

Algebra 1 8.8

Factor binomials that are the difference of squares

Use the difference of squares to solve equations

difference

factor

solve

whiteboards

Quiz 8.6-8.7

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Look for a pattern...

$$\begin{array}{r} x+5 \\ x-5 \\ \hline x^2 - 5x - 25 \\ +5x \\ \hline x^2 - 25 \end{array}$$
$$\begin{array}{r} a+3 \\ a-3 \\ \hline a^2 - 3a - 9 \\ +3a \\ \hline a^2 - 9 \end{array}$$

↑ ↑

$$\begin{array}{c} x^2 - 49 \\ (x-7)(x+7) \\ x^2 - 49 \end{array}$$

 **KeyConcept** Difference of Squares

Symbols $\underline{a}^2 - \underline{b}^2 = (\underline{a} + \underline{b})(\underline{a} - \underline{b})$ or $(\underline{a} - \underline{b})(\underline{a} + \underline{b})$

Examples $(x^2) - (25) = (x + 5)(x - 5)$ or $(x - 5)(x + 5)$

$t^2 - 64 = (t + 8)(t - 8)$ or $(t - 8)(t + 8)$

$$\begin{array}{c} -25 \\ \diagdown \quad \diagup \\ -5 \quad 5 \\ \diagup \quad \diagdown \\ 0 \end{array}$$

$$\begin{array}{c} -64 \\ \diagdown \quad \diagup \\ 8 \quad -8 \\ \diagup \quad \diagdown \\ 0 \end{array}$$

Is the first thing something squared?
Is the second thing something squared?
Are they subtracted?

$x^2 - 49$ $(x+7)(x-7)$
 $n^2 + 64$ \parallel
 $x^3 - 36$ \parallel
 $4a^2 - 16$ $(2a+4)(2a-4)$

Example 1 Factor Differences of Squares

Factor each polynomial.

a. $16h^2 - 9a^2$

$$(4h + 3a)(4h - 3a)$$

Is the first thing something squared?
Is the second thing something squared?
Are they subtracted?

b. $121 - 4b^2$

$$(11 + 2b)(11 - 2b)$$

Always check for GCF first

$$\begin{aligned} \text{c. } & \frac{27g^3}{3g} - \frac{3g}{3g} \\ & 3g(9g^2 - 1) \\ & 3g(3g + 1)(3g - 1) \end{aligned}$$

Guided Practice

1A. $81 - c^2$

$$(9 + c)(9 - c)$$

1B. $64g^2 - h^2$

$$(8g - h)(8g + h)$$

GCF?

1C. $\frac{9x^3}{x} - \frac{4x}{x}$

$$x(9x^2 - 4)$$

↓

$$x(3x+2)(3x-2)$$

15-43 odds

p. 518

Can it be rearranged?

1D. $-4y^3 + 9y$

$$9y - 4y^3$$

$$y(9 - 4y^2)$$

$$y(3 - 2y)(3 + 2y)$$

When is it finished? Check your answer...can anything be factored again? Watch out for DOS.

Example 2 Apply a Technique More than Once

Factor each polynomial.

a. $b^4 - 16$

esp. diff of squares...
easy to overlook

b. $625 - x^4$

GuidedPractice

2A. $y^4 - 1$

2B. $4a^4 - b^4$

2C. $81 - x^4$

2D. $16y^4 - 1$