

Algebra 1 9.2

Solve quadratic equations by graphing

Estimate quadratic solutions by graphing

integer

Solution

Root

x-intercept ←  $-\frac{b}{2a}$   $x =$  cross x-axis

Double root

standard form

equation

related function

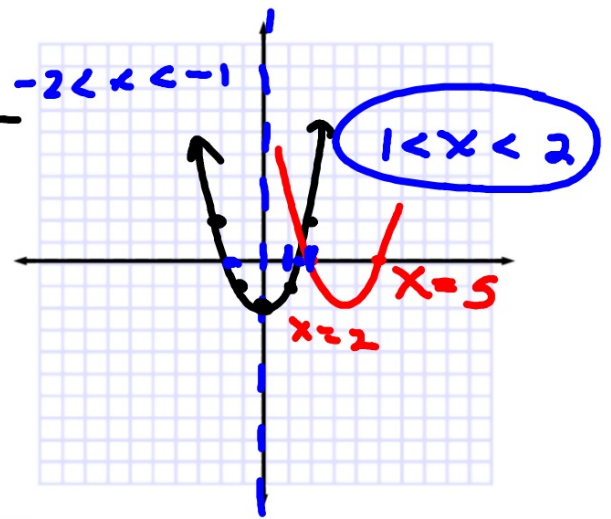
Whiteboards

Where does the graph cross the x-axis?  
 What is true about the y-coordinate there?

$$y = x^2 - 2$$

$$x = \frac{-b}{2a}$$

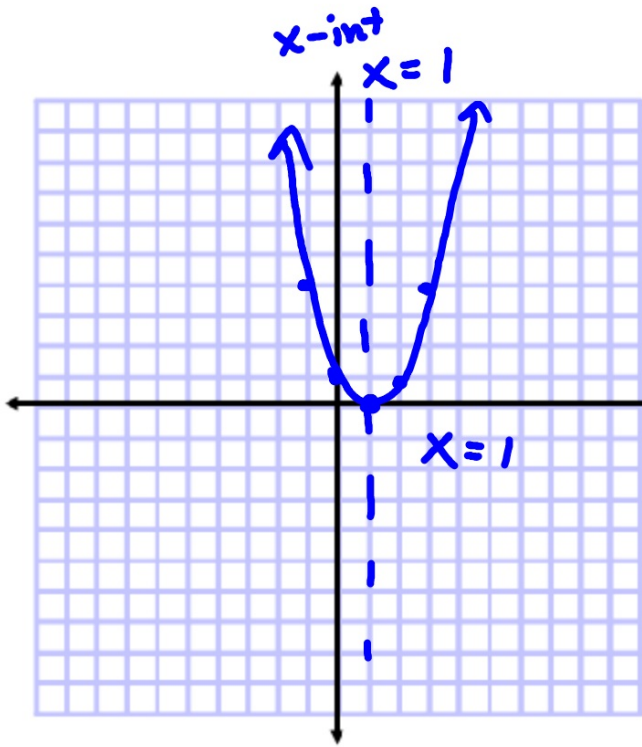
	$x^2 - 2$	
0	0 - 2	-2
1	1 - 2	-1
2	4 - 2	2

$$\frac{0}{2 \cdot 1} = 0$$


**Key Concept** Solutions of Quadratic Equations

two unique real solutions      one unique real solution      no real solutions

"double root"



$$y = 1x^2 - 2x + 1$$

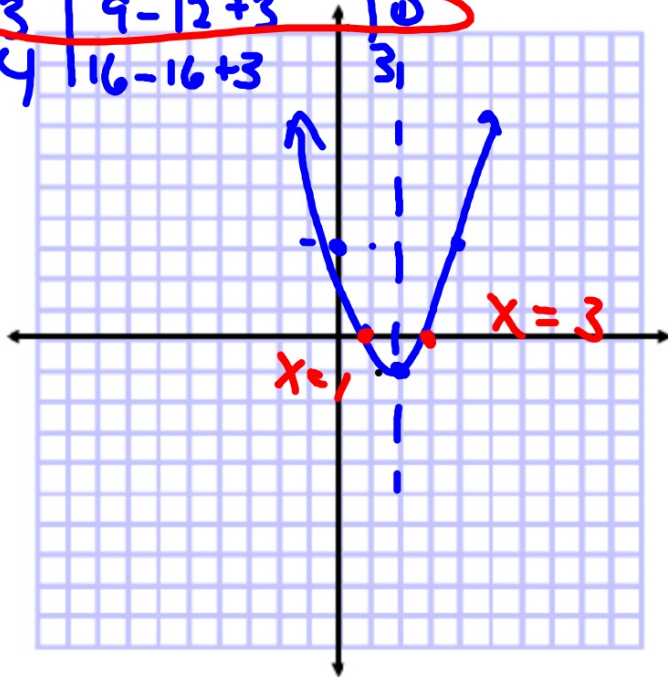
$$x = \frac{2}{2 \cdot 1} = 1$$

	$x^2 - 2x + 1$	
1	$1 - 2 + 1$	0
2	$4 - 4 + 1$	1
3	$9 - 6 + 1$	4

**Guided Practice** Solve each equation by graphing.

$$x = \frac{4}{2 \cdot 1} = 2$$

x	$x^2 - 4x + 3$	
2	$4 - 8 + 3$	-1
3	$9 - 12 + 3$	0
4	$16 - 16 + 3$	3



1B.  $x^2 - 4x + 3 = 0$

~~$y = -x^2 - 4x + 3$~~   $x^2$   $\cup$   
 $-x^2$   $\cap$

Does it open up or down?

Function form ( $y =$ )

$x = -b/2a$  etc.

Table of values

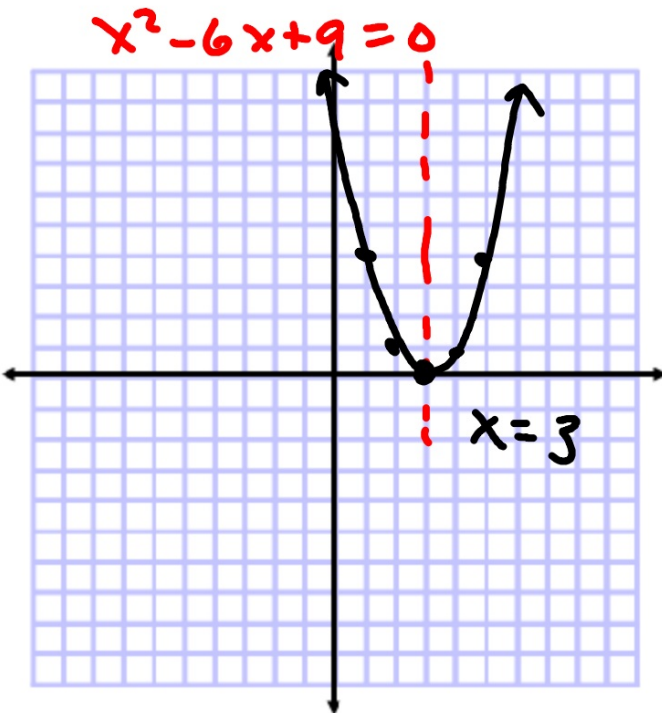
Answer the question

Solve: where does it cross x-axis?

hint: y-coordinate there is 0

### Example 2 Double Root

Solve  $x^2 - 6x = -9$  by graphing.  
 $+9 +9$



Change to  $=0$  (if necessary)

Open up or down?

Use function form ( $y=$ ) for graphing

Answer the question

If your graph is inaccurate...

$$y = x^2 - 6x + 9$$

$$x = \frac{6}{2 \cdot 1} = 3$$

	$x^2 - 6x + 9$	
3	$9 - 18 + 9$	0
4	$16 - 24 + 9$	1
5	$25 - 30 + 9$	4

Guided Practice

Rearrange (if necessary)  
Change to function form

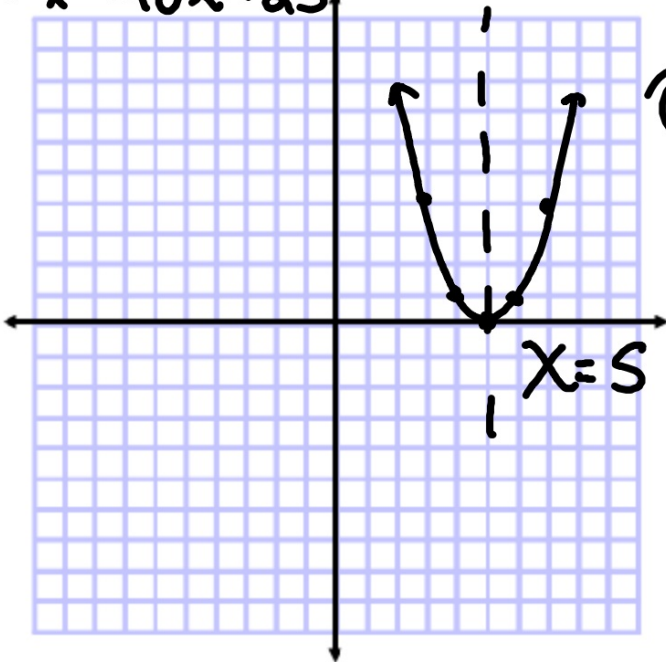
Solve each equation by graphing.

2A.  $x^2 + 25 = 10x$   
 $-10x \quad -10x$

$x = \frac{10}{2} = 5$

2B.  $x^2 = -8x - 16$

$y = x^2 - 10x + 25$

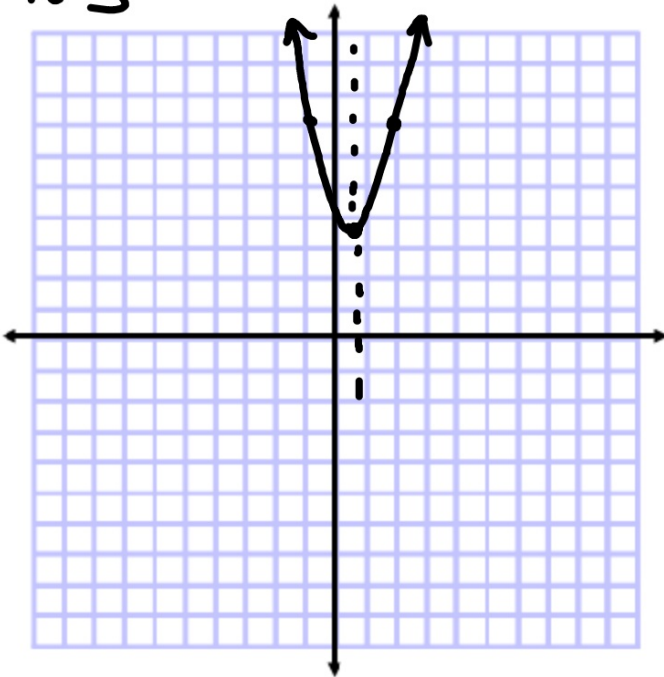


	$x^2 - 10x + 25$	
5	$25 - 50 + 25$	0
6	$36 - 60 + 25$	1
7	$49 - 70 + 25$	4

**Example 3** No Real Roots

Solve  $2x^2 - 3x + 5 = 0$  by graphing.

NS



$$x = \frac{3}{4} = 0.75$$

x	$2x^2 - 3x + 5$	
0.75	$2(.75)^2 - 3(.75) + 5$ $1.125 - 2.25 + 5$	3.9
2	$2 \cdot 4 - 3 \cdot 2 + 5$ $8 - 6 + 5$	7

complex number

Solve each equation by graphing.

NS

PSS8 11-29.0

3A.  $-x^2 - 3x = 5$

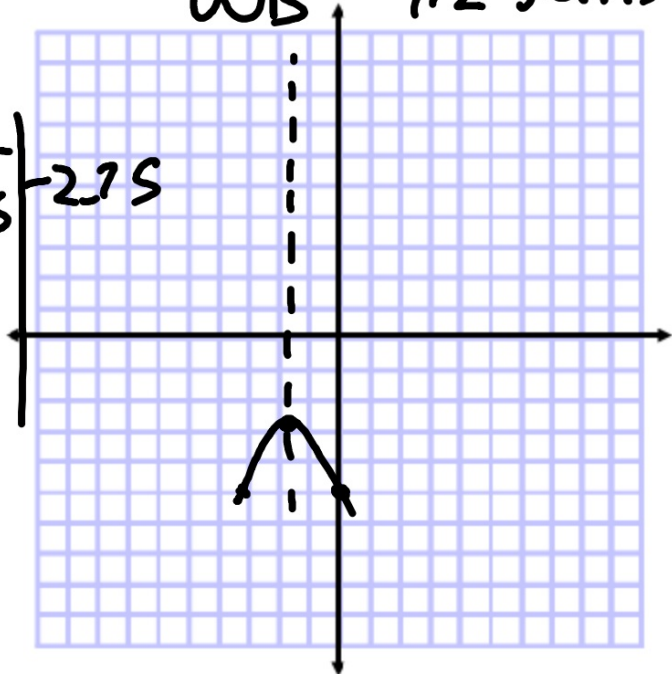
$x = \frac{3}{-2}$

WB 9.2 skills 1-8

$y = -x^2 - 3x - 5$

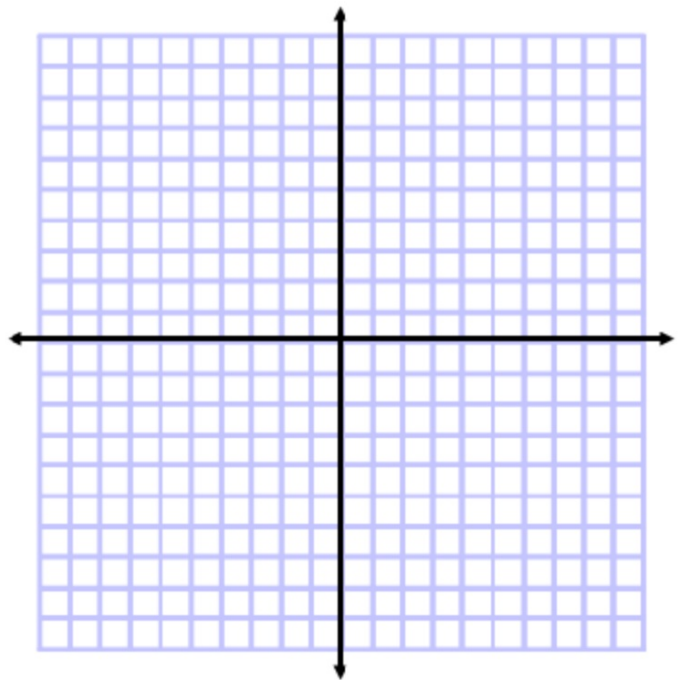
$-1 \cdot x \cdot x$

-1.5	$-1(-1.5)(-1.5) - 3(-1.5) - 5$	-2.25
0	$-0^2 - 3 \cdot 0 - 5$	-5





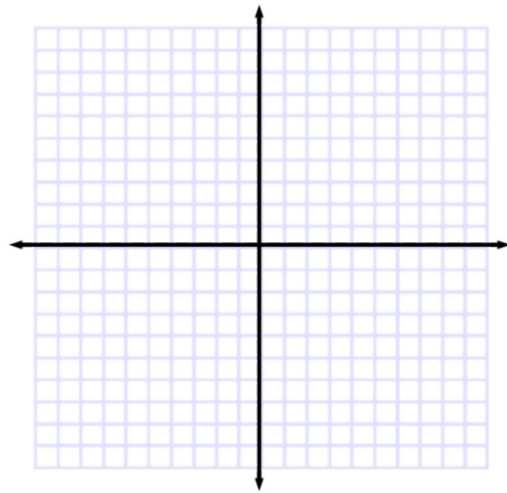
3B.  $-2x^2 - 8 = 6x$



What if the answer isn't an integer?

What is it between?

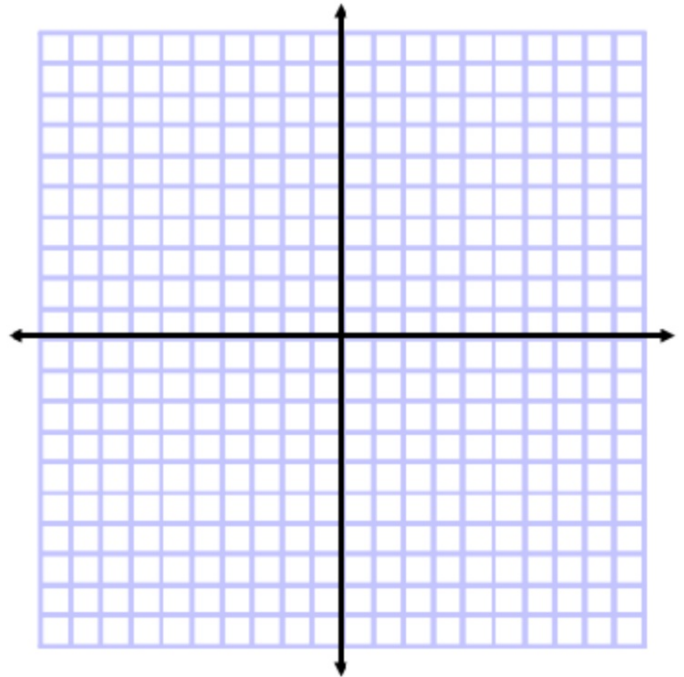
$$y = x^2 + 3x - 1$$



**Example 4** Approximate Roots with a Table

Solve  $x^2 + 6x + 6 = 0$  by graphing. If integral roots cannot be found, estimate the roots to the nearest tenth.

if not integers...  
what is it between?  
vs  
nearest tenth?



**Guided Practice**

4. Solve  $2x^2 + 6x - 3 = 0$  by graphing. If integral roots cannot be found, ~~estimate~~  
~~the roots to the nearest tenth.~~

What is it between?  
vs  
nearest tenth?

