

Trig 9.2

Graph polar equations
Solve systems of polar equations

rose

lemniscate

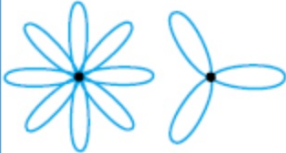

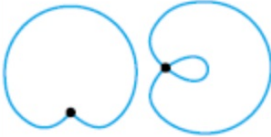


limacon

cardioid

spiral of Archimedes

activity: polar graphs and gallery walk

Classical Curves

| Curve | rose | lemniscate <i>(pronounced leh-m NIHS kuh-t)</i> | limaçon <i>(pronounced lee muh SOHN)</i> | cardioid <i>(pronounced KARD ee oyd)</i> | spiral of Archimedes <i>(pronounced ar kih MEED eez)</i> |
|-----------------------|---|---|--|---|---|
| Polar Equation | $r = a \cos n\theta$ $r = a \sin n\theta$ <i>n is a positive integer.</i> | $r^2 = a^2 \cos 2\theta$ $r^2 = a^2 \sin 2\theta$ | $r = 3 + 2 \cos \theta$ $r = a + b \sin \theta$ | $r = a + a \cos \theta$ $r = 5 + 5 \sin \theta$ | $r = a\theta$ (θ in radians) |
| General Graph |  |  |  |  |  |

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Graph the system of polar equations. Solve the system using algebra and trigonometry and compare the solutions to those of your graph.

$$r = 3 - 3 \sin 210$$

$$r = 3 - 3(-\frac{1}{2})$$

$$r = 3 - 3 \sin 330$$

$$= 3 - 3(-\frac{1}{2})$$

$$= 3 + 1.5$$

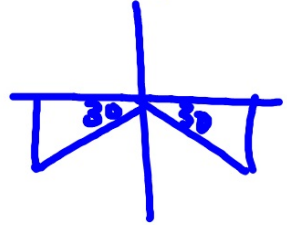
$$r = 3 - 3 \sin \theta \quad 3 + 1.5$$

$$r = 4 - \sin \theta \quad 4.5$$

$$\begin{array}{r} 3 - 3 \sin \theta = 4 - \sin \theta \\ -3 + \sin \theta \quad -3 + \sin \theta \end{array}$$

$$\frac{-2 \sin \theta}{-2} = \frac{1}{-2}$$

$$\sin \theta = -\frac{1}{2}$$



(r, Θ)

(4.5, 210°) ←

(4.5, 330°)

$$3.9^2 + 2.25^2 = r^2$$

11-210
2.5

26. $r = 1 + \cos\theta$
 $r = 1 - \cos\theta$

$(1, 90^\circ)$
 $(1, 270^\circ)$