

Algebra 1 6.2

Solve systems of equations using substitution method

Solve problems using substitution of equations

solve

solve by graphing

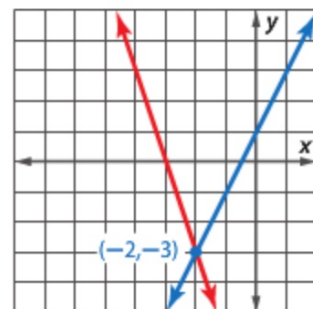


substitution

substitution method

activity: cut & paste
whiteboards

$$x = 2$$
$$y = x + 5$$



Are there ever any complications when solving by graphing?

- recipe: if you run out of one ingredient...
- coach: two players are equally skilled...

$$y = 4x + 5$$
$$13 = 4 \cdot 2 + 5$$
$$13 = 8 + 5$$

Cut & paste activity

$$(x, y)$$
$$(2, 13)$$
$$2x + y = 17$$
$$2 \cdot 2 + 13 = 17$$
$$4 + 13 = 17$$

$$y = 4x + 5$$
$$4 \cdot 2 + 5$$
$$8 + 5$$
$$2x + 4x + 5 = 17$$
$$6x + 5 = 17$$
$$\begin{array}{r} -5 \quad -5 \\ \hline 6x = 12 \\ \frac{6x}{6} = \frac{12}{6} \end{array}$$

$$y = 3 \cdot 3 - 2 = -9 + 2 = -11$$

$$y = 3x - 2$$

$$-11 = 3 \cdot 3 - 2$$

$$-11 = -9 + -2$$

$$2x - y = 5$$

$$2 \cdot (-3) - (-11) = 5$$

$$-6 + 11 = 5$$

$$2x + (3x - 2) = 5$$

$$2x - 3x + 2 = 5$$

$$-x + 2 = 5$$

$$-x = 5 - 2$$

$$-x = 3$$

$$x = -3$$

$$x = -3$$

$$(x, y)$$

$$\Rightarrow (-3, -11) \Rightarrow$$

$$y = 2 \cdot -2 + 1$$

$$= -3$$

Example 1 Solve a system by Substitution



Use substitution to solve the system of equations.

$$y = 2x + 1$$

$$3x + y = -9$$

← **Step 1** The first equation is already solved for y .

$$3x + (2x + 1)$$

$$\begin{array}{r} 5x + 1 = -9 \\ -1 \quad -1 \\ \hline 5x = -10 \\ \frac{5x}{5} = \frac{-10}{5} \end{array}$$

$$3 \cdot -2 + -3 = -9$$

$$-6 + -3 = -9$$

$$= -9$$

$$-3 = 2 \cdot -2 + 1$$

$$-3 = -4 + 1$$

$$(-2, -3)$$

You are the coach...
Who is on the sub list?

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Key Concept Solving by Substitution

- Step 1** When necessary, solve at least one equation for one variable.
- Step 2** Substitute the resulting expression from Step 1 into the other equation to replace the variable. Then solve the equation.
- Step 3** Substitute the value from Step 2 into either equation, and solve for the other variable. Write the solution as an ordered pair.

$$y = 3x - 2 \quad y = 2x - 5$$

$$3x - 2 = 2x - 5$$

$$\begin{array}{r} -2x \\ \hline \end{array}$$

$$\begin{array}{r} x - 2 = -5 \\ +2 \quad +2 \\ \hline \end{array}$$

$$x = -3$$

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$$-2 = 4 \cdot 1 - 6$$

Guided Practice

$$-2 = 4 + -6$$

1A. $y = 4x - 6$

$$5x + 3y = -1$$

$$5x - y = -1$$

$$5x - (4x - 6) = -1$$

$$5 \cdot 1 + 3 \cdot -2 = -1$$

$$5 + -6 = -1$$

$$5x + 3(4x - 6) = -1$$

⇐

$$5x + 12x - 18 = -1$$

$$(1, -2) \quad \color{red}{\smile}$$

$$17x - 18 = -1$$

$$17x = 17$$

$$x = 1$$

1B. $2x + 5y = -1$
 $y = 3x + 10$

How is this problem different?

Example 2 Solve and then Substitute

Use substitution to solve the system of equations.

$$\begin{aligned}x + 2y &= 6 \\ 3x - 4y &= 28\end{aligned}$$

GuidedPractice

2A. $4x + 5y = 11$
 $y - 3x = -13$

2B. $x - 3y = -9$
 $5x - 2y = 7$