

Algebra 1 7.8

Use a recursive formula to list terms in a sequence

Write recursive formulas for arithmetic and geometric sequences

sequence

arithmetic sequence

common difference (d)

geometric sequence

common ratio (r)

combination sequence (could be anything...)

recursive formula

explicit $\$25$
 $+10$
 $= 10x + 25$
 $10(x-1)$



Number of Customers	Cost (\$)
1	\$ 25
2	\$ 35
3	\$ 45
4	\$ 55
5	\$ 65
6	\$ 75

First: break the code. What are they saying?

Example 1 Use a Recursive Formula



Find the first five terms of the sequence in which $a_1 = 7$ and $a_n = 3a_{n-1} - 12$, if $n \geq 2$.

1	7
2	9
3	15
4	53
5	87

↑
1st term
is..

$$= 3(\quad) - 12$$

What's the rule? formula
(helps to say it in words)

a_1 = first term

a_n = next term

$a_{(n-1)}$ = previous term

domain

Can help to use a table

Guided Practice

1. Find the first five terms of the sequence in which $a_1 = -2$ and $a_n = -3a_{n-1} + 4$, if $n \geq 2$.

Table

1	-2	$-3(-2) + 4$
2	10	$-3(10) + 4$
3	-26	
4	82	$-3(-26) + 4$
5	-242	$-3(82) + 4$

First 5

$$a_1 = 7$$

$$a_n = 4a_{n-1} + 6 \quad \text{if } n \geq 2$$

1	7
2	34
3	142
4	574
5	2302

$$4(7) + 6$$

$$4(34) + 6$$

$$4(142) + 6$$

$$4(574) + 6$$

Example 2 Write Recursive Formulas

Write a recursive formula for each sequence.

a. 17, 13, 9, 5, ...

next term = previous term + d

1	17
2	13
3	9
4	5

$$a_1 = 17$$

$$n \geq 2$$

$$a_n = a_{n-1} - 4$$

What's the rule?
what is first term?
d=? (or r=?)
+ d (or x r)

1. What is the rule?
2. State first term
3. State domain $n \geq 2$ (always)

b. 6, 24, 96, 384, ...

1	6
2	24
3	96
4	384

$$a_1 = 6$$

$$a_n = 4 \cdot a_{n-1}$$

$$n \geq 2$$

next term = previous term \times r

Guided Practice

2B. 9, 36, 63, 90, ...

1	9
2	36
3	63
4	90

$$a_1 = 9$$

$$a_n = a_{n-1} + 27$$

$$n \geq 2$$

Example 4 Translate between Recursive and Explicit Formulas

a. Write a recursive formula for $a_n = 6n + 3$.

	$6n+3$	
1	$6 \cdot 1 + 3$	9
2	$6 \cdot 2 + 3$	15
3	$6 \cdot 3 + 3$	21
4	$6 \cdot 4 + 3$	27

1	9
2	15
3	21
4	27

$$a_1 = 9$$

$$a_n = a_{n-1} + 6$$
$$n \geq 2$$

Write out 3 or 4 terms (table?)

Look for the pattern

Write the equation (7.7)

try making a table...

Guided Practice

4A. Write a recursive formula for $a_n = 4(3)^{n-1}$.

	$4(3)^{n-1}$	
1	$4(3)^0$	4
2	$4(3)^1$	12
3	$4(3)^2$	36
4	$4(3)^3$	108

1	4
2	12
3	36
4	108

$a_1 = 4$

$a_n = 3 \cdot a_{n-1}$
 $n \geq 2$

1st term
rule
 $n \geq 2$

$$n \geq 2$$

7, 8 p. 448
11-22 all
↑
a