

Algebra 1

8.4

Find squares of sums and differences

Find the product of a sum and a difference

sum

difference

product

EWE

difference of squares

(+) (-)

(+) (+)

(-) (-)

X-factor

What does it mean to square something?

ewe $17^2 = 17 \cdot 17 = 289$
 $100 + 49$

Is $17 = 10 + 7$?

Is $17^2 = (10+7)^2$?
(what is the correct answer?)

Is that the same as $10^2 + 7^2$?

$$\begin{array}{r} x+3 \\ x+3 \\ \hline \end{array}$$

EWE: look for patterns

$$x^2 \quad 3x \quad 9 \quad (x+5)^2 = (x+5)(x+5) = x^2 + 10x + 25$$

$$(x+3)^2 = (x+3)(x+3) = x^2 + 6x + 9$$

$$(x-10)^2 = (x-10)(x-10) = x^2 - 20x + 100$$

$$(x+8)^2 = (x+8)(x+8) = x^2 + 16x + 64$$

$$(x-7)^2 = (x^2 - 14x + 49)(x-7)$$

EWE always!

Example 1 Square of a Sum

Find $(3x + 5)^2$. $(3x + 5)(3x + 5)$

$$\begin{array}{r} 3x + 5 \\ 3x + 5 \\ \hline \end{array}$$

$$\begin{array}{r} 9x^2 + 15x + 15x + 25 \\ \hline \end{array}$$

$$\underline{\underline{9x^2 + 30x + 25}}$$

$$(2x + 6)^2$$

$$4x^2 + 24x + 36$$

$$(5x - 2)^2$$

$$25x^2 - 20x + 4$$

$$(3x + 5)^2 = 9x^2 + 30x + 25$$

Guided Practice

Find each product.

1A. $(8c + 3d)^2$ $64c^2 + 48cd + 9d^2$

$$(5n + 7x)^2$$
$$25n^2 + 70nx + 49x^2$$

$$(10x - 3a)^2 = 100x^2 - 60xa + 9a^2$$

1B. $(3x + 4y)^2$

$$9x^2 + 24xy + 16y^2$$

Example 2 Square of a Difference

Find $(2x - 5y)^2$.

$$-10$$
$$4x^2 - 20xy + 25y^2$$

GuidedPractice

Find each product.

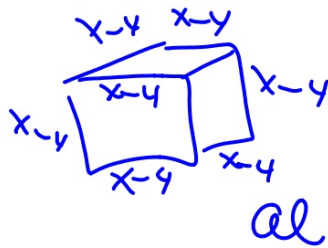
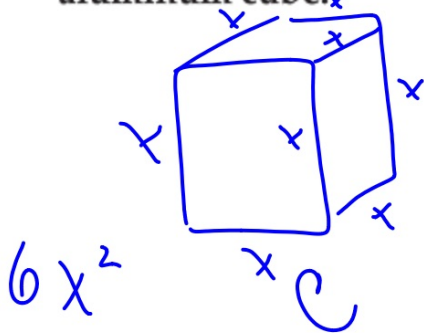
2A. $(6p - 1)^2$

2B. $(a - 2b)^2$

$$x^2 + 10x + 25 = (x + 5)^2$$

Real-World Example 3 Square of a Difference

PHYSICAL SCIENCE Each edge of a cube of aluminum is 4 centimeters less than each edge of a cube of copper. Write an equation to model the surface area of the aluminum cube.



$$6(x-4)^2$$

$$6(x^2 - 8x + 16)$$

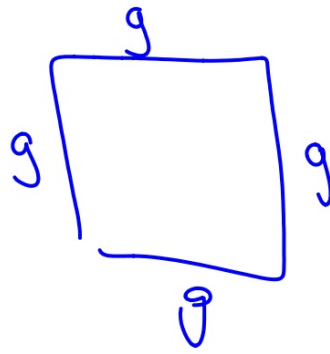
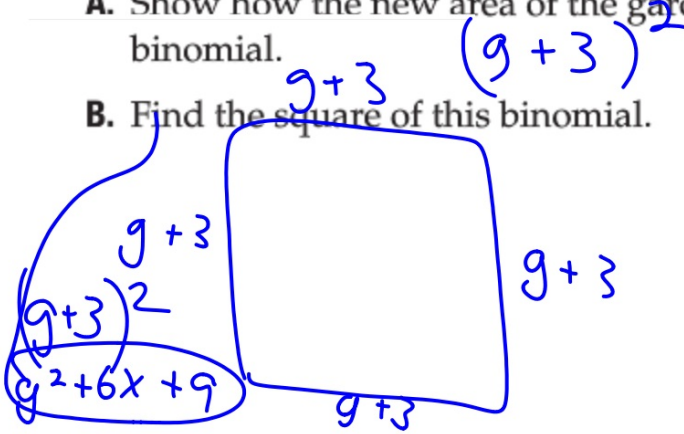
$$6x^2 - 48x + 96$$

Guided Practice

3. **GARDENING** Alano has a garden that is g feet long and g feet wide. He wants to add 3 feet to the length and the width.

A. Show how the new area of the garden can be modeled by the square of a binomial.

B. Find the square of this binomial.



" " Difference of squares: EWE look for a pattern

$$(x + 5)(x - 5) = x^2 - 25$$

$$(x + 3)(x - 3) = x^2 + -9 = x^2 - 9$$

$$(x + 9)(x - 9) = x^2 - 81$$

$$\begin{array}{r} x+5 \\ x-5 \\ \hline x^2 \quad \begin{array}{c} \cancel{5x} \\ \cancel{5x} \end{array} \quad -25 \\ \hline \end{array}$$

Example 4 Product of a Sum and a Difference

Find $(2x^2 + 3)(2x^2 - 3)$.

GuidedPractice

Find each product.

4A. $(3n + 2)(3n - 2)$

4B. $(4c - 7d)(4c + 7d)$