   $(2, -4)$

2B.



where is  $y=x$ ?





inverse: reflection over  $y=x$

Writing equations:  
slope-intercept form

function form

WB 4.7 prac 1-7 all

### KeyConcept Finding Inverse Functions

To find the inverse function  $f^{-1}(x)$  of the linear function  $f(x)$ , complete the following steps.

**Step 1** Replace  $f(x)$  with  $y$  in the equation for  $f(x)$ .

**Step 2** Interchange  $y$  and  $x$  in the equation.

**Step 3** Solve the equation for  $y$ .

**Step 4** Replace  $y$  with  $f^{-1}(x)$  in the new equation.

Remember:  $x$  and  $y$  trade places...

To consider: "What is happening to  $x$ ? What would be the opposite thing?"  
...so I should expect to see....

### **Example 3** Find Inverse Linear Functions

**Find the inverse of each function.**

a.  $f(x) = 4x - 8$

**b.**  $f(x) = -\frac{1}{2}x + 11$

### Guided Practice

**3A.**  $f(x) = 4x - 12$

**3B.**  $f(x) = \frac{1}{3}x + 7$